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AFCRL Atmospheric Absorption Line Parameters Compilation

R.A. McCLATCHEY
W.S. BENEDICT *
S.A. CLOUGH
D.E. BURCH †
R.F. CALFEE
K. FOX ‡
L.S. ROTHMAN
J.S. GARING

- * University of Maryland
- † Philco Ford Corporation
- ‡ University of Tennessee

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AFCRL Atmospheric Absorption Line Parameters Compilation

I. INTRODUCTION

About 10 years ago a program was initiated to compile spectroscopic data on individual vibration-rotation lines of water vapor in the 2.7 μm region (Gates, et al, 1964).

This work continued resulting in a publication on the 2.05 and 2. 7 μm bands of carbon dioxide (Calfee and Benedict, 1966) and a third publication on the 1.9 and 6.3 μm bands of water vapor (Benedict and Calfee, 1967). Other workers have published similar results on the 15 pm bands of CO_2 (Drayson and Young, 1967). the 9.6 μm bands of O_3 (Clough and Kneizys, 1965), the CO bands whose fundamental is near 5 μm (Kunde. 1967). the CH_4 bands near 3 and 7.5 μm (Kyle, 1968) and the unpublished rotational water data calculated by Benedict and Kaplan in 1959 (see Goody, 1964, p. 184).

About 5 years ago an effort was initiated at AFCRL to continue this work with the aim of providing a complete **set** of data for all vibration-rotation lines of all naturally occurring molecules of significance in the terrestrial atmospheres. With such data at hand, it would **be** possible to compute the transmittance appropriate for atmospheric paths by first computing the monochromatic transmittance many times in a finely spaced frequency grid and then degrading the results to any appropriate spectral resolution. Up to now the following molecules have been included in this compilation: (1) water **vapor**; (2) carbon dioxide; (3) ozone; (4) nitrous oxide; (5) carbon monoxide; (6) methane; and (7) oxygen.

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All of these molecules except oxygen are **minor** constituents of the atmosphere, but nonetheless represent most **of** the **absorption lines** in the visible and infrared. Although there is some evidence **for decreasing** concentration with height of N_2O , CO, and CH_4 , it is probably reasonable for most purposes to assume that all of these **gases** except H_2O , and O_3 are uniformly mixed by volume in the atmosphere unless other specific information is available. Table 1 provides concentrations and references for these "uniformly mixed gases". Water vapor and ozone are, of course, not uniformly mixed and an appropriate set of models useful in considering the radiation effects of these gases is provided by **McClatchey**, et al, 1972.

| Constituent | ppm by volume | Reference |
|------------------|------------------------------|-------------------------|
| CO ₂ | 336 | Fink etal,1964 |
| N ₂ O | 0.28 | Birkland and Shaw, 1959 |
| co | 0.075 | Shaw. 1968 |
| CH₄ | 1.6 | Goody, 1964 |
| 0, | 2.10 x 10⁵ | Valley, 1965 |

-Table 1. Concentrations of Uniformly Mixed Gases in Dry Air

2. **DESCRIPTION OF COMPILATION**

In order to compute the transmittance due to a given spectral line in the **atmos** sphere it is necessary to describe the absorption coefficient as a function of **frequency** for each line. The four essential line parameters for each line are the resonant **frequency**, ν_{o} (cm⁻¹), the intensity per absorbing molecule, $S(cm^{-1})$ molecule cm⁻²) the Lorentz line width parameter, α_{o} (cm⁻¹/atm), and the energy of the lower state, $E''(cm^{-1})$. The frequency, ν_{o} , is independent of both temperature and pressure (except for possibly very small pressure effects of less than 0.01 cm⁻¹/atm, which have been ignored here). The intensity, S, is pressure -independent, and, as discussed below, its temperature dependence can be calculated from E'' and ν

The line half-width 'at half maximum, α , is by definition proportional to the pressure, p, and its temperature dependence can be estimated as discussed below.

The precise line shape is a matter of some uncertainty, but in the derivation of line parameters' from laboratory measurements, it is customary to start from the Lorentz shape (see Goody, 1964) given in Eq. (1).

$$k(\nu) = \frac{S\alpha}{\pi(\nu - \nu_0)^2 + \alpha^2}$$

$$S = \int k(\nu) d\nu$$
(1)

The validity of Eq. (1) to describe the true line shape is subject to two limitations. The first, which can be precisely estimated and corrected for by the use of the Voigt shape, occurs when $\alpha_{o} P/\alpha_{D} < 1.0$ where α_{D} is the doppler line width which varies with frequency, temperature and molecular mass as given in Eq. (2).

$$\alpha_{D} = \frac{\nu}{c} \left(\frac{2kT}{m} \right)^{1/2} = 4.298 \times 10^{-7} \nu (T/M)^{1/2}$$
 (2)

where M = molecular weight and here k = **Boltzmann's** constant and m = mass of a molecule.

For atmospheric molecules and infrared frequencies, modifications of the Lorentz shape begin to be required at pressures below 10 to 100 mb.

The second limitation concerns possible inadequacies of the Lorentz shape, especially in the distant wings of a line ($|\nu - \nu_0| >> a$) (see Winters et al, 1964. and **Burch** et al, 1969) or when the long-range intermolecular forces responsible for collision broadening are dipole-quadrupole, leading to an exponent 1.75 rather than 2.0 for ($\nu - \nu_0$), (Varanasi, 1972). Throughout this **compilation** we assume the validity of the Lorentz exponent.

The line intensity is temperature dependent through the Boltzmann factor and the partition function as indicated in Eq. (3) (the induced emission term has intentionally been omitted here),

$$S(T) = \frac{S(T_s) Q_v(T_s) Q_r(T_s)}{Q_v(T) Q_r(T)} \exp_+ \left[\frac{1.439E''(T-T_s)}{TT_s} \right]$$
(3)

where $\mathbf{E''}$ (in cm⁻¹) is the energy of the lower state of the transition and where $\mathbf{Q_v}$ and $\mathbf{Q_r}$ are the vibrational and rotational partition functions. The vibrational partition functions for the most abundant isotopes are given in Table 2. Partition functions for the other isotopes are similar. The 'temperature dependence of the rotational partition function is given by $(\mathbf{T}/\mathbf{T_g})^{\mathbf{J}}$ where j is also provided in Table 2 $(\mathbf{T_g})^{\mathbf{J}}$ is taken to be $\mathbf{296^{\circ}K}$).

It is also necessary to know the temperature variation of **a.** In the absence of specific indications discussed under each molecule, the equation $\alpha(T)/\alpha(T_g) = (T/T_g)^{-n}$, with n = 1/2, corresponding to the assumption of temperature-independent collision diameters, may be made. The validity of the assumption is more uncertain, the larger the dependence of the diameter on the particular rotation-vibration transition, (that is, it is most unrealistic for H_2O and the low-J transitions of the other molecules). The theory of Tsao and Curnutte (1954) when applied to the determination of line width for H_2O lines gives a wide variation of n about the mean value of 0.62 (Benedict and Kaplan, 1959). Measurements made with a CO_2 laser (Ely and McCubbin, 1970) indicate a value of n = 1.0 for the P2O line of the P2O line of the P2O land.

| Molecule | j | Tempera - ture | 175 | 200 | 225 | 250 | 275 | 296 | 325 |
|------------------|-----|-------------------|--------|--------|--------|--------|--------|--------|--------|
| $_{ m H_2O}$ | 1.5 | | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.001 |
| CO2 | 1.0 | | 1.0095 | 1.0192 | 1.0327 | 1.0502 | 1.0719 | 1.0931 | 1.1269 |
| 03 | 1.5 | | 1.004 | 1.007 | 1.013 | 1.022 | 1.033 | 1.046 | 1.066 |
| N ₂ O | 1.0 | | 1.017 | 1.030 | 1.048 | 1.072 | 1.100 | 1.127 | 1.170 |
| co | 1.0 | | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| CH ₄ | 1.5 | | 1.000 | 1.000 | 1.001 | 1.002 | 1.004 | 1.007 | 1.011 |
| O_2 | 1.0 | | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.001 |

An examination of Eqs. (1) and (3) indicates that it is necessary to know the ν_0 , $S(T_g)$, $\alpha(P_0, T_g)$ and E'' value for each line in order to compute a spectrum. The data compilation described here contains these **four** quantities for each **of** the more than 100,000 lines between 1 μ m and the far infrared belonging to the seven molecular species listed in Table 3. Additional identifying information is also supplied for each line **as** indicated below.

Table 3. Intensity Criteria for Lines Included in Compilation

| Molecule | Identification No. | Criterion Intensity* Minimum at T=296K | Existing Intensity Minimum at T=296K |
|------------------|--------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------|
| H ₂ O | 1 | 3 × 10 ⁻²⁷ 2.2 × 10 ⁻²⁶ 3.5 × 10 ⁻²⁴ 3.0 × 10 ⁻²³ 8.3 × 10 ⁻²³ 3.3 × 10 ⁻²⁴ 3.7 × 10 ⁻³⁰ | 3 x 10'27 |
| CO ₂ | 2 | | 3.7 x 10 ⁻²⁷ |
| O ₃ | 3 | | 3.5 x 10 ⁻²⁴ |
| N ₂ O | .4 | | 4.0 x 10 -23 |
| ○ ○ | 5 | | 1.9 X 10 ⁻²³ |
| CH ₄ | 6 | | 3.3 x 10 ⁻²⁴ |
| O ₂ | 7 | | 3.7 x 10 ⁻³⁰ |

^{*}Units are cm⁻¹/(molecule-cm⁻²)

In order to establish the "Criterion Intensity Minimum" values given in Table 3, an extreme atmospheric path was considered, assuming the gas concentrations specified in Table 1 and maximum concentrations over the path of 3 X 10^{24} molecules/cm² for water vapor and 1 x 10^{20} molecules/cm² for ozone. This extreme radiation path was the atmospheric path tangent to the earth's surface, and extending from space to space. Using this criterion, lines yielding less than 10 percent absorption at the line center would normally be omitted.

Although this absolute line intensity cutoff was established, it has not always been possible to achieve. In some cases it would have been unrealistic to push calculations to this limit when experimental confirmation fell far short. There are two specific areas in which this absolute cutoff has been violated: (1) In regions of very strong absorption, very weak lines above this absolute limit have been neglected; (2) Q-branch lines below this limit have occasionally been included where it is felt that the accumulation of many weak, closely spaced lines would still produce an appreciable absorption under some atmospheric circumstances. In some cases, (for example, ${\bf CO_2}$), sufficient laboratory measurements and theoretical work were available so that this limit was exceeded throughout the infrared.

In the past, line intensities have been defined in various units, different for each molecular species. It was common to define water vapor concentration in precipitable cm, or ${\rm g/cm}^2$, in the path in question. On the other hand, the amount of ${\rm CO}_2$ and the other uniformly mixed gases in a path were often given in cm-atm of gas at STP. In order to unify the units and ultimately to lead to less confusion, we decided to use the more fundamental quantity, molecules/cm² as a measure of absorbing gas abundance along the path. The appropriate conversion factors are:

1 (cm-atm)_{STP} =
$$2.69 \times 10^{19}$$
 molecules/cm²
1 g/cm² of $H_2O = 3.34 \times 10^{22}$ molecules /cm².

It was also decided, as indicated in Table 3, to define line (and band) intensities at 296°K, the normal room temperature at which most measurements are made. Intensities of all bands are based on the total number of molecules of a given species of all isotopes in their normal abundance, not on the number of the particular isotope responsible for a given band. Isotopic abundance values for all molecules for which data are provided in the compilation are given in Table 4.

Half-widths of lines have been added where available. Details are discussed in the separate sections on individual molecules. In some cases, it is felt that insufficient data exist to warrant the inclusion of a variable half-width. In these cases, a mean, constant value has been inserted for each molecular species and values are given in Table 5.

A shorthand notation was adopted to identify the various isotopic species. It is easy to understand by considering the following examples for CO_2 : $^{16}O^{12}C^{16}O \equiv 626$, $^{16}O^{12}C^{16}O \equiv 636$, and for N_2O , $^{14}N^{1}N O^{16} \equiv 456$, etc. This same type of code is used for the other five molecules.

Table 4. Isotopic Abundances

| H ₂ O | 161 162 181 171 | 0.99729 0.000300 0.00204 0.000370 | CH₄ CH₃D | 211 311 212 | 0.98815 0.01110 0.00060 |
|------------------|-----------------------------------------------|-------------------------------------------------------------------------------------|----------------|-------------------|-------------------------------|
| CO2 | 626 636 628 627 638 637 828 | 0.98414 0.01105~ 0.00402 0.000730 0.0000452 0.00000820 0.00000412 | O ₂ | 66 68 67 | 0.99519 0.00407 0.00074 |
| 03 | 666 668 686 | 0.99279 0.00406 0.00203 | | | |
| N ₂ O | 446 456 546 448 447 | 0.99022 0.00368 0.00368 0.00202 0.00037 | | | |
| СО | 26 36 28 27 | 0.98652 0.01107 0.00202 0.000369 | | | |

Table 5. Mean Half-width Values

| Molecule | Half-width (cm ⁻¹ /atm) | References |
|--------------------------------------------------------------------------|------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------|
| CO ₂ O3 N ₂ O CO CH ₄ O2 | 0.07 0.11 0.08 0.06 0.055 0.060 | Yamamoto et al (1969) Lichtenstein et al (1971) Toth (1971) Bouanich and Haeusler (1972) Varanasi (1971) (see Section 6.3) Burch and Gryvnak (1969) |

A standard computer format was adopted for card or card-image input and is outlined below, the numbers between vertical lines representing the columns on an IBM card, and the letter-number combinations representing the computer format.* The first four quantities are: ν = frequency in

| <u>v</u> | S | α | E" | Rotation and Vibration ID | Date | Isotope | Molecule |
|----------|----------------|---|----------------|---------------------------|-------------|-------------|-------------|
| | 11-20 E10.3 | | 26-35 F10.3 | 36-70 5A6, A5 | 71-73 13 | 74-77 14 | 78-80 13 |

^{*}In the far infrared (ν < 100 cm-') a different format (F10.6) was occasionally chosen for the frequencies where high accuracy microwave measurements are available.

wavenumbers, S = line intensity in cm^{-1} /molecule -cm $^{-2}$ at 296° K, $\alpha = line$ half-width in cm $^{-1}$ atm at 296° K, E'' = energy of the lower state expressed in wavenumbkrs. The rotation and vibration identification are the most difficult to unify due to the differences in the quantum numbers required to define the upper and lower states for different kinds of molecules. The columns 36 through 70 are indicated below for water and ozone, both triatomic asymmetric molecules, where (') indicates upper state and ('') indicates the lower state.

J',
$$K_{\mathbf{a}}'$$
, $K_{\mathbf{c}}'$ J'', $K_{\mathbf{a}}''$, $K_{\mathbf{c}}''$ $v'_{1}v'_{2}v'_{3}$ $v_{1}''v_{2}''v_{3}''$

313 1x 313 2x 312 1x 312 1x

On the other hand, the quantum numbers specified for ${\rm CO_2}$ and ${\rm N_2O}$ between columns 36 and 70 are given below, where again (') indicates upper state and ('') indicates lower state, and where ${\bf r}$ refers to Fermi resonance (see section on ${\rm CO_2}$ for more details). The identification system for methane differs from those described here and is described in the section on methane.

$$v'_1v'_2 \ell'v'_3r'$$
 $v''_1v''_2 \ell''v''_3r''$ P(J''+1)
2x 5x 512 A8

The remaining fields specified above include the entry date of the datum (important primarily for our purposes), the isotopic code as described above, and the molecular identification as given in Table 3.

This work has now proceeded to the point where most of the data consistent with the above -mentioned line intensity limitation are fairly complete in the 1 μ m to 100 μ m region. The nature of the remaining uncertainties and omissions is discussed in the sections to follow. The data are frequency ordered on magnetic tape and are contained in records of 321 ten-character words per record. An initial control word indicates the number of words to follow (320 for a full record). Each such record contains 40 card images in the format described above. Thus, it is necessary after reading a record from the tape to decode it according to the format 110, 40 (F10.3, E10.3, F5.3, F10.3, **5A6**, A5, 13, 14, 13). In order to aid those using other than Control Data Corporation equipment, Table 6 is provided. The column headed "External BCD Code" indicates the character representation actually used on the tape. If a computer having a different character code is being used, a simple cross-referencing program must be constructed. End of file markers are placed on the tape at the following frequency points: **500**, **1000**, **2000**, **5000**, **7500**, **10**, **000** cm $^{-1}$ with a double end of file appearing at the end of the tape.

In Appendix A we have included a listing of a computer program for directly reading the tape on a CDC 6600 computer. (No card decks are available.) For other computer systems the used is left to his own devices. Appendix B provides a computer program and output for generating a synthetic spectrum for a constant pressure path.

Table 8. CDC 8000 Series Fortran Character 'Codes*

| Source | Console | External | Punch Position |
|--------------|----------|-----------------|-----------------------|
| Language | Display | BCD | in a Hollerith |
| Character | Code- | Code | Card Column |
| | Code | Code | Cara Column |
| A | 01 | 61 | 12-l |
| В | 02 | 62 | 12-2 |
| Č | 03 | | 12-2 12-3 |
| 5 | | 63 | |
| ם | 04 | 64 | 12-4 |
| E | 05 | 65 | 12-5 |
| F | 06 | 66 | 12-6 |
| G | 07 | 67 | 12-7 |
| н | 10 | 70 | 12-8 |
| l i | 11 | 71 | 12-9 |
| J | 1.2 | $4\overline{1}$ | 11-l |
| ĸ | 13 | 42 | 11-2 |
| L | 14 | 43 | 11-3 |
| M | 15 | 44 | 11-3 |
| | | 44 4 5 | 11-4 11-5 |
| N | 16 | | |
| O O | 17 | 46 | 11-6 |
| P | 20 | 47 | 11-7 |
| Q R | 21 | 50 | 11-8 |
| R | 22 | 51 | 11-9 |
| S | 23 | 22 | o-2 |
| T | 24 | 23 | о-3 |
| U | 25 | 24 | 0-4 |
| l v | 26 | 25 | 0-5 |
| w | 27 | 26 | 0-6 |
| X | 30 | 27 | 0-7 |
| Y | 31 | 30 | 0-8 |
| Ż | 32 | 31 | 0-9 |
| ő | 33 | 12 | 0-9 |
| 1 | 33 34 | 01 | 1 |
| 1 1 | 34 | 01 | i |
| 2 | 35 | 02 | 2 3 |
| 3 | 36 | 03 | 3 |
| 4 | 37 | 04 | 4 |
| 5 | 40 | 05 | 5 |
| 6 | | 0 6 | 4 5 8 7 |
| 7 | 42 | 07 | 7 |
| . 8 | 43 | 10 | 8 |
| 9 | 44 | 11 | 9 |
| + | 45 | 60 | 12 |
| - | 46 | 40 | 11 |
| * | 47 | 54 | 11-8-4 |
| l ' / | 50 | 21 | o-1 |
| l i | 51 | 34 | 0-8-4 |
| l j | 52 | 74 | 12-8-4 |
| \$ | 53 | 53 | 11-8-3 |
| Ψ = | 54 | 13 | 8-3 |
| blank(space) | 55 | 20 | |
| orank(space) | 56 | 20 33 | space 0-8-3 |
| , | | აა 70 | U-0-3 1000 |
| | 57 | 73 | 12-8-3 |

^{*}Taken from Control Data 6400/6500/6600 Fortran Reference Manual, Publication No. 60174900 Rev. C (1968) Control Data Corporation

Interested parties can obtain a copy of the data tape described here by mailing a new, 7-track, 800 **BPI** certified, 2400 ft long by **1/2** in. wide, magnetic tape to R. A. **McClatchey**, AFCRL **(OPI)**, L. G. Hanscom Field, Bedford, Ma. 01730.

Due to the large amount of material included on this tape and the likelihood of errors, it is clear that the ultimate test of the accuracy and completeness of the data will be its use by many people in the scientific community. Therefore, we ask the cooperation of all who use these data to keep us informed of any apparent errors or omissions. We would appreciate the receipt of new laboratory data or theoretical work related to improving the data. We will then update this tape as sufficient new or revised data become available.

3. GENERAL REMARKS ON THE DERIVATION OF PARAMETERS

The four tabulated parameters, ν_0 , $E^{"}$, S, and α must of course be derived from experimental observations, subjected to data reduction in the framework of the general theories of molecular spectroscopy. For the basic theory we refer the reader to such textbooks as Herzberg (19 50) and Goody (1964). The complexity needed to approach the problem depends both on the type of molecule and the accuracy of the observational data. We here outline the equations and methods used for the general types of molecules, linear triatomic (and diatomic) CO_2 , N_2O and CO; nonlinear triatomic, CO_2 , CO0 and CO1, where unpaired electrons complicate the rotational structure of the ground and excited electronic states.

The energy states and the transition probabilities between energy states of the molecules are defined primarily by their numerical values as established by experiments and by the indices (quantum numbers) which identify them. In nearly all the cases of interest, mathematical relations of greater or lesser complexity relate the numerical properties to the quantum numbers. We here present the general relations used to generate the tabulated data. The specific data and exceptional cases are discussed later for each molecule.

3.1 Energy Levels and Line Positions

3.1.1 LINEAR MOLECULES

For the triatomic linear molecules CO_2 and N_2O , the vibrational states are characterized by three quantum numbers, which are zero or positive integers, of pure vibration, vl, v_2 , and v_3 and a fourth number $l_2 = v_2, v_2 - 2 \dots$ which represents the contribution of the bending mode to the angular rotation. In order to calculate the purely vibrational part of the energy ("the band origins"), it is neces-sary first to compute an unperturbed energy,

$$G_{\mathbf{v}}^{\mathbf{unp}}$$
, by: $G_{\mathbf{v}}^{\mathbf{unp}} = \sum_{\mathbf{i}} \omega_{\mathbf{i}}^{\mathbf{vi}} + \sum_{\mathbf{i}\mathbf{j}} X_{\mathbf{j}}^{\mathbf{v}} \cdot \mathbf{v}_{\mathbf{i}}^{\mathbf{v}} \cdot \mathbf{j} + \mathbf{g}_{22} \ell_{\mathbf{i}\mathbf{j}\mathbf{k}}^{2} \sum_{\mathbf{v}_{\mathbf{i}} v_{\mathbf{j}} v_{\mathbf{k}}^{\mathbf{v}} + \mathbf{j}} \sum_{\mathbf{i}\mathbf{k}} v_{\mathbf{i}} \ell^{2} \mathbf{t} ...$ (4)

and then to incorporate the effects of resonance perturbation by combining all close-lying levels with common $\boldsymbol{\ell}$ and common symmetry in matrices whose diagonal elements are $\boldsymbol{G_{v}}^{unp}$, whose off-diagonal elements are functions of additional molecular constants and the four quantum numbers, and whose eigenvalues are the vibrational energy $\boldsymbol{G_{v}}$. For an excellent discussion and example, the reader is referred to the work on $\boldsymbol{N_{2}O}$ by Pliva (19681.

This perturbation calculation results in the "mixing" of states whose G_{v}^{unp} are particularly close, so that the final description of the level by the original four quantum numbers is a poor one. Accordingly, it is useful to add a fifth index, the rank **symbol** \mathbf{r} to label in order **of** decreasing energy all such mixed states. We have adopted this procedure for $\mathbf{CO_2}$, where the mixed states are $(\mathbf{v_1} \mathbf{v_2} \mathbf{l_2} \mathbf{v_3})$, $(\mathbf{v_1} + \mathbf{1}, \mathbf{v_2} - \mathbf{2}, \mathbf{l_2}, \mathbf{v_3})$, . . . etc. The highest value of $\mathbf{v_1}$ and the lowest value of $\mathbf{v_2}$ in each set are retained in the vibrational **indentification** for all levels of the set.

In the present compilation, the above method was used to generate those energy levels which have not been observed; for all observed states the experimental value (averaged from various sources) was used.

The rotational energy of each vibrational state is given by:

$$E_{\mathbf{V},\mathbf{i}} = G_{\mathbf{V}} + B_{\mathbf{V}} \left[J(J+1) - \boldsymbol{\ell}^2 \right] - D_{\mathbf{V}} \left[J(J+1) - \boldsymbol{\ell}^2 \right]^2 + H_{\mathbf{V}} \left[J(J+1) - \boldsymbol{\ell}^2 \right]^3 + \dots, \quad (5)$$

where the constants $\mathbf{B_v}$, $\mathbf{D_v}$, $\mathbf{H_v}$ for each vibrational state are either determined by observation or calculated from **a. smaller** number of rotational molecular constants. Whenever **accerate** constants have been observed, these are used; calculated values are reserved for the less important states. The equations for calculations of $\mathbf{B_v}$ and $\mathbf{D_v}$ are similar to those for $\mathbf{G_v}$, and likewise require modification through the resonance perturbation. Evaluation from data of the small $\mathbf{H_v}$ constants requires highly accurate measurements extending to high J, so that in most cases these are fixed at zero; the non-zero values arise from resonances.

It will be noted in Eq. (4) that the vibrational energy depends on ℓ^2 . When $\ell \neq 0$ there are two levels for each $J \geq \ell$, and this degeneracy is removed by rotation. The splitting (" ℓ -type doubling") results in two sets of levels, designated $\underline{\mathbf{c}}$ and $\underline{\mathbf{d}}$, with different effective rotational constants. When $\ell = 1$ the splitting is most important, and $\mathbf{B_c} \neq \mathbf{B_d}$, $\mathbf{D_c} \neq \mathbf{D_d}$, etc.; when $\ell = 2$, $\mathbf{B_c} = \mathbf{B_d}$ but $\mathbf{D_c} \neq \mathbf{D_d}$, etc.; when $\ell = 3$, the constants other than H are the same. Resonances occasionally cause larger deviations.

When the linear molecule has a center of symmetry, as in CO_2 with ^{16}O at both ends (but not when one oxygen is **isotopically** different), the paired atoms with zero nuclear spin cause zero statistical weight for rotational **levels** of a **given** parity. Thus, only even-J levels exist for the ground vibrational level and for all other levels with $\boldsymbol{\ell} = 0$ and $\boldsymbol{v_3}$ even (" $\boldsymbol{z_g}$ symmetry"); for levels with $\boldsymbol{\ell} = 0$ and $\boldsymbol{v_3}$ odd ($\boldsymbol{z_u}$), only J odd exists; when $\boldsymbol{\ell} > 0$, the c - and d- sublevels have different symmetry, so that for $\boldsymbol{\ell} = \mathbf{1}(\boldsymbol{\pi_g})$ the J = odd levels are c and the J = even levels are d. etc. In the compilation symbols c or d are appended to the rotational quantum number of the lower state only when required, that is for $\boldsymbol{\ell} \geq 1$ in the molecules without the center of symmetry. For example, R27C means 28c - 27c; Q27C means 27d - 27c.

The line frequencies are determined from the energy states by taking the differences corresponding to all allowed transitions. These depend on the familiar selection rules for the linear molecule:

When
$$\Delta l = 0$$
, $\Delta J = \pm 1$, $c \rightarrow c$, $d \rightarrow d$.
When $\Delta l = 1$, $\Delta J = \pm 1$, $c \rightarrow c$, $d \rightarrow d$, and $\Delta J = 0$ $c \rightarrow d$.

The line positions may thus be conveniently represented for computational purposes as given series in \underline{m} , where m = J'' t 1 for the R-branch ($J'' \to J'' + 1$), m = -J'' for the P-branch ($J'' \to J'' - 1$), and m = J'' for the Q-branch ($J'' \to J'' - 1$). A different equation is needed for Q-branch of a given transition than for the P and R branches, because of the differences in the \underline{c} and \underline{d} constants. The general equation is

$$v(m) = G_{v} t \text{ am } t \text{ bm}^{2} t \text{ cm}^{3} t \text{ dm}^{4} t \text{ em}^{5} t \text{ fm}^{6}, \text{ with a } = (B'_{v} t B''_{v});$$

$$b = (B'_{v} - B''_{v} - D' t D''); c = -2 (D'_{v} t D''_{v}); d = -(D'_{v} - D''_{v});$$

$$e = 3(H'_{v} + \tilde{f}H''_{v}); f = (H'_{v} - H''_{v}).$$
(6)

3. 1. 2 NONLINEAR MOLECULES

The nonlinear triatomic molecules $\mathbf{H_2O}$ and $\mathbf{O_3}$ have similar basic structures. The formula for the vibrational energy is identical with Eq. (4), except that the quantum number $\boldsymbol{\ell}$ and its associated constants do not exist. Vibrational resonances exist; in both $\mathbf{H_2O}$ and $\mathbf{O_3}$, $\boldsymbol{\omega_1} \sim \boldsymbol{\omega_3}$, but these are of different symmetry, so that interaction between the band origins and identical rotational states occurs only in (200,002), etc. In addition for $\mathbf{H_2O}$, and much more closely for the 162 isotope, $2\boldsymbol{\omega_2} \approx \boldsymbol{\omega_1}$, so that the properties of the higher vibrational levels must be computed by taking their resonances into account.

The rotational levels of these three-dimensional rotators, with three different reciprocal moments of inertia $A_v > B_v > C_v$ are labelled by three quantum numbers, J, K_a, K_c , with K_a and K_c assuming all values $0, 1, \ldots, J$, subject to K_a t $K_c = J$ or J t 1. There are thus 2J t 1 levels of a given J (each again- with a rotational statistical weight of 2J t 1); in addition there is a nuclear-spin statistical weight which gives alternate levels, depending on the odd or even parity of $\mathbf{J} + \mathbf{K_a} + \mathbf{K_c} + \mathbf{v_3}$, weights of 3 or 1 for $\mathbf{H_2O}$, 0 or 1 for isotopically symmetrical $\mathbf{O_3}$. The normal progressions, of energy within each J is increasing with increasing, $\mathbf{K_a}$ - $\mathbf{K_c}$; occasionally inversions of a few paired levels may occur in excited vibrational states as a result of rotation-vibration interactions between close-lying states of like over-all symmetry in different vibrational levels. As J increases, there is a tendency for the odd and even levels with $\boldsymbol{K_a}$ or $\boldsymbol{K_c}$ close in \boldsymbol{value} to J to approach very closely in energy, so that many apparently single lines are in reality degenerate pairs with unresolvable spacings. The range of $\mathbf{K_a}$, $\mathbf{K_c}$ in which these pairings occur, and the general spacing of the rotational levels is governed by the asymmetry parameter, κ = (2B-A-C)/(A-C), which. for the ground vibrational states of H_2O , HDO, O_2 is respectively -9.437, -0.689, and -0.984. As the parameter approaches -1, the energy level formula approaches that of the symmetric top with A > B = C namely,

$$E_{r} = \frac{B+C}{2}J(J+1) + (A-\frac{B+C}{2})K_{a}^{2} - D_{J}J^{2}(J+1)^{2} - D_{JK}J(J+1)K^{2} - D_{K}K^{4}$$
(7)

where the D's are centrifugal stretching constants, and where additional terms of powers higher $\operatorname{in} J^2$, K^2 are often required. For the asymmetric top molecules with $K \neq -1$, the, rotational energy cannot be given by a closed formula, but requires the construction and diagonalization of matrices whose diagonal elements are given by Eq. (7) whose off-diagonal elements involve B-C and two additional centrifugal stretching constants of power 4, etc., and whose eigenvalues are the rotational energy. From the eigenvectors of the diagonalization, one obtains effective angular moments about each axis, $\langle P_a^2 \rangle$, $\langle P_b^2 \rangle$, $\langle P_c^2 \rangle$, whose sum, $\langle P_a^2 \rangle$ and one slso obtains other coefficients necessary for the calculation of transition probabilities and other properties of each eigenstate.

The excited vibrational levels of water vapor may differ considerably from the ground state in their values of A, B, and C, and with a relatively high ratio of $\mathbf{A}/\boldsymbol{\omega_2}$ ($\simeq 0.018$, as contrasted to 0.00059 for $\mathbf{B}/\boldsymbol{\omega_2}$ in $\mathbf{CO_2}$), extensive overlapping occurs between rotational levels in nearby vibrational states, making the computation of the higher levels highly uncertain much beyond the limits of observation. Accordingly, for all except the lowest energy levels of the ground state it is preferable to use experimental rather than calculated values when available.

3.2 Line Intensities

The intensity of any line at frequency ${m v}$ may be expressed in a purely formal way as:

$$\mathbf{S_{m}} = \frac{\nu}{\nu} \cdot \mathbf{S_{v}^{o}} \cdot \mathbf{S_{Rot}} \cdot \mathbf{F}$$
 (8)

where $S_{\mathbf{v}}^{\mathbf{o}}$ is the vibrational intensity of a nonrotating molecule at the vibrational **origin**, $\mathbf{v}_{\mathbf{o}}$; $\mathbf{S}_{\mathbf{Rot}}$ is the rotational intensity **for** a rigid nonvibrating molecule and F is a factor that takes into account the fact that both forms of motion are occurring simultaneously. In the rigid case, $\mathbf{F} = \mathbf{1}$, and if $\mathbf{S}_{\mathbf{Rot}}$ is normalized so that $\mathbf{\Sigma}_{\mathbf{Rot}} \mathbf{S}_{\mathbf{Rot}} = \mathbf{1}$ and if the band extends over a limited frequency range so that $\mathbf{v}/\mathbf{v}_{\mathbf{o}} \sim \mathbf{1}$, then $\mathbf{S}_{\mathbf{v}}^{\mathbf{o}}$ as defined by Eq. (8) is identical with the quantity usually denoted by $\mathbf{S}_{\mathbf{v}}$, the total band intensity, $\mathbf{\Sigma}_{\mathbf{m}} \mathbf{S}_{\mathbf{m}}$.

 S_{Rot} consists of a temperature-independent factor, the rotational line strength, L_R , common to all linear molecules, and a temperature-dependent **Boltzmann** factor [Eq. (13)]. If the sum of all transitions from J'' is normalized to the statistical weight g = 2J'' + 1, and if one recalls the definition of the rotational partition function $Q_r(T) = Eg \exp_r(\tau^1 - 4393 - \frac{1}{R}T)$ (the summation is over all rotational levels of a given v), the normalization condition for all transitions ($ES_{Rot} = 1$) is fulfilled.

The equations for $\mathbf{L}_{\mathbf{R}}$ are as follows:

$$\Delta l$$
 AJ L_{R}

0 0 $l^{2}(2m + 1)/m(m + 1)$ (9)

0 +1 $(|m| - l^{2})/|m|$ (10)

+1 0
$$(|m|+1+l)(m+l)(2m+1)/m(m+1)$$
 (11)

+1 =+1
$$(|m| + 1 + \ell) (|m| + \ell)/|m|$$
 (12)

Equation (8) is exact with F = 1 only for a rigid molecule. In the actual molecule, a number of factors may cause deviations, which however will vary regularly along the band. (A very few exceptional situations, "crossing **perturbations**", may also be recognized.) Depending on the precision of the measurements, the non-rigidity corrections ("F-factors") for the linear molecule, may be expressed as regular functions of the running index, \mathbf{m} , as indicated in Eq. (131.

$$F = S_{nonrigid} / S_{rigid} = (1 + am + bm^2 ...).$$
 (13)

The first order theoretical correction is $F = (1 + \zeta m)^2$ or $a = 2 \zeta$, $b = \zeta$. For nearly all the intensities in the present compilation, a single ζ was used **for** each vibrational band; this is included in the tabulations of band parameters. More

refined measurements and theoretical calculations should, in future **revisions** of this **compilation**, permit the use of additional terms in Eq. (13).

For asymmetric top molecules, many more transitions are possible from each rotational level J $\mathbf{K_aK_c}$, but the same general definitions hold. The values of $\mathbf{L_{Rot}}$ depend on the degree of asymmetry. Tabulations exist (Wacker, 1964) which are useful for orientation purposes. In the present work we either derive $\mathbf{L_R}$ from the rotational constants, for pure-rotation bands and some fundamental bands, or make use of the tables.

The F-factor corrections to the intensities become of considerable significance for most of the vibration-rotation transitions in $\mathbf{H_2O}$. Various methods are used, based in part on theoretical considerations described later on, and in part on an arbitrary empirical adjustment of calculated values to the best observations.

A few general remarks should be made regarding the temperature dependence of $\mathbf{S_v}^{0}$. $\mathbf{S_v}^{0}$ is proportional to the product of the relative population of the lower state, given by the vibrational Boltzmann terms exp (-1.439 $\mathbf{G_v}$)/ $\mathbf{Q_v}$, (with $\mathbf{Q_v}$ $\mathbf{z}_{\mathbf{y}} \mathbf{g}_{\mathbf{y}} \exp \left(-1.439 \mathbf{G}_{\mathbf{y}}\right)$ where $\mathbf{g}_{\mathbf{y}}$ is the degeneracy of the level, 1 when $\mathbf{l} = 0$, 2 otherwise), and a temperature independent transition probability, $\mathbf{u_{vv}} = |\int \widetilde{\psi_{\mathbf{v}}} \mathbf{u} \psi_{\mathbf{v}}' \, \mathrm{d} \tau|^2$, $\psi_{\mathbf{v}}$ being the dipole moment function, usually expressed as a Taylor's series expansion in the dimensionless normal coordinates. We rely on measurement to give the total absorption strength in a given spectral region. When the spectral resolution is sufficiently high to distinguish lines of the strongest band in the region, usually the one with the lower level v = 0, from lines of all of the weaker "hot" or isotopic bands which accompany it, no problems arise: The ${f S}_{f r}^{f o}$ of each band, and accordingly the relative μ_{wv} is empirically established (along with favorable cases a determination of coefficients of the F-factor, leading to 25. for the region). However, most of the studies of quantitative band intensities have been made under conditions where only the total intensity is observed and the strengths of the weaker lines, which contribute only a few percent of the total, estimated from theoretical relations.

When all the transitions in the region are of the same type (that is, have identical $\Delta v_1, \Delta v_2, \Delta v_3, \Delta \ell$), a good approximation to the relative transition probability is to use harmonic oscillator wave functions and to assume that the leading term in the expansion of μ is formed by the $\Delta v's$: for example if A $v_1 = 2$, $\Delta v_3 = 1$, we require that this term be $\mu_{113} q^2 l q_3 with \mu_{113} = \partial^3 \mu / \partial q_1^2 \partial q_3$. Evaluation of the integral for arbitrary values of $v_1, v_2, v_3 \rightarrow vl$ t 2. v_2, v_3 t 1 then gives the ratio $\mu^2_{vv'} / \mu^2_{0201} = (v_1 t 2)! (v_3 t 1)! / v_1! v_3!$. The general formula (for A $\ell = 0$) is $(v_1 t A v)! (v_2 + \Delta v)! (v_3 t A v)! / v_1! v_2! v_3!$. When A $\ell = + 1$ similar relations involving, integers hold. Use of more realistic wave functions corrected for an

harmonicity with lower terms in the dipole expansion lead to very nearly the same ratios. Accordingly, for many transition regions this type of calculation is simple and acceptable.

When, however, as in the case of both CO2 and N_2O , the resonance perturbations mix the vibrational wavefunctions, a region includes several bands with different basic transitions. For example, the 1.6μ region of CO2 contains four strong A $\boldsymbol{l}=0$ bands, composing the resonance quartet 3001r-0, with r=1, 2, 3, 4. If we assume that only the A $\mathbf{v_1}$ = 3, $\mathbf{\Delta v_3}$ = 1 transition is involved, the relative transition probability of the four transitions should be given by the squared eigenvectors of the (301, 221, 141, 061) matrix, and the relative transition probability of the four hot transitions from 010 would be the same value (since $\Delta v_2 = 0$) multiplied by the squared eigenvectors of the $\{311, 231, 151, 071\}$ matrix. These are not identical with the other eigenvectors, and all four hot bands have different transition probabilities. Moreover, the observed ground-state intensities are not proportional to the first set of eigenvectors. Inclusion of a second basic transition integral for Avl = 2, Δv_2 = 2, Δv_3 = 1, together with the appropriate eigenvectors can, however, bring the observations in accord with calculation, if the ratio $\mu_{221}/$ μ_{301} is of the order of 0.1. The ratio 231 -O/221-010 is 3, and accordingly its inclusion increases the over-all -010/0 strength ratio and further shifts the relative probabilities. As one extends the calculations to lower states involving resonating groups with $\mathbf{v_2}$ = 2, 3, and higher, required in the stronger bands of $\mathbf{CO_2}$ and $\mathbf{N_2O_4}$ the situation cannot be predicted in advance. However, calculations similar to those sketched above have been performed; then reliability depends on the accuracy of the input constants, but it is believed that such a computation is useful.

One must also note that in the isotopically modified molecules, the **eigenvec**-tors of resonating groups vary widely. Thus, the simple assumption of a constant isotopic abundance ratio for the intensities is very far from correct. It should be adequate however to assume that the relative intensities of the underlying transitions (301-O and 221-O, in the example cited above) remain isotopically invarient.

It should also be remarked that the eigenvectors are rotationally dependent; the result would be a contribution to the \mathbf{m}^2 term in Eq. (9).

4. MOLECULARSPECIES

4.1 water Vapor

4.1.1 LINE POSITIONS

The frequencies of the lines of the principal isotope $(^{1}H^{16}O^{1}H = \text{Code 161})$ are calculated from a set of energy levels. These were obtained from the best available

data in all spectral regions by a smoothing process which is partly theoretical, partly empirical. The principal sources of data are identified and summarized in Table 7. The energy levels of the ground state, $v_1v_2v_3 = 000$, are by far the most extensive and accurate. They are based on a relatively small number (15, at the present writing) of microwave lines whose frequencies are precise to C 0.00001 cm⁻¹ (0.3 MHz), and several much larger groups of pure rotational lines, whose frequency accuracy may range from 0.001 to 0.002 cm⁻¹ for isolated lines measured with Michelson-type interferometers to 0.02 to 0.03 cm⁻¹ for weaker or partially blended lines measured with conventional spectrometers. With the long absorption paths available through the atmosphere, the observed lines extend to quite high energy levels. and by somewhat less accurate measurements with flame sources, to still higher levels, so that pure rotation transitions connect all levels from 0 to more than 4000 am -1. The 000 level is the lower state of the more than 50 vibration-rotation bands observed between 900 and 20,000 cm⁻¹, so that these measurements provide combination differences (common upper level in two or more transitions) for the 000 state that confirm, and for some states greatly improve those of the pure-rotation lines. In particular; the recent laboratory measurements of the 1.9 µm region give low-J energy differences that are selfconsistent to better than 0.001 cm⁻¹. A theoretical smoothing of the totality of the observed microwave, pure-rotation, and combination-difference data, by leastsquares fitting to a 29-constant Hamiltonian of the type described for D₂O (Benedict et al, 1970) then yields the ground state energy levels used in the compilation. Inasmuch as none of the theoretical calculations have been successful in reproducing all of the available data to their apparent accuracy, the levels adopted for the current compilation are a calculated set for E < 2500 cm⁻¹, and for higher energies are determined from observations. It is believed that the accuracy of lines involving these levels is ± 0.005 cm⁻¹ for E" < 1500 cm⁻¹; t 0.02 cm⁻¹ for 1500 < E'' < 3000 cm⁻¹, and + 0.05 cm⁻¹ up to the tabulated limit. The levels of the other vibration-rotation states are then obtained by averaging the sums of the observed lines and the lower-state levels. When upper-state levels have not been observed, although transitions to them have expected intensities above the lower limit, estimated values are chosen, either by direct calculations using an appropriate approximate Hamiltonian. or by extrapolation of the observed series of upper-lower rotational energy differences.

For the isotopic forms 181 and 17 1, the ground-state energies were obtained in the same way, except with much less extensive data (respectively 12 and 9 microwave lines). The dependence on theoretical calculations for the smoothing is more extreme, and the data for levels higher than 1500 cm⁻¹, the limit of observation, is quite uncertain. However, since the higher-order constants in the

Table 7. Summary of Principal Data Sources for Water-Vapor Energy Levels

| | | Range o f | eve | ls | ntensity | Precision | | |
|------------|-------------|----------------|-----|--------|----------|------------------|-------|--|
| Region | Type of | Rotat | | cional | Limit | of v | | |
| a m - ′ | Measurement | Vibrational | J | Ka | (2% K) | cm ⁻¹ | Ref. | |
| 0-25 | L,181,171 | 0,010 | 10 | 6 | C-27 | .00001 | a,b | |
| 0-25 | L,162,182 | 0,010 | 13 | 7 | <-27 | .00001 | c,đ | |
| 30-250 | L | 0 | 13 | 7 | -23 | .005 | е | |
| 256550 | L | 0 | 15 | 11 | -24 | .03 | f | |
| 480-690 | LH | 0 | 15 | 12 | -25 | | g | |
| 430-650 | r | 0,010 etc. | 30 | 15 | C-27 | .05 | h | |
| 700-1100 | LH | 0,010 | 19 | 12 | -26 | .1 | i | |
| 750-1400 | λ | 0,010 | 18 | 12 | -25 | .05 | į | |
| 860-1100 | A | 0,010 | 18 | 12 | -25 | -02 | k | |
| 1270-1450 | LH | 010,020 | 16 | 9 | -27 | .05 | 1 | |
| 1200-1700 | L,162 | 010 | 14 | 7 | -27 | .02 | 110 | |
| 1330-1970 | L, 181, 171 | 010 | 13 | 6 | -26 | .01 | n | |
| 1840-2500 | LH | 010,020,001+ | 18 | 10 | -26 | .03 | 0,2 | |
| 1925-2182 | A,U | 010,020,001+ | 28 | 10 | <-27 | .01 | P | |
| 2390-2970 | A,U | 100,001, etc. | 32 | 19 | <-27 | .01 | P | |
| 2480-3030 | L,162 | 100,020 | 18 | 10 | e-27 | .005 | q | |
| 2900-3500 | λ'— | 020,100,001 | 16 | 11 | -26 | :02 | r | |
| 2800-3500 | F | 001,011, etc. | 33 | 13 | e-27 | .02 | a | |
| 2900-4330 | L,162 | 001,100, etc. | 14 | 9 | -25 | .005 | t * | |
| 3340-4030 | L,181,171 | 001,100, etc. | 13 | 7 | -26 | .01 | u | |
| 3940-4300 | F | 001,011, etc. | 33 | 19 | <-27 | .02 | s | |
| 4032-5090 | A,U | 001,011,020 + | 33 | 17 | C-27 | .01 | V | |
| 3950-5200 | A | 001,030,011,et | 18 | 13 | -26 | .01 | W | |
| 4500- 5915 | L,162 | 011,030,110,et | 14 | 8 | -25 | .005 | t * | |
| 5090-5575 | L | 011,110 | 12 | 7 | -24 | .005 | X | |
| 5540-7000 | A | 011,021,120 + | 16 | 9 | -26 | .01 | W | |
| 5550-6720 | A,U | 011,021,120 + | 24 | 11 | <-27 | .01 | V | |
| 7000-7500 | L | 101,200 | 13 | | -24 | .05 | Y | |
| 7400-9000 | Ā | 101,002,111 + | 16 | 9 | -26 | .01 | W | |
| 7390-8800 | A.U | 101,001,111 + | 16 | 9 | -25 | .01 | V | |
| 8300-10000 | Α | 111,012,041 | 16 | 8 | -25 | .03 | x | |
| 9150-9350 | A | 012,111 | 10 | 7 | -27 | .005 | 88 | |

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The data wurces are of five types: <u>L</u>, laboratory absorption measurements on water vapor or moist air at room temperature; <u>LH</u>, similar measurements in cells heated to 75-540°C; <u>F</u>, laboratory measurements of emission from oxy-hydrogen or oxy-acetylene flames, yielding -10" molecules/cm² H₂0 at +2500-3500K; <u>A</u>, measurements of solar radiation through the atmosphere, containing 10²²-10²⁵ molecules/cm²; <u>U</u>, observations of the raticed spectrum of sunspot/photosphere, alw containing about 10¹⁹ mol/cm² at ~3600K. Iwtopic symbols are appended when enriched samples were studied, underlined when a major component, dashed when moderately increased above natural abundance. The range of vibrational and rotational levels is a rough indication of the extent of levels observable down to the intensity limit of S° (cm²/mol cm²), corrected to 296K, with the rewlving power used. The ground state, (v=0) is implied in all regions.

• In reference t, the observed contamination of the sample by deuterium to give the HDO abundances varying from 10-200 times normal was not reported.

theoretical fit were constrained near their values in ${\rm H_2O\text{-}161}$, the tabulated line positions for all pure-rotation lines should be accurate to t 0.5 cm $^{-1}$. Upperstate levels for these molecules are likewise available only for the strongest lines, so that the uncertainties of weak lines here might approach t 1 cm $^{-1}$.

The asymmetrically substituted HOD (162) molecule has been studied, both in the microwave and infrared regions with thoroughness comparable to 161, so that the frequency data, for the 000,010, 100, 020, 110, and 030 bands should be of the same accuracy as for 161. The 001 and 011 levels may have errors larger by a factor of five.

Quite reliable data can be calculated for the pure-rotation spectra of isotopic forms 182, 172, and 282, which are only of very minimal importance in the atmosphere. Weak lines in vibration-rotation bands of 182 (as yet unobserved, except for a few lines in 100-000) also have been included by estimating constant vibrational shifts from 162.

4.1.2 LINE INTENSITIES

The intensities of pure rotation lines were calculated by a program in which the effects of vibration-rotation interaction on both the rotational eigenfunctions and on the dipole moment were included. The eigenfunctions were obtained from a Hamiltonian with 25 independent constants -which gave an excellent fit to the energy levels, and the dipole moment was expressed as a linear expansion in the dimensionless normal coordinates:

$$\mu = \mu_{e} + (\partial \mu / \partial q_{1})q_{1} + (\partial u / \partial q_{2})q_{2} + (\partial \mu / \partial q_{3})q_{3} + \dots$$
 (14)

The $\partial \mu/\partial \mathbf{q_i}$ coefficients in this expression were obtained from the $\mathbf{S_v^o}$ values of the three fundamental bands by the equation $\mathbf{S_{v_i}^o} = 4.16 \times 10^{-19} \nu (\partial \mu/\partial \mathbf{q_i})^2$. The algebraic signs of $\partial \mu/\partial \mathbf{q_i}$ were chosen so that the observed vibration-rotation effects on intensities were reproduced in the fundamental bands of $\mathbf{H_2O}$ and verified by noting that these and only these choices also gave a reasonable fit to the band intensities and interaction effects in the isotopic molecules. The value of the permanent moment in the equilibrium configuration, $\mu_e = 1.847D$ (Clough and Beers, 19731, was derived from Stark Effect measurements on 8 microwave lines in three isotopic water molecules (161, 162, 262), and is in excellent agreement with recent molecular-beam measurements (Dyke and Muenter, 1972). The uncertainty in the calculated intensities should result from inaccuracy of the $\partial \mu/\partial \mathbf{q_i}$ coefficients and neglect of higher terms in the expansion; accordingly, it should be of minor importance for low J lines, and is estimated to be less than 1 percent for $\mathbf{E}'' \leq 1000$ cm⁻¹ and less than 10 percent for all lines in the tabulation, with the possible exception of the very low probability lines in such branches as $\mathbf{R_{53}}$, $\mathbf{Q_{55}}$, etc. (Benedict, Classen and Shaw, 1952).

The intensities of vibration-rotation lines are more difficult to calculate, because they differ from those of the rigid asymmetric rotor by three interrelated effects: (1) the centrifugal effects, as used above for pure rotation; (2) the fact that the asymmetry, and hence the rotational eigenfunctions, are vibrationally dependent; and (3) the fact that for all vibrations above 010, the rotational levels of like symmetry and equal J in different vibrational levels are at energies sufficiently close that the vibrational eigenfunctions are rotationally dependent, and in special cases "perturbations" lead to abnormal mixing and intensities. Only the first-named effect has been incorporated in the computations, through the method described by Benedict and Calfee (1967). Table 8 lists the constants used for each band. The footnotes to Table 8 list the sub-branches which are observed to disagree in a regular way from the results of the calculation, and which were adjusted accordingly. The lines that are exceptionally perturbed (effect 3) are identified by the symbol P following K'; for these the total intensity of the two "interacting" lines was divided as required by the calculated vibrational mixing ratios or further adjusted to agree with measurements. No general statement can be made concerning the accuracy of the intensities of individual lines; for the low-J lines of the strongest bands it should be within \pm 10 percent, within a factor of two for other lines of sufficient intensity (>10⁻²⁵ cm⁻¹/mol-cm⁻²) to appear in laboratory and/ or solar spectra, and within an order of magnitude for the weakest lines.

The intensities of the isotopic lines of species 181 and 171 were taken equal to those of 161 multiplied by the abundance factor (except for the cases of strong perturbation where the vibrational mixing ratios are different). The asymmetric isotopic species 162 is widely different, so that a completely independent calculation of its intensities, in both pure rotation and vibration-rotation has been made. The band parameters are included in Table 8.

4.1.3 LINE WIDTHS

Recent high-resolution spectra of air -broadened or N_2 -broadened water vapor lines (**Brault**, 1972, private communication) have in general confirmed the calculations of Benedict and Kaplan (1959) to \pm 10 percent. A striking discrepancy is, however, observed (**Blum** et al, 1972) for the lines of highest J which are much narrower than the lower limit of 0.032 cm $^{-1}$ atm $^{-1}$ which was imposed on the calculated value by choosing a minimum collision diameter equal to the **kinetic**-theory diameter. If the Anderson Theory (Anderson, 19491 is modified by eliminating a distance of closest approach (that is, setting the kinetic theory collision diameter equal to **zero**) the calculated half-width at half-height of 161, 16 $^{-15}$ $^{-15}$ is lowered from 0.032 to 0.0098 cm $^{-1}$, still slightly above the observed **value** (0.0086). The validity of the theory is thus in question for high-J transitions but a revised

Table 8. Water Vapor **Band** Intensity Data and Interaction Coefficients

| vo | | | 5 ⁰ (296K) R | | R | Interaction Coefficients | | | |
|------------------|------|-----------------|-------------------------|---------------------------------------|----------------|--------------------------|----------------|----------------|-------------|
| cm ⁻¹ | iso | A, A. | Rot Type | cm ⁻¹ /molcm ⁻² | Debyes | α | В | Υ | Notes |
| 1403.489 | 162 | 010 000 | А | 8.0 -022 | .066 | | | | |
| | | | B | 1.92 -021 | . 105 | | | | <i>(</i> 1) |
| 1556.695 | 161 | 020 010 | B | 8.61 -021 | .171 | | | | (1) |
| 1568.279 | 181 | 010 000 | B | 2.12 -020 | .121 | | | | (1) (1) |
| 1591.32 | 171 | 010 000 | 8 | 3.93 -021 | .121 | 25 | .0065 | 004 | (=) |
| 1594.736 | 161 | 010 000 | В | 1.061-017 | .121 | 5 | .013 | 005 | (2) |
| 2062.318 | 161 | 100 010 | В | 8.9 -023 | .0167 | | | | |
| 2161.188 | 161 | 001 010 | A | 4.9 -022 | .0394 | | 0108 | 015 | |
| 2709.35 | 182 | 100 000 | A | 1.31 -024 | .0437 | | | | |
| 2723.667 | 162 | 100 000 | A | 6.53 -022 | .0437 | 322 | .0130 | .077 | |
| | | | a A | 2.0 -023 | .0076 .0153 | | | | |
| 2782.014 | 162 | 020 000 | B | a.1 -023 9.0 -024 | .0051 | | | | |
| 3072.058 | 161 | 030 010 | 8 | 7.99 -023 | .0121 | | | | (1) |
| 3139.02 | 161 | 020 000 | В | 1.32 -022 | .0070 | | | | (1) |
| 3144.96 | 171 | 020 000 | В | 4.92 -023 | .0070 | | | | (1) |
| 3151.631 | 161 | 020 000 | В | b.58 - 020 | .0070 | | .005 | .003 | (3) |
| 3640.245 | 161 | 110 010 | 3 | 1.50 -022 | .0149 | | | | (1) |
| 3649.690 | 181 | 100 000 | В | 7.24 -022 | .0149 | | | | (1) |
| 3653.14 | 171 | 100 000 | В | 1.33 -022 | .0149 | | | | (1) |
| 3657.054 | 161 | 100 00 | 8 | 3.62 -019 | .0149 |)75 | .035 | .028 | (3) |
| 3707.459 | 162 | 001 000 | A B | 1.2 -021 3.0 -022 | .0509 .0255 | | | | |
| 3736.509 | 161 | 011 010 | Α | 3.30 -021 | .0708 | | | | (1) |
| 3741.571 | 16.1 | 001 000 | Α | 1.60 -020 | .0708 | | | | (1) |
| 3748.36 | 171 | 001 000 | Α | 2.96 -021 | .0708 | | | | (1) |
| 3755.924 | 161 | 001 000 | А | 7.994-018 | .0708 |)695)278 | .0310 .0124 | .0160 .0064 | (4) |
| 4099.954 | 1b2 | 110 000 | A B | 2.0 -023 1.5 -024 | .0088 | (F : | =1+0.15 | (a) | (5) |
| 4145.483 | 162 | 030 000 | A | 2.0 -023 1.5 -024 | 0 | (P 1 | =1-0.15 | Ka05m) | (5) |
| 4666.720 | 161 | 030 00 0 | В | 2.0 -022 | .000: | .01 | .10 | .12 | |
| F0 F20 | 160 | 011 00 | A | 3.0 -023 | .0069 | .02 | | | |
| 5oa9.539 | 162 | 011 000 | В | 6.0 -024 | .003 | .02 | | | |
| 5180.36 | 161 | 120 010 | B | | .004 | | | | (1) |
| 5221.28 | 181 | 110 000 | В | | .002 | | | | (1) |
| 5227.75 | 171 | 110 00 1 | В | | .002 | | | | (1) |
| 5234.981 | 161 | 110 00 | В | | .002 | .05 | 015 | 02 | |
| 5276.776 | 161 | 021 01 | Α | | .028 | | | | (1) |
| 5310.43 | 181 | 011 00 | Α | | .020 | | | | (1) |
| 5320.25 | 171 | 011 00 | Α | 3.36 -022 | .020 | 1 | | | (1) |

Table 8. Water Vapor Band Intensity Data and Interaction Coefficients (Contd)

| ٧o | | s _g (296K) | | _ [| Interaction Coefficient | | | icients | |
|------------------|-----|-----------------------|--------------------|----------------------------------------|-------------------------|---|---|---------|-------|
| cm ⁻¹ | iso | A, A. | Not Type | cm ⁻¹ /mol cm ⁻² | R Debyes | а | В | Υ | Notes |
| 5372.114 | 162 | 200 000 | А | 1.2 -023 | .0042 | | | | |
| 6679.21 | 161 | 130 010 | В | 4.32 -024 | .00194 | | | | |
| 6755.40 | 181 | 120 000 | В | 7.05 -024 | .00112 | | | | |
| 6775.10 | 161 | 120 000 | В | 3.53 -021 | .00112 | | | | |
| 6779.08 | 161 | 031 010 | Α | 6.94 -023 | .0076 | | | | |
| 6844.59 | 181 | 021 000 | Α | 1.13 -022 | .0044 | | | | |
| 6657.32 | 171 | 021 000 | Α | 2.09 -023 | .0044 | | | | |
| 6671.512 | 161 | 021 000 | Α | 5.64 -020 | .0044 | | | | |
| 7186.68 | 181 | 200 000 | В | 1.06 -022 | .0042 | | | | |
| 7201.48 | 161 | 200 000 | В | 5.29 -020 | .0042 | | | | |
| 7213.26 | 161 | 111 010 | Α | 3.98 -022 | .0157 | | | | |
| 7222.68 | 181 | 101 000 | Α | 1.49 -021 | .0157 | | | | |
| 7235.57 | 171 | 101 000 | Α | 2.76 -022 | .0157 | | | | |
| 7249.93 | 161 | 101 000 | A | 7.47 -019 | .0157 | | | | |
| 7371.79 | 161 | 012 010 | В | 2.17 -024 | .00131 | | | | |
| 7417.54 | 181 | 002 000 | В | 1.06 -023 | .00131 | | | | |
| 7430.54 | 171 | 002 000 | В | 1.96 -024 | .00131 | | | | |
| 7745.04 | lb1 | 002 000 | В | 5.29 -021 | .00131 | | | | |
| 8238.84 | 161 | 041 010 | А | 5.66 -024 | .00204 | | | | |
| 8273.95 | 161 | 130 000 | В | 2.4 -022 | .00027 | | | | |
| 6341.32 | 181 | 031 000 | Α | 7.2 -024 | .00102 | | | | |
| 8356.70 | 171 | 031 000 | Α | 1.33 -024 | .00102 | | | | |
| 8373.82 | 161 | 031 000 | Α | 3.6 -021 | .00102 | | | | |
| 8734.97 | 161 | 121 010 | Α | 4.10 -023 | .0037 | | | | |
| 6761.57 | 161 | 210 000 | В | 3.6 -022 | .00031 | | | | |
| 8779.75 | 181 | 111 000 | А | 9.96 -023 | .0037 | | | | |
| 8792.63 | 171 | 111 000 | Α | 1.85 -023 | .0037 | | | | |
| 8807.00 | 161 | 111 000 | A | 4.98 -020 | .0037 | | | | |
| 8966.53 | 181 | 012 000 | В | 2.4 -024 | .00057 | | | | |
| 9000.13 | 161 | 012 000 | В | 1.2 -021 | .00057 | | | | |
| | | | 1 | | Į. | | | | |

Notes to Table 8.

- (1) Insufficient data to establish interaction coefficients; these are assumed identical with corresponding band of 161.
- (2) Lower line for strong lines (L rigid>1); upper line for others.
- (3) Many lines, especially those with entranced resonance with 001, require special treatment.
- (4) Lower line for stronglines (Lrigid>0,5); upper line for others.
- (5)Very close resonance of these two states at K =0, all transition of tributed $\bullet 0$ from 0

calculation with b $_{\min}$ = 0 does reproduce the empirical results better than the original'calculation. Accordingly this has been incorporated in the current tabulation. As in previous computations, no vibrational dependence of the width has been included. The widths of the isotopic lines (181 and 171) have been set equal to those of 161; for 162 a new calculation, with μ_e = 1.847, q_{air} = 2.62 x 10 $^{-26}$ esu and p_{\min} 0 has been made, where μ_e is the dipole moment of water, q_{air} is the effective quadrupole moment of the colliding gas and p_{\min} is the collision diameter.

4.2 Grbon Dioxide

4.2.1 LINE POSITIONS

The line positions and lower-state energies of each of the significant isotopic modifications of CO_2 were calculated for each band by a rotational formula for the linear molecule including terms up to $D_vJ^2(Jt1)^2$. For some of the higher states involving Fermi resonances of high rank, an additional term $H_vJ^3(Jt1)^3$ was required. A very few of the vibrational levels are involved in a rotational perturbation, for which special calculations were needed as discussed below. The constants for each levelare summarized in Table 9. For each isotopic species the band constants form a self-consistent set; that is, if a vibrational state appears more than once, as either initial or final state, its value of G_v, B_v, D_v (and occasionally H_v) is the same. This requirement results in some deviations of the smoothed final line positions from their best observed values, but in general the positions of observed lines, up to J=40, will be within t 0.01 cm $^{-1}$ of the tabulation.

The constants were calculated for each isotopic species separately, using a set of constants similar to those of Chedin and Cihla (19721, for 626, 636, and 628, **but** the isotopic sets were not consistently readjusted to fit a potential function. However, for isotopic forms for which the data are less extensive, approximate isotopic relations were used.

The data **used** for the band constants are taken from various sources. The highest precision data are those for the laser transitions 00011-l 0001 and **00011**-10002 in the 626 isotope. The measurements of Gordon and **McCubbin** (1965, **1966**), Oberly et al, **(1968)**, and **Drayson(1967)** provide the data for interrelations among the lowest states. The most extensive data for the higher states are those from the planet Venus. as observed and summarized by Connes et al, (1969).

The vibrational notation may not be familiar to all users, and accordingly will be explained at this point. Five digits are used for each state, in order, $v_1v_2 l v_3 r$. The fifth digit, r, takes the possible values 1, 2, . . . $v_1 + 1$, and serves to locate the level in the Fermi resonating group of v t 1 levels; $v_1, v_2 l$, $v_3; v_1 - 1(v_2 t 2)^l$, $v_3; \ldots 0$, $(v_2 + 2v_1)^l$, v3. The value of r decreases with increasing energy. (In

Table 9. Vibrational Energy Levels and $\mathbf{Molecular}$ Constants $\mathbf{for}\,\mathbf{CO_2}$

| Energy Level | G | 3 | D Multiply | Energy Level | G | • | D Multiply | Energy Level | G | • | D |
|---------------------|------------------------------|----------------------|---------------------|----------------------------|-----------------------------|--------------------------|------------------------|---------------------|-------------------------------|----------------------|---------------------|
| | -1 | -1 | by 10 ⁻⁷ | | | _ | by 10 ⁻⁷ | | _ | | by 10 ⁻⁷ |
| | (cm ⁻¹) | (cm ⁻¹) | (cm ⁻¹) | | (cm ⁻¹) | (cm ⁻¹) | (cm ⁻¹) | | (cm ⁻¹) | (cm ⁻¹) | (cm ⁻¹) |
| | Isc | tope 626 | | 40004 | 5197.249 | 0.390092 | 1.89 | 41114 C | 8081.179 | 0.387643 | 1.56 |
| 00001 | 0.00 | 0.390218 | 1.331 | 32203 c | 5245.469 | .391490 | 1.335 | 41114 d | | ,389753 | 1.66 |
| 01101 c | 667.279 | . 390643 | 1.255 | 32203 d | 547E AT1 | 200100 | 1.535 | 41113 c | 8250.644 | .386233 | 1.355 |
| 01101 4 | 007.279 | .391253 | 1.355 | 21113 C 21113 d | 5475.071 | . 388153 . 389423 | 1. 61° 1.705 | 41113 d 41112 c | 8425,000 | ,387813 ,386817 | 1.355 0.935 |
| | | | | 40002 | 5475. 565 | . 390093 | 0.895* | 41112 d | 0423.000 | .306517 | 0.965 |
| 10002 | 1205.412 | .390481 | 1.563 | 13312 od | 5521.279 | . 389732 | 1.52 | 11132 c | 8803.265 | . 301850 | 1.49 |
| 02201 c 02201 d | 1225.129 | . 391682 | 1.249 1.279 | 05511 od 21112 c | 5627.254 5632.760 | .390913 .387018 | 1.44 1.265 | 11132 d 03331 cd | 8063,640 | .382744 | 1.56 1.40 |
| 10001 | 1388.187 | . 390188 | 1.142 | 21112 đ | | .388128 | 1.385 | 11131 c | 8944,146 | . 381264 | 1.22 |
| | 1022 430 | 300734 | | | 5730.618 | . 309269 | 1.51 | 11131 d | | ,381874 | 1.10 |
| 11102 c 11102 d | 1932.470 | . 390736 | 1.441 | 21111 c 21111 d | 57W.579 | .387413 | 1.125 1.025 | 20033 | 92Y.996 | . 38234 | 1.72 |
| 03301 cd | 2003.238 | . 392420 | 1.402 | 10022 | 5915.209 | . 304526 | 1.57 | 12232 c | 9419.169 | . 36307 | 1.27 |
| 11101 c | 2076.865 | . 390416 | | 02221 C | 5956.529 | . 385617 | 1.35 | 12232 d | | | 1.25 |
| 11101 d 00011 | 2249.146 | . 391 344 | 1.195 1.225 | 02221 d 10021 | 6016.690 | . 383917 | 1.31 1.17 | 20032 12231 c | 9516.970 9589 , 929 | . 38048 . 38247 | 1.29 1.43 |
| 00011 | 2247.140 | | 1.223 | 10021 | 0010.040 | . 303717 | 2.27 | 12231 4 | 3303, 929 | . 30447 | 1.53 |
| 20003 | 2548. 280 | .391183 | | 20014 | 6075.983 | | 2.052 | 20031 | 9631.350 | . 38125 | 1.04 |
| 12202 c 12202 d | 2585.006 | . 391843 | 1.45 1.25 | 22213 c 22213 d | 6102.670 | . 389428 | 1.29 1.67 | 21133 c | 9987.48 | . 30251 | 1.55 |
| 20002 | 2671.113 | . 389556 | | 14412 c | 6176.622 | . 390485 | | 21133 d | ,,,,,, | .30251 | 1.63 |
| 04401 cd | 2671.690 | . 393162 | | 41102 c | 6179.010 | . 389642 | 1.33 | 21132 c | 10145.43 | . 38096 | 1.25 |
| 12201 c 12201 d | 2760.725 | . 391535 | 1.44 1.25 | 30013 22212 c | 6227.924 6288.492 | . Y6697 | 1.643 1.38 | 21132 d 21131 c | 10007.05 | . 30258 | 1.25 |
| 20001 | 2797.154 | . 390563 | | 22212 @ | 0200.474 | . 3004 / 2 | 1.28 | 21131 d | 10297.05 | .38127 .38237 | 1.10 1.00 |
| 01111 c | 2004.016 | . 387593 | | 30012 | 6347.854 | . 386451 | 0.951 | | Isotope | | |
| 01111 d | | .388190 | 1.349 | 41101 @ | 6300.005 | . 390290 | 0.92 | 00001 | 0.00 | . 390235 | 1.330 |
| 21103 C | 2161.450 | . 391028 | 1.62 | 14411 cd 22211 C | 6296.047 "74.120 | .390017 .388662 | 1.27 1.53 | 01101 c | 648.484 | . 390598 | 1.330 |
| 21103 d | 2101.430 | . 392316 | | 22211 d | 74.120 | | 1.21 | 01101 4 | 012.101 | .391236 | 1.330 |
| 13302 cd | 2240.564 | . 392696 | | 30011 | 6503.081 | . 387974 | 0.719 | | | | |
| 21102 c 21102 d | 2229.240 | .390035 | | 11122 c 11122 d | 6527.956 | . 384804 . 385722 | 1.475 1.606 | 10002 02202 c | 1265.820 1297.269 | .390920 .391603 | 1.58 1.274 |
| 05501 cd | 2240.415 | . 393908 | | 11121 c | 6679.709 | . 384310 | | 02202 d | 1497.409 | . 391403 | 1.324 |
| 13301 ca | 2442.256 | . 392312 | | 11121 d | | .305127 | 1.115 | 10001 | 1270.667 | . 389707 | 1.160 |
| 21101 c | 3500.590 | .390461 | | 00031 | 6972.578 | . 380990 | 1.331 | 01102 c | 1096.49 | 101117 | 1 40 |
| 21101 d 10012 | 2612.944 | . 387496 | | 21114 C | 6668.274 | . 388547 | 1.725 | 01102 d | 1096.49 | . 391137 . 392096 | 1.40 1.13 |
| 02211 c | 2659.277 | . 388647 | 1.303 | 21114 d | | . 390246 | 1.825 | 03301 od | 1946.343 | . 392293 | 1.34 |
| 02211 đ | 2214 761 | 107051 | 1.273 | 31111 c | 6063.553 | . 386930 | | 11101 c | 2017.093 | .390015 | 1.18 |
| 10011 | 3714.781 | 387051 | 1.13 | 31113 d 31112 c | 7022.672 | . 388333 . 386755 | | 11101 d 00011 | 2283.490 | . 390975 . 387300 | 1.13 1.225 |
| 30004 | 2792.702 | . 391760 | 2.02 | 31112 d | 7022.072 | . 388127 | | | | | 1.223 |
| 22202 C | 3821.984 | . 392359 | | 20023 | 7133.819 | . 385288 | 1.75 | 20003 | 2507.56 | .391815 | 1.76 |
| 22203 d 14402 cd | 3898,117 | . 393434 | 1.68 1.54 | 12222 c 12222 d | 7166.049 | . 386017 | 1.15 1.35 | 12202 c 12202 d | 2531.63 | . 39220 | 1.22 1.40 |
| 30003 | 2942.492 | . 389584 | | 31111 c | 7203.824 | . 387607 | | 04401 cd | 2595.614 | . 392987 | 1.24 |
| 22202 C | 4007.950 | . 391485 | | 31111 4 | | . 389117 | | 20002 | 2645.666 | . 389826 | 1.46 |
| 22202 d 30002 | 4063.908 | . 389606 | 1.40 0.925 | 12221 c 12221 d | 7338.149 | 285497 | 1.33 1.28 | 12201 c 12201 d | 2706.25 | . 39126 | 1.30 1.34 |
| 14401 | 4122.247 | . 393036 | 1.26 | 20021 | 7277.679 | . 384403 | | 20001 | 2750.46 | .389670 | |
| 22201 c | 4197.412 | . 391719 | | 01131 C | 7602.529 | . 381503 | | 01111 c | 2920.244 | , 387664 | 1.325 |
| 22201 d 30001 | 4225.110 | . 391090 | 1.13 | 01131 4 | | . 302063 | 1.255 | 01111 d | | . 399286 | 1.225 |
| 11112 C | 4247.712 | . 387773 | | 40015 | 7262.961 | . 389550 | | 21103 C | 2127.2. | . 39155 | 1.70 |
| 11112 d | | . 388690 | | 22214 C | 7207.651 | . 389942 | | 21103 d | | . 39306 | 1.68 |
| 03311 cd 11111 c | 4214.912 4390.628 | . 389387 . 387350 | | 22214 d 40014 | 7466 520 | . 387322 | 1.64 1.92 | 13302 cc 21102 c | 3169.21 3289.71 | .39272 .39001 | 1.45 1.25 |
| 11111 d | 4370.020 | . 388230 | | 32213 c | 7466.520 7505.219 | . 388632 | | 21102 d | 3209.71 | . 39120 | 1.25 |
| 00021 | 4672.227 | . 384063 | | 32213 d | | | 1.1. | 13301 cd | | . 39188 | 1.25 |
| 23304 = | 4416.150 | . 391357 | 1 1/2 | 40013 32212 c | 7592.690 | . 385562 . 388252 | | 21101 c 21101 d | 2422.70 | . 39292 | 1.04 |
| 31104 C 31104 d | 4416.150 | . 393078 | | 32212 d | 7694.416 | . 100232 | 1.14 | 10012 | 2527.740 | .388030 | 1.10 1.56 |
| 31103 c | 4591.114 | . 389925 | 1.53 | 40012 | 7724.452 | . 386954 | 0.59 | 02211 c | 3557.314 | . 388668 | 1.28 |
| 31103 d | 4750 450 | . 391348 | | 21122 C | 7742.700 | . 385358 | | 02211 d | 2632 017 | 304734 | 1.33 |
| 33102 c 31102 d | 4752.450 | . 389708 . 391098 | | 21123 d 32211 c | 7697.572 | . 386488 . 388965 | | 10011 | 3632.917 | . 386726 | 1.21 |
| 20013 | 4652.620 | . 388188 | 1.77 | 32211 d | | | 0.939** | 30001 | 4145.95 | .39010 | 1.224 |
| 12212 C | 4887.970 | | 1.33 | 21122 c | 7901.479 | . 384008 | | 11112 c | 4147.224 | .38811 | 1.49. |
| 12212 d 31101 c | 4938.410 | . 389358 | 1.43 0.995 | 21122 đ 40011 | 7920.840 | . 385128 . 388558 | | 11112 d 03311 cd | 4194.704 | . 38915 . 389348 | 1.59 1.33 |
| 31101 4 | 4354.410 | . 391130 | | 21121 c | 6056.024 | . 384408 | | 11111 c | 4217.695 | . 387654 | 1.27 |
| 04411 cd | 4970.909 | | | 21121 d | | . 385525 | | 11111 d | 45.40.555 | .387977 | 1.26 |
| 20012 12211 c | 497, .830 5061.776 | , 386529 , 388508 | | 10032 02231 c | 8192.556 8332.880 | .381561 | | 00021 | 4542.552 | . 384360 | 1.33 |
| 12211 d | 3001.770 | , ,66,509 | 1.12 | 02231 4 | G.,2.000 | | 1.28 | 20013 | 4748.054 | .388845 | 1.815 |
| 20011 | 5099.666 | . 387448 | 0.921 | 10031 | 8293.957 | . 380805 | | 12212 c | 4770.965 | . 38925 | 1.25 |
| 01121 c 01121 d | 5215.720 | . 384548 . 385148 | | 0.00.7-4 | ependent i | nteractions | | 12212 d 04411 cd | 4831.99 | , 39003 | 1.27 1.34 |
| ATTAT G | | . 303146 | | , 0-0 | chairmann y | | • | 44454 00 | ******** | 1 12007 | 4.54 |

Table 9. Vibrational Energy Levels and Molecular Constants for ${\bf CO_2}$ (Contd)

| Energy | G | 3 | D Multiply by 10 ⁻⁷ | Energy Level | G | | Nultiply by 10 ⁻⁷ | Energy Level | G | 8 , | D Multiply |
|----------------------------|----------------------|---------------------|--------------------------------------|----------------------------------|----------------------|---------------------------------|---------------------------------|---------------------------|----------------------|----------------------|-----------------------------------------|
| | (cm ⁻¹) | (cm ⁻¹) | (cm ⁻¹) | | (cm ⁻¹) | (cm ⁻¹) | (cm ⁻¹) | | (cm ⁻¹) | (cm ⁻¹) | by 10 ⁻⁷ (cm ⁻¹) |
| | | | | | | | | | · · · · | | |
| 20012 | 4987.3% | 0.396847 | 1.4, | 21102 d | 3281.07 | 0.36916 | 1.12 | 11112 c | 4223.33 | 0.37616 | 1.31 |
| 12211 c | 4939.80 | . 38831 | 1.44 | 13301 cd | | . 37077 | 1.28 | 11112 4 | | . 37700 | 1.34 |
| 12211 d | | | 1.40 | 21101 c | 3453.99 | . 36881 | 0.98 | 11111 C | 4367.09 | .37600 | 1.18 |
| 20011 | 4991.350 | . 386705 | 0.94 | 21101 d | | . 37007 | 0.90 | 11111 d | | .37686 | 1.15 |
| 01121 C | 5168.600 | . 384695 | 1.33 | 10012 | 3571.143 | . 365284 | 1.27 | 00021 | 4655.205 | . 372674 | 1.20 |
| 01121 d | | . 385305 | 1.33 | 02211 c | 3632.52 | . 366595 | 1.19 | 20013 | 4821.500 | .376411 | 1.62 |
| | | | | d | | | 1.15 | 26012 | 4939.350 | .375131 | 1.21 |
| 21113 c | 5357.004 | . 388614 | 1.50 | 10011 | 3675.130 | . 365524 | 0.95 | 20011 | 5064.910 | . 376321 | 1.00 |
| 21113 d 1,312 cd | 5397.09 | . 390108 . 38978 | 1.30 | 30003 | 3056.65, | . 367405 | 1.24 | 21112 a 21112 d | 5593.645 | . 375625 . 376759 | 1.22 1.22 |
| 21112 c | 5519.944 | . 387038 | 1.16 | 30002 | 3987.610 | . 368174 | 0.91 | 00031 | 6945.610 | . 369691 | 1.20 |
| 21112 d | | . 388206 | 1.30 | 11112 c | 4201.19 | . 365666 | 1.23 | | 1 - | 6 % | 1.20 |
| 13311 cd | 5599.17 | . 38907 | 1.44 | 11112 d | | . 366423 | 1.26 | 00001 | 0.00 | . 368180 | 1.11 |
| 21111 c | 5662.269 | . 386837 | 1.10 | 03311 cd | 4293.35 | . 36726 | 1.19 | | | | |
| 21111 d | | . 387936 | I . w | 11111 c | 4346.13 | . 365716 | 1.05 | 01101 c | 643.23 | . 36857 | 1.12 |
| | | | | 11111 4 | | . 366568 | 1.00 | 01101 d | | . 36912 | 1.12 |
| 30014 | 5951.600 | . 389640 | 2.326 | 00021 | 4639.502 | . 362372 | 1.11 | | | | |
| 22213 ¢ 22213 d | 5970.949 | . 389913 | 1.57 | 20013 | 4791.260 | . 365734 | | 10002 | 1244.93 | . 36820 | 1.30 |
| 30013 | 6119.618 | . 387540 | 1.33 1.786 | 12212 C | 4936.63 | . 366707 | 1.25 1.27 | 02201 ⊂ 02201 d | 1286.86 | . 36951 | 1.14 1.11 |
| 22212 c | 6155.37 | . 38852 | 1.36 | 20012 | 4904.850 | . 364844 | 1.11 | 10001 | 1342.37 | . 36844 | 0.90 |
| 22212 d | 0100.07 | | 1.30 | 12211 c | 5012.55 | . 366735 | 1.26 | 00011 | 2265.973 | . 365388 | 1.11 |
| 30012 | 6241.964 | . 385859 | 1.113 | d | | | 1.06 | 20002 c | 2586.43 | .36778 | 1.04 |
| 22211 🧲 | 6326.049 | . 388103 | 1.04 | 20011 | 5042.570 | . 366124 | 0.86 | 01111 c | 299,. 58 | . 36579 | 1.12 |
| 22211 🖪 | | | 1.35 | 01121 c | 5277.147 | . 362848 | 1.06 | 01111 d | | . 36633 | 1.12 |
| 30011 | 6363.616 | . 387033 | | d | | . 363356 | 1.06 | 10012 | 3490.39 | . 36588 | 1.26 |
| 11122 c | 6374.49, | . 36521 | 1.46 | 21113 c | 5406.069 | . 365893 | 1.41 | 02211 C | 3529.59 | . 36671 | 1.14 |
| 11122 d | | . 38607 | 1.56 | d | | . 366904 | | 02211 d | | | 1.12 |
| 00031 | 6790.215 | . 301353 | 1.33 | 21112 c | 5558.553 | . 365318 | 1.10 | 10011 | 3567.54 | . 36525 | 1.01 |
| 33334 - | /FF2.0F4 | . 388958 | 1 (2 | 21111 c | 5727.046 | . 365948 | 1.10 1.11 | 00021 20012 | 6S06.749 4814.570 | .36260 | 1.11 |
| 31114 c 31114 d | 6552.954 | . 390896 | 1.63 1.63 | 4 | 5/2/.046 | . 367138 | | 20012 | | .364810 pa 637 | 1.11 |
| 31113 c | 6736.6% | . 387368 | 1.63 | 10022 | 5858.022 | . 362490 | | 00001 | 0.00 | .379658 | 1.21 |
| 31113 4 | 0730.0% | . 388906 | 1.58 | 02221 🗷 | 5915.23 | . 36376 | 1.18 | 01101 c | 645.72 | . 379036 | 1.22 |
| 31112 c | 6692.054 | .386378 | 1.33 | d | | | 1.15 | 01101 4 | 0.0.72 | . 379627 | 1.22 |
| 31112 u | | . 387706 | 1.16 | 10021 | 5959.5% | . 362605 | | 10002 | 1254.93 | . 37900 | 1.40 |
| 31111 c | 7046.029 | . 386858 | 1.23 | 30014 | 593.58L | . 366337 | | 02201 C | 1292.90 | . 38000 | 1.22 |
| 31111 d | | . 388236 | 0.93 | 30013 | 6127.782 | . 364495 | 1.31 | 02201 | | | 1.22 |
| 01131 c | 7393.599 | . 381803 | 1.33 | 30012 | 6254. 592 | . 365274 | | 10001 | 1355.52 | . 37849 | 1.04 |
| 01131 d | | . 382391 | 1.33 | 30011 | 6429.172 | | 0.60 | 00011 | 2274.33 | . 37579 | 1.21 |
| 40040 | 7404 540 | 305435 | | 00031 | 6922.210 | . 359479 | 1.10 | 01111 c | 2918.38 | .37617 | 1.22 |
| 40013 | 7481.510 7600.130 | . 385435 | 0.33 | 40000 | | . 359684 | 4.05 | 01111 d 10002 | 0500.07 | .37675 | 1.22 |
| 40012 10032 | 7981.1-0 | . 382275 | 0.63 1.52 | 10032 10031 | 6120.104 9220.363 | . 359656 | 1.25 0.95 | 10002 | 3509.07 3609.05 | .37641 .37540 | 1.41 1.11 |
| 10032 | 8089.040 | . 380735 | 1.26 | 10031 | I so top | | 0.73 | 10001 | | pe 828 | 1.14 |
| 10031 | Isotop | | 1.20 | wool | 0.00 | | 1.20s | 00001 | 0.00 | .346799 | 1.04 |
| 0 0 0 0 1 | 0.00 | . 368164 | 1.11 | | | | | 01101 c | 6\$7.33 | .347224 | 1.04 |
| | | | | 01101 c | 664.735 | . 379065 | | 01101 d | | .347736 | 1.04 |
| 01101 c | 662.368 | . 368588 | 1.13 | 01101 d | | . 379639 | 1.22 | 10002 | 1230.20 | . 34620 | |
| 01101 d | | . 369128 | 1.13 | | | | | 02201 c | 1315.08 | .34812 | 1.10 |
| • | | | | 10002 | 1271.975 | . 378738 | | 02201 d | | | 1.04 |
| 10002 | 1259.430 | . 368114 | 1.26 | 02201 c | 1329.87 | . 380061 | | 10001 | 1347.22 | .34776 | |
| 02201 c 02201 d | 1325.15 | . 369520 | 1.20 1.16 | 02201 d 10001 | 1376.28 | 170004 | 1.22 1.04 | 00011 01111 c | 5313.97 2959.06 | . 34412 . 34455 | 1.04 |
| lowl | 1365.845 | . 368502 | 0.962 | 10001 | 13/0.20 | . 3/0000 | 1.04 | 01111 4 | 2959.06 | . 34504 | 1.04 |
| 10 W I | 1303,043 | . 100102 | 0.706 | 11102 c | 1916.31 | . 37903 | 1.27 | 10002 | 3525.205 | . 343840 | |
| 11102 c | 1901.748 | . 36845 | 1.23 | 11102 d | | . 37989 | 1.32 | 10001 | 3639.067 | . 344636 | |
| 11102 d | | . 36925 | 1.26 | | 1995.36 | . 37977 | 1.22 | | Isotop | | 0.707 |
| 03301 cd | 1988.328 | .370182 | 1.20 | 11101 c | 2062.41 | . 37894 | 1.15 | 00001 | 0.00 | . 35695 | 1.07 |
| 11101 c | 2049.346 | . 36860 | 1.06 | 11101 d | | . 37987 | 1.10 | 01101 c | 659.70 | .35737 | 1.08 |
| 11101 d | | . 36954 | 1.01 | 00011 | 2340.01 | . 375659 | 1.20 | 01101 d | | . 35789 | 1.00 |
| 00011 | 2332.112 | . 365267 | 1.11 | | | | | 00011 | 1322.52 | .35419 | 1.07 |
| | | | | 20003 | 2523.58 | . 37924 | | | | | |
| 20003 | 2500.776 | .368463 | 1.44 | 12202 c | 2566.33 | . 380125 | | | | | |
| 12202 C | 2549.425 | . 36954 | 1.25 | 12202 d | 2641 27 | 3401 4 | 1.25 | | | | |
| 12202 d 20002 | 2614.235 | . 367807 | 1.27 | 20002 12201 ¢ | 2641.26 2743.66 | . 37814 . 3 8 005 | 1.18 1.20 | | | | |
| 20002 04401 cđ | 2614.235 2651.975 | .36/80/ | 1.04 | 12201 c 12201 d | 2/43.00 | . 30003 | 1.20 | | | | |
| 12201 C | 2729.264 | . 36966 | 1.30 | 20001 | 2776.00 | . 37927 | 0.88 | | | | |
| 12201 d | 2,2,.204 | | 1.07 | 01111 6 | 2992.310 | .376103 | | | | | |
| 20001 | 2727.229 | . 369039 | 0.77 | 01111 d | 0 | . 376664 | | | | | |
| 01111 c | 2982.106 | . 365707 | 1.13 | 10012 | 3590.86 | . 375835 | | | | | |
| | | | | 02211 C | 3645.02 | . 377091 | | | | | |
| 21103 C | 3127.31 | . 36455 | 1.34 | "2211 d | | _ | 1.22 | | | | |
| 21103 d | | 36 157 | 1.43 | 10011 | 3693.64 | . 375754 | 1.06 | | | | |
| 13302 cd | 3200.15 | .3 /23 | 1.28 | | | | | | | | |
| 21102 c | 3291.07 | . 36817 | 1.14 | | | | | | | | |

this **scheme**, v_2 is always equal to ℓ .) The desirability **of labelling** the states in Fermi resonance by the same symbols except for \mathbf{r} is to emphasize the very important role played by the Fermi resonance, which is very nearly exact for most of the groups. It must also be emphasized very strongly that the long-established custom of calling the upper level of the $(10^0 0,02^0 0)$ resonance at 1388.18 cm $^{-1}$, v_1 , and the lower level at 1285.41, $2v_2$, is not only confusing the issue, but is wrong, since the now ten year old work of **Amat** and Pindert (19651 has shown that the unperturbed position of $2v_2^0$ lies above that of v_1^0 , in the 626 isotope. This is also true in 627, 628, and 828, but in 636, 637, 638, it lies below. It seems vastly preferable always to label the upper level 10001 and the lower 10002.

4.2.2 LINE INTENSITIES

The intensity data (summarized in Table 10) are based on quantitative studies of resolved lines where such exist; and where not, on total intensities in a given region. The relations between the strengths of the principal band in a region and its associated weaker "hot" and isotopic neighbors were based on computations relating the transition moments to the vibrational eigenfunctions, taking into account terms up to the quartic in the molecular constants, with particular attention to the degree of Fermi mixing in the states, and an approximate calculation of the "unperturbed" (before Fermi mixing) transition moments. This procedure appears to give fairly good agreement for the ground-state and "first-hot" transitions in such Fermi groups as 2001-0000 and 3001-0000, and seems adequate for estimating strengths of higher unobserved hot bands. However, when experimental data are available (Burch, 19701, as for the 12201-11102 band at 828.28 cm -1, these were used.

For the isotopic molecules, empirical data were again used where available, as for 628 bands which are forbidden in the symmetric molecules. When the isotopic bands overlap stronger bands of 626, the abundance ratios were **used to** estimate the total strength of a group, but the particular Fermi parameters were used to divide the strengths.

The influences of vibration-rotation interactions on line intensities has been **measured** in some cases. As a generalization, it can be said that these are usually negligible for the parallel bands ($\ell' - \ell'' = 0$) but become of considerable importance for all the perpendicular bands ($\ell' - \ell'' = t_1$) except those in the 15 μ m region. For all the other bands, Coriolis-type resonances are responsible for inducing a large part of the transition moment in the R- and P-branches, thus "borrowing" intensity from the stronger parallel bands, while leaving the Q-branches unchanged. Accordingly, the latter may remain very weak (or in some cases be unobservable - for example, the 410 group). We have used the approximate equation $\mathbf{S_m} = \mathbf{S_v}^0$ (1 t m $\mathbf{\xi_v}$)² to correct for this interaction, with the values

Table 10. Band Origins and Intensities for CO,

| Band Center Vo | Upper Level | Lower | tope | & at 296K (multiply by 10 ⁻²⁷ mol ⁻¹ | Band Center Vo | Upper Level | Lover | Iso- tope | SW at 296K (multiply 4 10 ⁻²² mol ⁻¹ |
|---------------------------|-----------------------|------------------------|-------------------|------------------------------------------------------------------|---------------------------|-----------------------|-----------------------|-------------------|------------------------------------------------------------------|
| (cm ⁻¹) | | | | cma ² ca ^{−1}) j் | (cm ⁻¹) | | | | cm² cm²¹) 5 |
| 471.415 | 20003 | 11101 | 626 | 0.0097 | 681,27 | ,220, | 11101 | 627 | .0082 Q |
| 479.929 | 13302 | 12201 | 626 | .0012 | 681.521 | 13301 | ,220, | 626 | .460 |
| 494.537 506.141 | 12202 12202 | 11101 11101 | 436 626 | .00079 Q .0516 | 693.501 | 11101 | 10001 | 626 | .77 |
| 510.337 | 2.103 | 20002 | 626 | .0040 | 683.870 696.13 | 12201 11101 | 11101 | 626 627 | 9.05 0.13 |
| 526.423 | 1,102 | 10001 | 636 | .035 | 669.679 | 11101 | 10001 | 626 | 148.8 |
| 535.903 | 11102 | 10001 | 628 | . 011 Q | 696.623 | 2220, | 21101 | 626 | 0.0195 |
| 542.1% 544.283 | 21102 11102 | 20003 10001 | 626 626 | .00711 2.723 | 699.14 | 10001 | 01101 | 638 | . 058 |
| 546.275 | 13302 | 04401 | 629 | 0.00026 Q | 703.477 703.436 | 10001 21101 | 01101 20001 | 626 | 9.20 0.246 |
| 557 .642 | 14402 | 05501 | 626 | .00253 | 707.993 | 20001 | 11101 | 629 | .024 |
| 561.097 564.999 | 12202 20002 | 03301 | 628 628 | .0058 .0043 | 709.80 | 10001 | 01101 | 637 | .0094 |
| 568.874 | 13302 | 11101 04401 | 626 | .0716 | 710.765 711.545 | 10011 | 01111 | 626 | .0202 |
| 570.97 | 12202 | 03301 | 627 | .00092 Q | 712.487 | 10001 20002 | 01101 11102 | 627 62. | 1.26 0.013 |
| 573.536 | 13302 | 04.0, | 636 | .00115 | 713.397 | 20001 | 11101 | 636 | .047 |
| 576.599 579.605 | 11102 21102 | 0220, ,220, | 629 626 | .169 .0376 | 713.59 | 20001 | 11101 | 627 | .0038 |
| 579.95 | 20002 | 11101 | 627 | .00072 Q | 720.299 720.909 | 20001 10001 | 11101 01101 | 626 626 | 4.794 ,953. |
| 581.424 | 22203 | 13302 | 626 | .0096 | 720.909 | 10001 | 01101 | 636 | 17.9 |
| 581.768 565.297 | 12202 12202 | 03301 03301 | 626 636 | 1.934 • 034 | 724.196 | 11101 | 02201 | 628 | 0.315 |
| 596.44 | 11102 | 02201 | 627 | .0439 | 724.95 732.54 | 20002 11101 | 1,102 0220, | 627 627 | .0024 <i>Q</i> .0474 |
| 569.46 | 21102 | 12201 | 636 | .00055 Q | 733.45 | 12201 | 2000, | 636 | .0021 Q |
| 594.248 | 20002 21103 | 11101 | 626 | .908 | 736.643 | 20002 | 11102 | 626 | 3,021 |
| 595.65 596.444 | 21103 | 12202 12202 | 636 626 | .0038 .257 | 739.624 | 11101 | 0220, 03301 | 636 | 0.70 |
| 597.062 | 10002 | 01101 | 628 | 5.19 | 739.936 739.855 | ,220, 21101 | ,220' | 636 626 | .0157 .176 |
| 597.34, | 11102 | 0220, | 626 | 52.09 | 741.736 | 11101 | 02201 | 626 | 79.01 |
| 599.028 599.22, | 20003 11102 | 11102 02201 | 628 636 | 0. 0031 .702 | 748.32 | 12201 | 03301 | 627 | 0.0025 0 |
| 601.70 | 10002 | 01101 | 638 | .055 | 746.5% 753.055 | 20002 13301 | 11102 04401 | 636 628 | .0378 .00058 Q |
| 607.14 | 10002 | 01101 | 627 | 1.17 | 754.334 | 21102 | 12202 | 626 | ,1607 |
| 607.27 | 20003 | 11102 | 627 | 0.021 | 757.497 | ,220, | 03301 | 626 | 3.296 |
| 607.993 608.828 | 20002 10012 | 11101 01 111 | 636 626 | .0111 .0175 | 765.896 770.355 | 13301 ,330' | 04401 04401 | 634 626 | 0.00173 Q .1351 |
| 609.1, | 10002 | 01111 | 637 | .0106 | 771.273 | 11101 | 10002 | 636 | .138 |
| 611.01 | 20003 | 11102 | 636 | .102 | 781.872 | 1.40, | 05501 | 626 | .0051 |
| 615.810 | 20003 | 11102 | 626 | 6.99 | 789.916 790.536 | 11101 11101 | 10002 10002 | 626 627 | .056 .010 Q |
| 617.336 616.033 | 10002 10002 | 01101 01101 | 636 626 | 20.5 1436. | 791.060 | 21102 | 20003 | 626 | .0548 |
| 619.78 | 21103 | 20003 | 636 | 0.0085 | 791.452 | 11101 | 10002 | 626 | 11.23 |
| 633.170 | 21103 | 20003 | 626 | .649 | 603.76 | 12201 1220, | 11102 11102 | 636 639 | 0.0052 .0009 ♀ |
| 636.754 637.56 | 01111 13302 | 00011 12202 | 636 636 | .0121 .013 | 926.516 828.265 | ,220, | 11102 | 624 | .201 |
| 640.670 | 11102 | 10002 | 636 | 2.60 | 929.467 | 21101 | 20003 | 626 | .0548 |
| 642.319 | 11102 | 10002 | 628 | 0.78 | 657.250 | 13301 | 12202 | 624 | .0110 .0432 |
| 643.23 644.435 | 01101 11102 | 00001 10002 | 638 627 | 3.57 0.15 | 964.694 863.15, | 20001 01111 | 1,102 11101 | 626 636 | .00495 |
| 645.72 | 01101 | 00001 | 637 | .642 | 996.542 | 02211 | 12201 | 626 | .0132 |
| 646.11 | 0220, | 01101 | 637 | .055 | 913.423 | 00011 | 10001 | 636 | .0614 |
| 647.056 648.484 | 11102 01101 | 10002 00001 | 626 636 | 222 , 960. | 915.584 917.627 | 21101 10011 | 12202 20001 | 626 626 | .00195 Q .0087 |
| 648.785 | 02201 | 01101 | 636 | 73.4 | 927.15, | 01111 | 11101 | 626 | .3556 |
| 649.074 | 03301 | 0220, | 636 | 4.69 | 932.760 | 01111 | 11101 | | .00135 |
| 649.271 | 04401 | 03301 | 636 | 0.266 ,01<2 | 941.731 952.310 | 10012 21101 | 20002 20003 | 626 626 | .01146 .00064 0 |
| 649.580 650.02 | 05501 12202 | 04401 11102 | 636 627 | .0162 | 952.310 960.959 | 00011 | 10001 | 626 626 | 4.910 |
| 652.536 | 12202 | 11102 | 626 | 16.52 | 963.73 | 00011 | 10001 | 427 | .0032 |
| 654.870 | 01111 | 00011 | 626 | 0.885 | 966.267 1017.670 | 00011 00011 | 10001 10002 | 639 636 | .0195 .0726 |
| 655.558 657.31 | 13302 01101 | 12202 20001 | 626 820 | 0.990 ,343 | 1017.670 | 01111 | 11102 | 636 | .00072 |
| 657.69 | 02202 | 00111 | A28 | .0277 | 1063.734 | 00011 | 10002 | 626 | 6.324 |
| 657.553 | 14402 | 13302 | 626 | .0442 | 1068.135 | 00011 | 10002 | 627 | .0047 |
| 659.79 661.32 | 01101 | 00001 12201 | 72H 636 | .0635 .0055 | 1071.546 1072.682 | 00011 | 11102 10002 | 628 | .540 .0285 |
| 662.368 | 01101 | 00007 | 628 | 330. | 1074.271 | 02211 | 12202 | 626 | .0227 |
| 662.782 | 02201 | 01101 | 628 | 26.2 | 1080.358 | 01111 | 11102 | | .00243 |
| 663.157 663.178 | 12201 03301 | 11101 0220, | 636 628 | 0.106 1.50 | 1239.380 | 11102 | 01101 | 629 | 0.035, |
| 663.547 | 04401 | 0220, 03301 | 628 | 0.078 | 1244.93 | 10002 | 00001 | 638 | .0038 |
| 664.735 | 01101 | 00001 | 627 | 62.2 | 1259.430 | 10002 | 00001 | 628 | . 382 |
| 665.135 | 02201 | 01101 | 627 | 4.69 0.365 | 1271.875 | 10002 10001 | 00001 00001 | 627 636 | .0220 .0068 |
| 665.49 667.026 | 03301 | 02201 10001 | 627 636 | 1.58 | 1342.37 1365.645 | 10001 | 00001 | 629 | . 561 |
| 667.379 | 01101 | 00001 | 626 | 2 82580. | 1376.28 | 10001 | 00001 | 627 | .0323 |
| 667.750 | 02201 | 01101 | 626 | 6488. | 1386.978 | 11101 | 01101 | 629 | .0516 |
| 668.109 | 0330, | 02201 20002 | 626 626 | 392.4 0.332 | 1946.321 | 21103 | 0220, | 626 | .000331 |
| 666.227 669.452 | 21102 04401 | 03301 | 626 | 18.45 | 1959.02 | 20003 | 01101 | 636 | .000161 |
| 668.785 649.10 | 0550, | 04401 | 626 | 0.976 | 1960.232 | 30004 | 11102 | 626 | .00004 ~.1 |
| | | 05501 | 626 | .077 | 1965,607 | 30003 | 11101 | 626 | .000071 |

Table 10. Band Origins and Intensities for $\mathbf{CO_2}$ (Contd)

| Center v _o (cm ⁻¹) | Upper Level | Lovel | Iso- tope | sV at 296K (multiply by 10 ⁻²² mol ⁻¹ om ² cm ⁻¹) 5 | Bend Center Wo (cm ⁻¹) | Upper Level | Lower Level | Iso- tope | SV at 296K (multiply by 10 ⁻²² mol ⁻¹ cm ² cm ⁻¹) J |
|-------------------------------------------|----------------|-----------------------|--------------------|-----------------------------------------------------------------------------------------------------------|---------------------------------------------|-----------------------|-------------------------|-------------------|-----------------------------------------------------------------------------------------------------------|
| | | | | • | | | | | |
| 1883.146 1889.514 | 12202 22203 | 01101 | 63 6 626 | 0.0014906 | 2299.442 2301.041 | 11112 12211 | 11102 12201 | 629 6% | 0.686 3.17 |
| 1896.490 | 11102 | 00007 | 636 | .0012708 .014906 | 2301.73 | 01111 | 01101 | 929 | 0.31 |
| 1896.038 1901.748 | 21103 11102 | 10002 | 626 628 | .0110107 .0297606 | 2301.909 2302.365 | 10021 10022 | 10011 10012 | 6 26 6% | 0.0269 0.0473 |
| 1905.435 | 13302 | 02201 | 626 | .178606 | 2305.340 | 20013 | 20003 | 626 | 4.352 |
| 1917.627 1930.985 | 12202 22202 | 01101 11101 | 626 626 | .4226055 .0008206 | 2306.717 2307.02 | 20012 11112 | 20002 1'102 | 626 627 | 2.3% 0.116 |
| 1932.470 | 11102 | 00001 | 624 | 4.092062 | 2307.37 | 02211 | 02201 | 629 | 10.5 |
| 1951.153 1996.602 | 21102 20002 | 10001 01101 | 626 636 | .0070706 .001504 | 2307.39 2309.295 | 00021 10011 | 00011 10001 | 629 629 | 0.0791 4.47 |
| 2003.734 | 20002 | 01101 | 626 | .0081803 | 2311.675 2311.713 | 03311 10012 | 03301 10002 | 626 629 | 122.9 7.29 |
| 2004.211 | 21102 30003 | 02201 11102 | 626 6% | .0011804 .0001305 | 2311.715 | 01121 | 01111 | 626 | 1.793 |
| 2037.093 | 11101 | 00001 | 636 | .18605 | 2313.744 2313.97 | 11111 | 11101 00001 | 626 828 | 8.56 3,60 |
| 2049 . 346 20 65 . 846 | 11101 12201 | 00001 01101 | 628 628 | .037203 .005203 | 2335.15 | 02232 | 02202 | 627 | 1.91 |
| 2062.41 2075.380 | 11101 22202 | 00001 11102 | 627 626 | .0052035 | 2315.243 2317.36 | 11112 | 11102 10001 | 6 % 627 | 17.11 0.805 |
| 2076.865 | 11101 | 00001 | 626 | 22.32041 | 2318.985 | 10012 | 10002 | 627 | 1.29 |
| 2093.356 2094.861 | 12201 20001 | 01101 01101 | 626 628 | 3.958038 0.005504 | 2319.738 2322.52 | 01111 00011 | 01101 00001 | 628 729 | 25 8. 1,35 |
| 2101.996 | 20001 | 01101 | 636 | .014903 | 2324.146 | 02211 | 02201 | 626 | 3080. |
| 2107.127 2112.461 | 13301 21101 | 02201 10001 | 626 626 | .253035 .11208 | 2324.182 2326.594 | 00021 10011 | 00011 10001 | 626 624 | 20.98 1183. |
| 2119.119 | 14401 | 03301 | 626 | .0156033 | 2327.432 | 10002 | 10002 | 626 | 1934. |
| 2120.548 2127.235 | 22201 12212 | 11101 1220, | 626 626 | .011904 .00247 | 2327.575 2332.112 | 01111 00011 | 01101 00001 | 627 626 | 49.7 3330. |
| 2129.775 | 20001 | 01101 | 626 | 1.302046 | 2336.637 | 01111 | 01101 | 626 | 76600. |
| 2148.245 2157.673 | 30001 10012 | 11101 10001 | 626 636 | .0059510 .0152 | 2340.01 2349. 146 | 00011 00011 | 00001 | 627 626 | 637. 95 980 0. |
| 2165.461 | 21101 | 02201 | 426 | .059505 | 2367.097 | 10011 | 10002 | 6 % | 0.0131 |
| 2170.848 | 11112 20012 | 11101 20001 | 626 626 | .0507 .000 9 2 | 2415.700 2429.547 | 10011 20011 | 10002 20002 | 628 6% | .0056 .00146 |
| 2182.507 | 20013 | 20002 | 626 | .00172 | 2429.349 | 10011 | 10002 | 6 % | 1.059 |
| 2205.298 2224.647 | 10012 10012 | 10001 | 628 626 | .00558 1.272 | 2429.5% WM.159 | 20012 11111 | 20003 11102 | '26 626 | 0.00256 .0402 |
| 2225.05 | 05511 | 05500 | 636 | 0.00261 | 2464.942 | 21103 | 01101 | 6 % | .0058 |
| 2227.88 2229.724 | 13312 21113 | 13302 2'103 | 636 636 | .00401 .00488 | 2 M o . 7 7 2523.56 | 20003 | 00001 00001 | 62. 627 | .075 .0060 |
| 2230.234 | 21112 | 21102 | 636 | .00216 | 2599.43 2414.235 | 20003 20002 | 00001 | 6 % | .0020 |
| 2236. 376 2238.55 | 04411 12211 | 04401 1220, | 636 436 | .0632 .0384 | 2618.702 | 21102 | 01101 | 629 626 | .186 .0148 |
| 2239.355 2240.558 | 12212 20013 | 12201 20003 | 636 636 | . 129 | 2641.26 2757.229 | 20002 20001 | 00001 | 627 626 | .018 .022 |
| 2240.87 | 20011 | 20001 | 636 | .0724 .0122 | 2776.00 | 20001 | 00001 | 627 | .0023 |
| 2242. 304 2242.776 | 20012 00021 | 20002 00011 | 636 638 | . 0258 . 00124 | 2791.622 | 21101 | 01101 | 626 | .0015 |
| 2242.73 | 02211 | 02201 | 636 | .149 | 3125.32, | 30004 | 01101 | 626 | .00024 .40 |
| 2245.17 2245.46 | 10011 10012 | 10001 10002 | 639 638 | .0555 .0816 | 3154.605 3181.45 | 22203 21103 | 01101 00001 | 626 626 | .00074 .40 |
| 2248.356 | 01121 | 01111 | 636 | .0280 | 3275.113 | 30003 | 01101 | 626 | .0102 .02 |
| 2248.361 2250.602 | 03311 11111 | 03301 11101 | 636 636 | 1.52 0.96 | 3291.07 3269.71 | 21102 21102 | 00001 | 629 636 | .00017 .14 .00042 .14 |
| 2250.744 | 11112 | 11102 | 636 | 1.9' | 3339.340 3340.471 | 21102 | 10000 | 626 | .0417 .14 |
| 2251.01 2253.24 | 02211 10012 | 02201 10002 | 637 637 | 0.0264 0.0146 | 3396.529 | 22202 30002 | 01101 01101 | 626 626 | .0063 .14 .00185 .30 |
| 2253.53 | 10011 | 10001 | 637 | .0098 | 3399.2% 3450.75 | 21113 21113 | 11101 03301 | 624 636 | .00413 |
| 2254.35 2260.045 | 01111 02211 | 01101 02201 | 638 636 | 3 . u 34.6 | 3460.534 | 21113 | 11102 | 636 | .0174 .0409 |
| 2260.062 2261.920 | 00021 10012 | 100011 | 636 636 | 0.306 20.3 | 3465.433 3473.716 | 20013 12212 | 10001 02201 | 626 636 | .1786 .3422 |
| 2262.66 | 01111 | 01101 | 637 | 0.62. | 3492.239 | 20013 | 10002 | 636 | -450 |
| 2262.850 2265,973 | 10011 00011 | 10001 00001 | 636 629 | 12.3 38.6 | 3 482.851 34%. 3% | 21112 10012 | 11101 | 6 % 63. | .0134 .463 |
| 2271.763 | 01111 | 01101 | 636 | ele. | 3497.46 | 4 30001 | 01101 | 636 | .0 pert |
| 2274.33 2274.367 | 00011 06611 | 00001 06601 | 637 626 | 7.15 0.0068 | 3498.750 3500.590 | 11112 21101 | 01101 00001 | 636 626 | 7.314 .1052 ,14 |
| 2281.688 | 22213 | 22203 | 626 | .0369 | 3504.320 3504.933 | 21103 | 11102 | 628 | .0110 |
| 2282.69 2283.490 | 04411 00011 | 04401 | 626 636 | .0157 9602. | 3508.07 | 14412 100'2 | 04401 00001 | 626 637 | .0475 .0771 |
| 2284.286 | 12211 | 12201 | 628 | 0.0115 | 3509.207 3511.59 | 21302 11112 | 11101 | 62. 626 | .0046 .161 |
| 2286.779 2287.205 | 05511 12212 | 03501 12263 | 626 629 | .1942 .0262 | 3517.323 | 20032 | 10001 | 636 | .177 |
| 2288.352 2290.615 | 13311 20012 | 13301 20002 | 626 626 | .11 6 3 .0107 | 3525.205 3527.703 | 10012 30014 | 00001 20003 | 828 626 | .0588 .1034 |
| 2290, 484 | 20013 | 20003 | 628 | . 0180 | 3527.740 | 10012 | 00001 | 636 | 94.2 |
| 2290.715 2293.420 | 13312 21112 | 1 3302 21102 | 626 626 | .3125 .1919 | 3527.757 3531.93 | 22212 20013 | 12201 10002 | 6 % 629 | .0374 .181 |
| 2293.621 | 21113 | 21103 | 626 | . 3965 | 3533.942 | 11122 | 01111 | 626 | .0353 |
| 2296.784 2295.022 | 11111 03311 | 11101 03301 | 628 628 | .325 .406 | 3530.022 3539.005 | 11112 20012 | 01101 1 00 01 | 628 629 | 4.449 . 0761 |
| | | | 626 | | 5557.005 | | | 029 | . 4744 |

Table 10. Band Origins and Intensities for ${
m CO_2(Contd)}$

| Band Center Vo | Upper Level | Lower Level | Iso- tope | SV at 296K (multiply by | Band Center Vg | Upper Level | Lower Level | iso- tope | s at 296K (multiply by |
|-------------------------|----------------|----------------|--------------|-------------------------------------|----------------------|----------------|----------------|----------------------------|--------------------------------------|
| | | | | 10 ⁻²² mol ⁻¹ | _ | | | | 10 ⁻²² mol ⁻¹ |
| (cm ⁻¹) | | _ | | cm² cm²¹) 5 | (cm ⁻¹) | | | | cm ² cm ⁻¹) 1 |
| 3549.625 | 20013 | 10002 | 627 | 0.0224 | 4807.692 | 21113 | 01101 | 626 | 6.695 |
| 3550.700 3552.841 | 30012 12212 | 20001 02201 | 626 626 | 0.0195 31.25 | 4808.188 4814.570 | 40002 20012 | 01101 00001 | 626 63 8 | 0. pert .0134 |
| 3555.895 | 21112 | 11101 | 626 | 1.101 | 4821.500 | 20013 | 00001 | 627 | .0744 |
| 3556.749 3558.595 | 30013 | 20002 01101 | 626 | 0.0629 | 4839.737 | 30013 | 10001 | 626 | .1376 |
| 3563.070 | 11112 20012 | 10001 | 627 627 | .668 .0135 | 4853.620 4871.46 | 20013 21112 | 00001 01101 | 626 636 | 80.7 .238 |
| 3566.063 | 10022 | 00011 | 626 | . 208 | 4887.390 | 20012 | 00001 | 636 | 2.976 |
| 3568.208 3571.143 | 20013 10012 | 10002 | 626 628 | 33.78 52.2 | 4887.970 | 12212 | 00001 | 626 | (8.1-08 A) |
| 3578.670 | 22213 | 12202 | 626 | 0.138 | 4896.185 4904.850 | 21112 20012 | 01101 | 628 628 | .0 693 1.116 |
| 3580.334 | 11112 | 01101 | 626 | 803.5 | 4925.010 | 30011 | 00001 | 638 | 0.00446 |
| 3587.540 3590.86 | 10011 10012 | 00001 00001 | 638 627 | 0.703 8.41 | 4928.910 4931.083 | 21112 | 01101 | 627 626 | .00744 .0 96 7 |
| 3609.05 | 10011 | 00001 | 637 | 0.126 | 4939.350 | 3113 20012 | 11102 00001 | 627 | .2306 |
| 3612.844 | 10012 | 00001 | 626 | 10350. | 4942.512 | 30013 | 10002 | 626 | 1.414 |
| 3621.283 3621.570 | 20012 20012 | 10001 10002 | 636 636 | 0.283 0.435 | 4946.807 4953.363 | 31112 22212 | 11101 02201 | 626 626 | 0.0595 1.042 |
| 3623.454 | 21112 | 11102 | 636 | .0433 | 4959.667 | 30012 | 10001 | 626 | 0.837 |
| 3625.176 | 21111 | 11101 | 636 | .0324 | 4965.381 | 21112 | 01101 | 626 | 26,56 |
| 3632.917 3638.067 | 10011 | 00001 | 636 828 | 160. 0.0392 | 4977.830 4991.35 | 20012 | 00001 | 626 636 | 349.7 2.12 |
| 3641.717 | 13311 | 03301 | 636 | .0240 | 5013.785 | 21101 | 01101 | 6 36 | 0.1711 |
| 3659.277 3655.42 | 02211 20012 | 00001 10002 | 626 628 | (1.7-06 △) .187 | 5028.78 5042.57 | 22211 20011 | 02201 00001 | 636 628 | .00298 |
| 3656.805 | 21112 | 11102 | 628 | .0149 | 5061.776 | 12211 | 00001 | 626 | .227 (9.2−08 △) |
| 3667.475 | 20012 | 10002 | 627 | .0333 | 5062.442 | 30012 | 10002 | 626 | . 238 |
| 3667.544 3675.130 | 10021 10011 | 00011 | 626 628 | . 363 47.8 | 5064.680 5068.910 | 21111 20011 | 01101 00001 | 628 627 | . 260 . 0632 |
| 3675.694 | 11121 | 01111 | 626 | 0.0331 | 5099.66 | 20011 | 00001 | 626 | 112.3 |
| 3676.725 | 20011 | 10001 | 628 | .164 | 5114.894 | 30011 | 10001 | 626 | 0.309 |
| 3676.741 3679.644 | 30012 30013 | 20002 20003 | 626 626 | .0915 .0986 | 5123.20 5139.401 | 21111 22211 | 01101 02201 | 626 626 | 10.64 0.409 |
| 3683.762 | 11111 | 01101 | 628 | 3.884 | | ***** | 01101 | 020 | 0.409 |
| 3677.702 3687.40 | 21111 12211 | 11101 | 628 | 0.0134 | 5168.60 | 01121 | 00001 | 636 | .00372 |
| 3692.41A | 20012 | 02201 10002 | 628 626 | .143 42,4 | 5217.669 5247.030 | 30001 10022 | 10002 01101 | 626 626 | .0234 .nlnl |
| 3693.640 | 10011 | 00001 | 627 | 10.2 | 5277.07 | 01121 | 00001 | 628 | .00149 |
| 3699.064 3700.290 | 20011 21112 | 10001 11102 | 627 626 | 0.0279 3.549 | 5291.16 5315.73 | 02221 01121 | 01101 | 62 6 62 6 | .0275 .390 |
| 3702.345 | 11111 | 01101 | 627 | 0.771 | 5349.36 | 10021 | 01101 | 626 | .00506 |
| 3703.486 | 22212 | 12202 | 626 | .1503 | | | | | |
| 3705.927 3711.473 | 30011 20011 | 20001 10001 | 626 626 | .0551 35.01 | 5584.391 5687.166 | 00031 00031 | 10001 10002 | 626 626 | .00707 .00751 |
| 3713.714 | 21111 | 11101 | 626 | 2.816 | | | | | |
| 3713.795 3714.781 | 22211 10011 | 12201 00001 | 626 626 | 0.1094 15000. | 5858.022 5951.600 | 10022 30014 | 00001 00001 | 628 636 | .00372 .00179 |
| 3723.249 | 11111 | 01101 | 626 | 1135. | 5959.954 | 10021 | 00001 | 628 | .00335 |
| 3725.530 | 20011 | 10002 | 636 | 0.0078 | 5972.52 | 32214 | 02201 | 626 | .00253 |
| 3726.351 3726.647 | 14411 12211 | 04401 02201 | 626 626 | .0499 48.5 | 5993.581 6020.795 | 30014 31114 | 00001 | 628 626 | .00357 .0465 |
| 3727.380 | 13311 | 03301 | 626 | 2.09 | 6072.343 | 40014 | 10001 | 626 | .00104 |
| 3783.14 | 20011 30012 | 10002 20003 | 628 626 | 0.0035 .0028 | 6075.983 6088.21 | 30014 31113 | 00001 | 626 636 | . 454 . 00238 |
| 3799 .574 3814 . 248 | 20011 | 10003 | 626 | 0.770 | 6100,30 | 31113 | 01101 | 628 | .00208 |
| 3831.968 | 30011 | 20002 | 626 | .00092 .0251 | 6119.618 6127.782 | 30013 30013 | 00001 | 636 628 | .0290 ,0238 |
| 3858.109 3856.657 | 21111 30003 | 11102 00001 | 626 628 | .016 | 6149.760 | 41114 | 11102 | 626 | .00179 |
| | | | | | 6170.090 | 32213 | 02201 | 626 | .01265 |
| 3987.610 4005.948 | 30002 00021 | 00001 01101 | 628 626 | .0149 .00818 .14 | 6175.118 6175.950 | 40014 30013 | 10002 | 626 627 | .02269 .00320 |
| 4416.150 | 31104 | 00001 | 626 | .00037 .15 | 6179.01 | 41102 | 00001 | 626 | (1.5-06 TT) |
| 4508.749 | 00021 40004 | 00001 01101 | 638 626 | .00186 | 6196.174 6205.503 | 31113 40013 | 01101 10001 | 626 626 | . 268 . 0127 |
| 4529.870 4578.090 | 32203 | 01101 | 626 | .00018 .20 | 6227.924 | 30013 | 00001 | 626 | 4.27 |
| 4591.118 | 31103 | 00001 | 626 | .00205 .18 | 6241.964 | 30012 | 00001 01101 | 636 | .0461 .00409 |
| 4614.779 4639.502 | 01121 | 01101 00001 | 628 628 | .01042 .1302 | 6243.57 6254.592 | 31112 30012 | 00001 | 636 628 | .01414 |
| 4655.205 | 00021 | 00001 | 627 | .0127 | 6265.170 | 31112 | 01101 | 628 | .00119 |
| 4673.680 | 22213 | 02201 10002 | 636 | .00149 .00186 | 6298.110 6308.278 | 30012 40013 | 00001 10002 | 627 626 | .00275 .02455 |
| 4685.780 4687.796 | | 10001 | 636 626 | .00521 | 6318.17 | 41113 | 11102 | 626 | .00179 |
| 4692.180 | 20013 | 00001 | 638 | .00260 | 6346.265 | 40012 | 10001 | 626 | .0119 |
| 4708.52 4733.50 | 21113 23313 | 01101 03301 | 636 626 | .0298 .00670 | 6347.854 6356.293 | 30012 31112 | 00001 01101 | 626 626 | 4.27 0.327 |
| 4743.70 | 21113 | 01101 | 628 | .0335 | 6359.287 | 32212 | 02201 | 626 | .0116 |
| 4748.058 | 20013 | 00001 | 636 | .214 | 6363.616 | 30011 | 00001 | 636 | .0127 |
| 4753.450 4755.705 | 31102 31114 | 00001 | 626 626 | .00298 .10 .0179 | 6388.015 6397.545 | 41101 31111 | 00001 01101 | 626 636 | (4.8-06 T) .00119 |
| 4768.541 | | 02201 | 626 | . 2604 | 6429.172 | 30011 | 00001 | 628 | .00112 |
| 4784.675 | 20023 | 00011 | 626 | .00149 | 6466.440 | 20023 | 01101 | 626 | .00104 |
| 4786.688 | 31113 | 11101 | 626 | .0119 | 6494.67 | 12222 | 01101 | 626 | .00119 |
| 4790.571 | 30014 | m o o 2 | 626 | .1562 | 6503.081 | 30011 | 00001 | 626 | . 498 |

Table 10. Band Origins and Intensities for ${\bf CO_2}$ (Contd)

| Band Center | Upper Level | Lower Level | Iso- tope | SV at 296K (multiply by | |
|---------------------|----------------|----------------|--------------|----------------------------|---------------------------------------------------------------|
| 70 | 56762 | | 0000 | | |
| | | | | 10 ⁻²² mol | |
| (cm ⁻¹) | | | | cm² cm²¹) y | |
| 6536,445 | 31111 | 91191 | 626 | .0476 | |
| 6537.956 | 11122 | 00001 | 626 | .0223 | |
| 6562.444 | 32211 | 02201 | 626 | .00223 | |
| 6679.709 | 11121 | 00001 | 626 | .0263 | |
| 6745.11 | 01131 | | 636 | .01339 | Notes to Table IV-2.2 |
| 6780.21 | | 01101 | 636 | .1637 | |
| 6860.410 | | 00001 | 626 | .00201 | Bands deriving all their intensity from J-dependent |
| 6867.280 | | 03301 | 626 | .00112 | perturbation are designated o pert, when one near |
| 6870.79 | | 11101 | 626 | .00241 | band provides the intensity, TT, when the listed |
| 6885.150 | | 11102 | 628 | .00402 | intensity is multiplied by $m(m+1)$, and Δ , when the |
| 6897.75 | | 01101 | 626 | .0424 | listed intensity is multiplied by m^2 (m+1) ² . |
| 6905.77 | | 02201 | 626 | .0171 | |
| 6907.14 | | 10001 10002 | 626 | .0290 | Q designates bands with intensity below the |
| 6922.21 | | 00001 | 628 | .0521 | criterion limit, whose Q - branches are |
| 6935.15 | | 01101 | 626 | 1.131 | significant. |
| 6945.61 | | 00001 | 627 | 0.0112 | |
| 6972.57 | | 00001 | 626 | 14.95 | • |
| | | 00001 | | | |
| 7283.96 | 40015 | 00001 | 626 | 0.00186 | |
| 7460.53 | 40014 | 00001 | 626 | .0428 | • |
| 7481.51 | 40013 | 00001 | 636 | .00112 | |
| 7583.26 | 5 41113 | 01101 | 626 | .00833 | |
| 7593.69 | 0 40013 | 00001 | 626 | .1064 | |
| 7616.62 | 51102 | 00001 | 626 | (1.12-06 Tr) | |
| 7734.45 | | 00001 | 626 | .0279 | |
| 7757.62 | | 01101 | 626 | .00298 | |
| 7901.47 | | 00001 | 626 | .00149 .018 | |
| 7920.84 | | 00001 | 626 | .00186 | |
| 7981.18 | | 00001 | 636 | .00232 | |
| 8084.06 | | 02201 | 626 | .00193 | |
| 8089.84 | | 00001 | 636 | .00707 | |
| 8103.57 | | 10002 | 626 | .00205 | |
| 8120.10 | | 00001 | 628 | .00201 | |
| 8128.78 | | 10001 | 626 | .00071 | |
| 8135.88 | | 01101 | 626 | .0402 | |
| 8192.55 | | 00001 | 626 | .424 | |
| 8220.36 | | 00001 | 628 | .00201 | |
| 8243.16 | | 10001 | 626 | .00108 | |
| 8254.80 | | 02201 | 626 | .00164 | |
| 8276.76 | | 01101 | 626 | .0461 | |
| 8293.95 | 7 10031 | 00001 | 626 | .614 | |
| 9388.99 | 0 20033 | 00001 | 626 | .00415 | |
| 9478.05 | | 01101 | 626 | .00180 | |
| 9516.97 | | 00001 | 626 | .0233 | |
| 0621 35 | | 00001 | 020 | 0003 | |

of $\zeta^{\mathbf{v}}$ included in Table 9. Note that when $\zeta_{\mathbf{v}}$ is larger than 0.01, the total band strength, if defined as the sum of the Q, R- and P-branch lines, $\mathbf{r}_{\mathbf{m}}^{\mathbf{z}} \mathbf{S}_{\mathbf{m}}^{\mathbf{y}}$, may be much larger than $\mathbf{S}_{\mathbf{v}}^{\mathbf{o}}$, its value when $\zeta_{\mathbf{v}} = 0$. The entry in **Table 10** is $\mathbf{S}_{\mathbf{v}}^{\mathbf{o}}$, not $\mathbf{s}_{\mathbf{m}}^{\mathbf{z}} \mathbf{S}_{\mathbf{m}}^{\mathbf{o}}$.

As a higher-order effect of Coriolis interactions, transitions with $\ell' - \ell'' = +2$ also become allowed, the effect increasing as m^2 , so that a few such bands are intense enough to appear; here we list the value of $S_{\mathbf{v}}^{\mathbf{o}}$ in the formula $S_{\mathbf{m}} = S_{\mathbf{v}}^{\mathbf{o}} (|\mathbf{m}| + \mathbf{m}^2) \exp[(-1.439 \mathbf{E''}) / \mathbf{T}] / \mathbf{Q}_{\mathbf{r}}.$ There are also a few special cases of near-or crossing-perturbations, where

There are also a few special cases of near-or crossing-perturbations, where a normally **very** weak band "borrows" intensity from a stronger neighbor. A notable example is represented by the bands at 4808.186 cm⁻¹, where the 40002-01101 band with zero intensity, resonates with the 21113-01101 band at 4807.692 cm⁻¹. The positions and intensities of the individual lines are here calculated using an appropriate Coriolis constant and dividing the strength of 21113 -01101 according to the degree of perturbational mixing.

4.2.3 CO, LINE HALF-WIDTHS

The half-widths for CO_2 were assigned by a linear function of the rotational quantum number. The work of Yamamoto, Tanaka and Aoki (1969) gave methods of estimating half-widths for the 15 μ m and 4.3 μ m regions, but the differences between their limited comparisons of calculated values and laboratory measurements did not seem to warrant any more complicated procedure in arriving at a half-width dependence upon J for CO_2 .

4.3 Ozone

The band centers and intensities of all bands included in the compilation are given in Table 11.

The pure rotational transitions of ozone have been calculated using the molecular constants of Lichtenstein, Gallagher, and Clough (1971) obtained from microwave measurements. Transitions with upper state J less than 61 and intensities greater than $3.5 \times 10^{-24} \, \mathrm{cm^{-1}/mol - cm^2}$ have been tabulated using a value of $\mu = 0.53D$ for the dipole moment. Lines with K_a less than 10 should be accurate to 0.001 $\mathrm{cm^{-1}}$. Multiplets up to $K_a = 12 \, (\approx 100 \, \mathrm{cm^{-1}})$ have been observed and the calculated contours agree within the experimental accuracy (see Gebbie et al, 1966). At higher values of K_a , the calculations become increasingly less certain. However, even the highest value of K_a included in the listing (that is, $K_a = 20$) is substantially less #an the value of K for which the calculation is divergent. The mean line width has been determined to be 0.11 (Lichtenstein et al, 1971).

| T | | | | |
|---------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------|--------------------------------------------------------------------|-------------------------------------------------------------|
| 3and Center | Σ_{i}^{S} | Vibrational | Transition | Isotope |
| cm ⁻¹ | cm ⁻¹ mol/cm ² | Upper State | Lower State | · |
| 0. 700.930 1007.693 1007.996 1021.096 1027.096 1028.096 1042.096 1103.157 2110.790 2785.241 3041.200 | 4.13 × 10 ⁻¹⁹ 6.70 × 10 ⁻¹⁹ 9.49 × 10 ⁻²¹ 2.49 × 10 ⁻²⁰ 4.23 × 10 ⁻¹⁹ 1.62 × 10 ⁻¹⁹ 5.16 × 10 ⁻²⁰ 1.29 × 10 ⁻¹⁷ 3.47 × 10 ⁻¹⁹ 1.33 × 10 ⁻¹⁸ 2.32 × 10 ⁻²⁰ 1.10 × 10 ⁻¹⁹ | 000 010 101 001 011 002 001 001 100 101 111 003 | 000 000 100 000 010 001 000 000 000 000 | 666 666 686 686 666 668 666 666 666 |

Table 11. Ozone Transitions Included in Data Compilation

For the ν_2 fundamental of ozone, upper-state molecular constants have been obtained from microwave data by Tanaka and Morino (1970a). For a discussion of the determination of the band center see Tanaka and Morino (1970b). Transitions up to J = 60 with intensities greater than $3.5 \times 10^{-23} \, \mathrm{cm}^{-1}/\mathrm{mol-cm}^2$ have been tabulated. The dipole moment constant for the ν_2 fundamental has been taken as $(\partial \mu/\partial q_2) q_2 = 0.048D$ giving a band intensity of 6.76 $10^{-19} \, \mathrm{cm}^{-1}/\mathrm{mol-cm}^2$ based on the measurements of McCaa and Shaw (1968).

The ν_3 and ν_1 regions of the ozone spectrum have been studied by Clough and Kneizys (1965, 19661, and Tanaka and Morino (1968). The positions of the ν_1 and ν_3 transitions for the main isotope are expected to be accurate to 0.01 cm⁻¹ for J less than 40 and $\mathbf{K_a}$ less than eight with a degradation of accuracy for higher values of the quantum numbers. In conformity with the results of McCaa and Shaw (1968), the band intensity of ν_3 has been taken as $130 \times 10^{-19} \, \mathrm{cm}^{-1}/\mathrm{mol-cm}^2$.

Also, more lines have been included than were given in the report of Clough and Kneizys (1965). Goldman, et al (1970) have found that the absorption by large ozone amounts could not be satisfactorily explained without introducing the hot bands and the isotopic bands. Since the energy levels are known for the 101, the 100 and the 010 vibrational levels, transitions for the $\mathbf{101} \leftarrow 100$ and $\mathbf{101} \leftarrow 001$ bands may be calculated directly. The line positions for these bands with J less than 30 and $\mathbf{K_a}$ less than \mathbf{six} are presumed accurate to +0. 03 cm⁻¹. The line positions for the $\mathbf{011} \leftarrow 010$ hot band have been obtained by applying a calculated shift of $\mathbf{-21.0}$ cm⁻¹ to the $\mathbf{v_3}$ transitions of the main isotope. For J less than 30 and $\mathbf{K_a}$ less than six an error of up to 1 cm⁻¹ may be expected. For the $\mathbf{002} \leftarrow 001$

hot band, a calculated shift of -15.0 cm $^{-1}$ has been applied to the \emph{v}_3 transitions of the main isotope. In this case, the rotational levels of the upper- and lower-vibrational states are not accurately described, and these lines must be considered to be useful only for their general contribution to the low-resolution absorption in the region. These **shifts** have been calculated using harmonic frequencies and **an**-harmonic corrections determined from an analysis of the available vibrational data.

For the 668 and 686 isotopes, shifts of -13.1 cm $^{-1}$ and -34.1 cm $^{-1}$ respectively have been determined from force constant calculations using the structural constants given by Tanaka and Morino (1968). These shifts have similarly been applied to the original ν_3 line calculations, neglecting the isotopic effect on the rotational constants. Consequently, only the general contribution to low -resolution spectra by these lines is valid. The intensities of the hot bands and the isotopic bands have been determined by applying the appropriate Boltzmann correction, isotopic abundance factor, dipole moment matrix element value, and degeneracy factor to the intensities of the ν_3 fundamental.

Although the addition of the isotopic bands and the hot bands gives improved agreement between calculated absorption and the observed absorption for large ozone amounts, it appears that an intensity anomaly still exists. In the P branch region (~ 1000 cm-') the calculated intensity is evidently too low, while in the R branch region the calculated intensity is too high. Until better intensity measure - ments are available, it will be difficult to obtain experimental F factors (see Section 3.2).

The $(v_1 + v_3)$ combination band (101 \leftarrow 000) has been observed and analyzed using the **rig:d** rotor approximation by Trajmar and McCaa (1964). The value of the band center was found to be 2110.79 cm⁻¹. The resolution and calibration accuracy of the observed spectra were not good, so that the line positions up to J = 20 and $K_a = 4$ are accurate to only 0.3 cm⁻¹. The error in line position is expected to be significantly greater for higher quantum numbers. The band intensity for the tabulated lines is 1.19 x 10⁻¹⁸ cm⁻¹.

The (ν_1 t ν_2 t ν_3) combination band (111 \sim 000) at 2785.241 has been studied by Snider and Shaw (1971). The rigid rotor analysis used gives line positions for J less than 25 and K_a less than 6 accurate to 0.1 cm⁻¹. The intensity for this band is 2.46 x 10⁻²⁰ cm⁻¹ and was also obtained from McCaa and Shaw (1968).

Constants for the 3 ν_3 band (003 \leftarrow 000) have been obtained from a second order calculation using the results of Tanaka and Morino (1968). The band intensity has been taken as 1.12 x 10⁻¹⁹ cm⁻¹/molecule-cm⁻² from McCaa and Shaw (1968). The accuracy of the line positions should not be in error by more than \pm 5 cm⁻¹

4.4 Nitrous Oxide

Nitrous oxide is an asymmetric linear molecule (N-N-O) with three fundamental vibration-rotation bands, v_1, v_2 , and v_3 , at 1284.907, 588.767, and 2223.756 cm⁻¹, respectively, for the main isotope. As for $CO_2, v_1 \cong 2v_2$ so that Fermi resonance occurs between these two levels, causing shifts of the band centers from the positions otherwise expected. Five different isotopes provide significant absorption. When no reference to a particular isotope is made, the most abundant one, 446, is implied. The abbreviated notations and natural abundances of each isotope used to calculate intensities of the isotopic bands are (446), 99.043 percent; (456), 0.358 percent; (546), 0.358 percent; (448), 0.199 percent; and (447), 0.040 percent. These values differ slightly from those given in Table 4, the difference arising from slight differences in the oxygen and nitrogen natural abundances taken from the 48th edition and the 42nd edition of the Handbook of Physics and Chemistry.* The 48th edition values were used in the construction of Table 4. These abundance differences are very small, but can be accounted for by modifying the line intensities accordingly.

4.4.1 LINE POSITIONS

Table 12 lists the constants used to calculate the line positions. Values of the vibrational energy, G, are relative to the $00^{0}0$ level for each isotope and are probably accurate to a few thousandths of a cm⁻¹ for the 446 isotope. The uncertainty is much greater for some of the levels of the rarer isotopes. The majority of the constants for the 446 isotope and a few for the other isotopes are from Pliva (1964, 1968a, 1968b). Most of the other values have been derived by Benedict (private communications1 from a variety of data.

Line positions for the P- and R-branches can be calculated by inserting the constants from Table 12 into Eq. (6). The selection rules are: AJ = 0, +1; $\Delta l = 0$, +1; and J = 0, +1; $\Delta l = 0$. The allowed values of J for a given vibrational level must be taken into account in order to determine missing lines. For example, in a $\phi \leftarrow \Delta$ band ($l = 3 \leftarrow l = 2$) the following lines are missing because of rotational energy levels that are not allowed: **P1**, P2, P3, QO, **Q1**, **Q2**, RO and **R1**.

A few lines of the $10^{\circ}1,06^{\circ}0,06^{2}0$, and $10^{\circ}1-10^{\circ}0$ bands are shifted from the positions based on the constants in Table 12 because of Fermi interactions. These are discussed in more detail below and summarized in Table 15.

^{*}Published by the Chemical Rubber Co., Cleveland, Ohio

Table 12. Vibrational Energy Levels and Molecular Constants for ${\bf N_2O}$

| | | Energy Levels and IV | | 2 |
|---------------------|--------------------------|--------------------------|-------------------------------------------------------------------|--------------------------------------------------------------|
| Energy Level | G (cm ⁻¹) | B (cm ⁻¹) | D Multiply by 10⁻⁷ (cm ⁻¹) | M & ply by 10⁻¹² (cm ⁻¹) |
| | | Isotope 446 | | |
| | | isotope 110 | | |
| 00 ⁰ 0 | 0 | 0.4190113 | 1.795 | 1.17 |
| 01 ^{1°} 0 | 588.767 | 0.4191777 | 1.785 | 1.17 |
| 01 ^{1d} 0 | 588.767 | 0.419969 5 | 1.785 | 1.17 |
| 02 ⁰ 0 | 1168.134 | 0.4199193 | 2.445 | 1.17 |
| 02 ^{2C} 0 | 1177.750 | 0.4201253 | 1.165 | 1.17 |
| 02 ^{2d} 0 | 1177.750 | 0.4201253 | 1.795 | 1.17 |
| 10 ⁰ 0 | 1284.907 | 0.4172563 | 1.775 | 1.17 |
| 03 ^{1°} 0 | 1749.058 | 0.4196063 | 2.195 | 1.17 |
| 03 ^{1d} 0 | 1749.058 | 0.4210883 | 2.195 | 1.17 |
| 03 ^{3d} 0 | 1766.958 | 0.420674 | 1.805 | 2.20 |
| 03 _{3c} 0 | 1766.958 | 0.420674 | 1.805 | 0.14 |
| 11 ¹⁰ 0 | 1880.268 | 0.4174673 | 1.765 | 1.17 |
| 11 ^{1d} 0 | 1880.268 | 0.4183803 | 1.775 | 1.17 |
| 04 ⁰ 0 | 2322.570 | 0.4206113 | 4.095 | 16.17 |
| 04 ^{2°} 0 | (2331.15) | 0.4210113 | 1.350 | 1.17 |
| 04 ^{2d} 0 | (2331.15) | 0.4210113 | 2.50 | 1.17 |
| 12 ⁰ 0 | 2461.998 | 0.4181483 | 2.465 | 3.77 |
| 12 ^{2c} 0 | 2474.785 | 0.4187143 | 1.210 | 1.17 |
| 1 2 ^{2d} 0 | 2474.785 | 0.4187143 | 1.700 | 1.17 |
| 20 ⁰ 0 | 2563.341 | 0.4224193 | 1.645 | 1.17 |
| 00 ⁰ 1 | 2223.756 | 0.4155613 | 1.795 | 1.17 |
| 05 ^{1°} 0 | 2897.876 | | 2.085 | 1.17 |
| 05 ^{1d} 0 | 2897.876 | | 2.355 | 1.17 |
| 13 ^{1c} 0 | 3046.213 | 0.4177633 | 2.145 | 1.17 |
| 13 ^{1d} 0 | 3046.213 | 0.4193783 | 2.165 | 1.17 |
| 13 ^{3c} 0 | 3067.749 | 0.419109 | 1.805 | 0.47 |
| 13 ^{3d} 0 | : 3067.749 | 0.419109 | 1.805 | 1.87 |
| [] | l l | u . | 1) | B. |

Table 12. Vibrational Energy Levels and Molecular Constants for $\mathbf{N_2O}$ (Contd)

| | | | | 2 , |
|--------------------|-------------|---------------------|--------------------------------------------|----------------------------|
| Energy Level | G | В | D Multiply by 10⁻⁷ | H Multiply by lo-;'" |
| | (cm^{-1}) | (cm ⁻¹) | (cm ⁻¹) | (cm) |
| _ | | | (CIII) | (CIII / |
| | | Isotope 446 (Contd) | | |
| 21 ^{1c} 0 | 3165.857 | 0.4158333 | 1.595 | 1.17 |
| 21 ^{1d} 0 | 3165.857 | 0.4169163 | 1.595 | 1.17 |
| 01 ^{1°} 1 | 2798.290 | 0.4157723 | 1.795 | 1.17 |
| 01 ^{1d} 1 | 2798.290 | 0.4165473 | 1.795 | 1.17 |
| 14 ⁰ 0 | 3620.941 | 0.4187873 | 3.885 | 14.17 |
| 14 ^{2°} 0 | 3631.601 | 0.4190143 | 0.375 | 1.17 |
| 14 ^{2d} 0 | 3631.601 | 0.4190143 | 2.045 | 1.17 |
| 22 ⁰ 0 | 3748.252 | 0.4163273 | 2.395 | 2.77 |
| 22 ^{2°} 0 | 3766.060 | 0.4172013 | 1.200 | 1.17 |
| 22 ^{2d} 0 | 3766.060 | 0.4172013 | 1.560 | 1.17 |
| 30 ⁰ 0 | 3836.373 | 0.4141473 | 1.385 | 1.17 |
| 02 ⁰ 1 | 3363.974 | 0.4165443 | 2.445 | 1.17 |
| 02 ^{2°} 1 | 3373.137 | 0.4167523 | 1.195 | 1.17 |
| 02 ^{2d} 1 | 3373.137 | 0.4167523 | 1.795 | 1.17 |
| 10 ⁰ 1 | 3480.821 | 0.4137843 | 1.745 | 1.17 |
| 23 ^{1°} 0 | 4335.798 | 0.4159193 | 2.045 | 1.17 |
| 23 ^{1d} 0 | 4335.798 | 0.4176813 | 2.115 | 1.17 |
| 31 ¹⁰ 0 | 4446.379 | 0.4143703 | 1.625 | 1.17 |
| 31 ^{1d} 0 | 4446.379 | 0.4156713 | 1.365 | 1.17 |
| 03 ^{1°} 1 | 3931.258 | 0.4162253 | 1.915 | 1.17 |
| 03 ^{1d} 1 | 3931.258 | 0.4176843 | 1.925 | 1.17 |
| 03 ^{3c} 1 | 3948.344 | 0.417327 | 1.815 | 0.14 |
| 03 ^{3d} 1 | 3948.344 | 0.417327 | 1.815 | 2.20 |
| 11 ^{1c} 1 | 4061.979 | 0.4140513 | 1.775 | 1.17 |
| 11 ^{1d} 1 | 4061.979 | 0.4149343 | 1.735 | 1.17 |
| 40 ⁰ 0 | 5105.65 | 0.4131913 | 1.795 | 1.17 |
| 32 ⁰ 0 | 5026.34 | 0.4143113 | 1.795 | 1.17 |
| 20 ⁰ 1 | 4730.828 | 0.4121163 | 1.625 | 1.17 |
| 1201 | 4630.164 | 0.4147633 | 2.475 | 4.17 |
| 12 ^{2c} 1 | 4642.463 | 0.4151583 | 1.315 | 1.17 |
| 12 ^{2d} 1 | 4642.463 | 0.4151583 | 1.315 | 1.17 |
| 002 | 4417.379 | 0.4120963 | 1.765 | 1.17 |

Table 12. Vibrational Energy Levels and Molecular Constants for $\mathbf{N_2O}\left(\mathbf{Contd}\right)$

| Energy | G | В | D | Н , |
|------------------------------------------|----------------------|------------------------|---------------------------|-----------------------------|
| Level | | | Multip ly by 10 | Multiply by 10 12 |
| | (cm ⁻¹) | (cm ⁻¹) | (cm ⁻¹) | (cm ⁻¹) |
| | | Isotope 446 (Contd) | i | |
| 21 ^{1c} 1 | 5319.175 | 0.4124313 | 1.675 | 1.17 |
| 21 ^{1d} 1 | 5319.175 | 0.4134703 | 1.555 | 1.17 |
| 01 ^{1c} 2 01 ^{1d} 2 | 4977.695 4977.695 | 0.4123583 0.4131183 | 1.785 1.785 | 1.17 1.17 |
| 01 2 | 4377.033 | Isotope 456 | 1.700 | 1.17 |
| 00 ⁰ 0 | 0 | 0.4189821 | 1 75 | - |
| | | | 1.75 | |
| 01 ¹⁰ 0 01 ^{1d} 0 | 575.5 575.5 | 0.419095 0.419891 | 1.75 1.75 | |
| 10 ⁰ 0 | 1280.5 | 0.41719 | 1.72 | |
| 11 ¹⁰ 0 | 1861.9 | 0.41734 | 1.71 | |
| 11 ^{1d} 0 | 1861.9 | 0.41820 | 1.70 | |
| 20 ⁰ 0 | 2554.3 | 0.41545 | 1.67 | |
| 00 ⁰ 1 | 2177.659 | 0.41568 | 1.75 | |
| 01 ^{1C} 1 01 ^{1d} 1 | 2739.63 2739.63 | 0.415855 0.416605 | 1.75 1.75 | |
| 10 ⁰ 1 | 3430.95 | 0.41387 | 1.72 | |
| | | Isotope 546 | | <u> </u> |
| 00°0 | 0 | 0.4048564 | 1.64 | |
| 01 ^{1°} 0 | 585.320 | 0.4050304 | 1.65 | |
| 01 ^{1d} 0 | 585.320 | 0.4057724 | 1.65 | |
| 10 ⁰ 0 | 1269.894 | 0.403269 | 1.60 | |
| 11 ^{1c} 0 | 1863.080 | 0.4034614 | 1.59 | |
| 11 ^{1d} 0 | 1863.080 | 0.4043814 | 1.57 | |
| 20 ⁰ 0 | 2534.21 | 0.401870 | 1.45 | |
| 00 ⁰ 1 | 2201.604 | 0.401495 | 1.65 | |
| 01 ^{1c} 1 01 ^{1d} 1 | 2745.709 2745.709 | 0.4017054 0.4024104 | 1.65 1.65 | |
| 10 ⁰ 1 | 3443.659 | 0.399876 | 1.60 | |
| 10 1 | 3443.039 | 0.399870 | 1.00 | 1 |

Table 12. Vibrational Energy Levels and Molecular Constants for N2O (Contd)

| Energy Level | G | В | D Multiply by 10⁻⁷ | H Multiply by 10⁻¹² | | |
|------------------------------------------|-------------------------|-----------------------|--------------------------------------------|---------------------------------------------|--|--|
| | (cm ⁻¹) | (cm ⁻¹) | (cm ⁻¹) | (cm -1) | | |
| | <u>Isotope 448</u> | | | | | |
| 00 ⁰ 0 | 0 | 0.395577 | 1.65 | | | |
| 01 ^{1c} 0 01 ^{1d} 0 | 584.1 584.1 | 0.39 5749 0.396461 | 1.65 1.65 | | | |
| 10 ⁰ 0 | 1247.9 | 0.394057 | 1.55 | | | |
| 11 ^{1c} 0 11 ^{1d} 0 | 1839.8 1839.8 | 0.39430 0.39513 | 1.56 1.50 | | | |
| 20 ⁰ 0 00 ⁰ 1 | 2491.3 2218.97 | 0.39279 0.392317 | 1.31 1.65 | | | |
| 01 ^{1c} 1 01 ^{1d} 1 | 2786.80 2788.80 | 0.392549 0.393209 | | | | |
| 10 ⁰ 1 | 3439.1 | 0.39078 | 1.55 | | | |
| | | Isotope 447 | | | | |
| 00°0 | 0 | 0.406691 | 1.72 | | | |
| 01 ^{1c} 0 01 ^{1d} 0 | 586.3 586.3 | 0.406860 0.407610 | 1.72 1.72 | | | |
| 10 ⁰ 0 | 1265.5 | 0.405961 | 1.67 | | | |
| 00 ⁰ 1 | 2221.3 | 0.40334 | | | | |
| 01 ^{1C} 1 01 ^{1d} 1 | 2793.55 2793.55 | 0.403 57 0.40430 | | | | |

4.4.2 LINE INTENSITIES

Each band system contains a main band and associated hot bands that arise from transitions from excited energy levels with the same changes Δv_1 , Δv_2 , and Δv_3 in the vibrational quantum numbers as in the main band. The change Δl may be either 0 or \pm 1 within the same band system. For example, the 0° 01 band is the main band in a system that also contains the hot bands $01^{1}1 - 01^{1}0$, $02^{\circ}1 - 02^{\circ}0$, $02^{2}1 - 02^{2}0$, $10^{\circ}1 - 10^{\circ}0$, and many others from higher excited energy levels. The relative intensities of the hot bands decrease with increasing value of the lower energy level because of the decrease in its population. Thus, only a few of the hot bands are usually significant. Corresponding bands of the rare isotopic molecules are also part of the system. The main band of the common isotope accounts for 78 percent to 89 percent of the entire system for $296^{\circ}K$ samples, depending on the band system.

Table 13 summarizes the normal band systems containing lines with intensities greater than 4×10^{-23} molecules $^{-1}$ cm 2 cm $^{-1}$. Each band system is identified by the main band whose center position is given. The intensities are based on recent measurements of the quantity f(-1/u) / n T d ν by Burch et al, (1971a,1971b,1971c, 1972). The integration was performed over the entire band system, and u is the N_2O thickness in molecules cm $^{-2}$. The intensity, S_Q , of only the Q-branch of the band at 1974.571 cm $^{-1}$ is listed because the P and R branches contain no lines with intensities above the cut-off. The Q-branch may be significant although each of its lines is very weak because they occur very close together. Bands containing the 06^O 0 and 06^O 0 levels are not listed because the band systems are very weak. However, as a result of Fermi interaction between a few of the rotational levels, the intensities of the corresponding lines are anomalously high and their positions arc shifted. These lines are discussed in more detail below.

Table 14 lists the intensities of each of the bands with lines above the cutoff intensity, nominally 4×10^{-23} molecules $^{-1}$ cm 2 cm $^{-1}$. Each line entry in the table corresponds to a given band, and blank lines occur before and after each **band** system. Note that 16 bands are listed for the $\mathbf{00^{0}1}$ band system, whereas only 1 or 2 bands are listed for some of the weaker systems.

Each rotationallevel within a vibrationallevelfor which quantum number $\ell \neq 0$ is split into two sublevels normally indicated by "c" and "d" (see section 3. 1. 1). A band involving two A levels, or two π levels, or one of each level consists of two sub-bands, one from the c portion of the lower level and one from the d portion. The $c \leftarrow c$ portion of the first sub-band contains only P- and R-branches, whereas the $d \cdot c$ portion contains the Q-branch. Similarly, the $d \leftarrow d$ and the $c \leftarrow d$ portions of the second sub-band contain the P t R branches and the Q-branch, respectively. The **intensities**, $S_{n,r}$ given in Table 14 are the total for both sub-bands.

Table 13. Summary of N₂O Band Systems

| - | | | |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Center of Main Band (cm ⁻¹) | Upper Level | Lower Level | Intensity of System Multiply by 10 ⁻²⁰ Molecules ⁻¹ cm ² cm ⁻¹ |
| (em) | | | Molecules Cit Citi |
| 588.767 | 0110 | 00 ⁰ 0 | 118 <u>+</u> 9 |
| 696.140 938.849 1168.134 1284.907 | 10 ⁰ 0 00 ⁰ 1 02 ⁰ 0 10 ⁰ 0 | 01 ¹ 0 10 ⁰ 0 00 ⁰ 0 00 ⁰ 0 | 0.354 t 0.020 0.254 7 0.010 38.5 t-i.5 996 + 40 |
| 1634.989 1749.058 1880.268 1974.571 2223.756 | 03 ¹ 000 ⁰ 1 1110 20 ⁰ 0 00 ⁰ 1 | 01 ¹ 0 00 ⁰ 0 00 ⁰ 0 0110 00 ⁰ 0 | 0.278 ± 0.02 0.241 ∓ 0.02 1.66 ± 0.08 $S_{Q} = 0.024 \pm 0.002$ 5710 ± 250 |
| 2322.624 2461.998 2563.341 2798.290 3363.974 3480.821 3620.941 3748.252 3836.373 4061.979 4335.798 4417.379 4630.164 4730.828 4977.69 5 5026.34 5105.65 | 04°0 12°0 20°0 01°1 02°1 10°1 14°0 22°0 30°0 30°0 12°1 20°1 20°1 20°1 20°1 20°1 20°1 2 | 0000 00°0 00°0 00°0 00°0 00°0 00°0 00° | 2.7 t 0.3 33.4 + 1.5 135 t-7 9.62-t 0.96 10.6 \neq 0.5 197 t-10 0.56-t 0.02, -0.05 4.12 t 0.2 8.15 \neq 0.4 0.111 t 0.006 0.1 t 6.1, -0.07 6.9 t 0.7 0.68 + 0.07 4.4 t-b.4 0.071) t 0.008 0.29 t-b.04 0.29 \neq 0.03 |

Table 14. N20 Band Intensities

| - 0 1 0 1 | ** | T | T . | C |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------|
| E 3and Center | Upper Level | Lower Level | Isotope | S _v at 296K |
| ν _e | Levei | Level | | (Multiply by 10⁻²⁰ |
| (cm ⁻¹) | | | | Molecules -1 cm ² cm ⁻¹ |
| 588.767 579.367 588.983 580.924 57 1.308 589.208 595.361 585.320 575.5 586.3 | 01 ¹ 0 02 ⁰ 0 02 ² 0 03 ¹ 0 03 ¹ 0 03 ³ 0 11 ¹ 0 0110 0110 0110 | 00°0 0110 0110 0220 0220 10°0 00°0 00°0 | 446 446 446 446 446 446 446 546 456 447 448 | 98.4 4.90 11.26 0.599 0.256 0.958 0.216 0.356 0.356 0.039 0.197 |
| 696.140 | 10 ⁰ 0 | 01 ¹ 0 | 446 | 0.294 |
| 938.849 | 00 ⁰ 1 | 10 ⁰ 0 | 446 | 0.223 |
| 1168.134 1160.291 1154.436 1153.40 | 02 ⁰ 0 0310 04 ⁰ 0 04 ² 0 | 0000 0110 0200 0220 | 446 446 446 446 | 31.7 5.72 0.201 0.228 |
| 1177.750 | 0220 | 0000 | 446 | See Note A |
| 1284.907 1291.501 1293.864 1297.035 1278.434 1297.155 1300.791 1285.589 1280.5 1286.4 1269.894 1277.760 1247.9 1255.7 | 10°0 1110 12°0 1220 20°0 13°0 1330 2110 10°0 11°0 11°0 11°0 | 00°0 0110 02°0 0220 10°0 03°3 03°3 1110 00°0 010 010 010 010 010 00°0 | 446 446 446 446 446 446 446 456 456 546 54 | 872. 100.6 3.16 5.92 3.73 0.390 0.364 0.412 3.15 0.354 3.15 0.362 1.75 0.200 0.350 |
| 1634.969 | 00 ⁰ 1 | 01 ¹ 0 | 446 | 0.231 |
| 1749.058 | 0310 | 0000 | 446 | 0.200 |
| 1880.268 1886.018 1873.231 | 11 ¹ 0 1220 12 ⁰ 1 | 00⁰0 0110 0110 | 446 446 446 | 1.41 0.156 0.053 |
| 1974.571 | 20 ⁰ 0 | 0110 | 446 | S_Q = 0.024 |
| 2181.66 | 06 ⁰ 0 | 1000 | 446 | See Note B |

Table 14. N_2O Band Intensities (Contd)

| | _ | | 7 | |
|---------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------|--------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------|
| Band Center | Upper | Lower | Isotope | S _v at 296K |
| $\nu_{ m c}$ | Level | Level | | (Multiply by 10 ⁻²⁰ |
| (cm ⁻¹) | | | | Molecules -1 cm ² cm -1) |
| 2223.756 2209.523 2195.840 2195.387 2195.914 2182.200 2181.386 2181.711 2193.623 2177.659 2164.13 2201.604 2187.389 | 0001 0111 0201 0221 1001 0311 0331 1111 0002 0011 0111 | 00°0 0110 02°0 0220 10°0 0310 0330 11°0 00°1 00°1 00°0 01°0 | 446 446 446 446 446 446 446 446 456 456 | 5023. 568. 16.8 31.8 10.1 1.958 1.88 1.10 0.201 18.1 2.04 18.1 2.10 |
| 2218.97 2204.70 2221.3 2207.25 | 0001 0111 0001 0111 | 00°0 0110 00°0 01°0 | 448 448 447 447 | 10.1 1.15 2.01 0.234 |
| 2322.624 2309.109 | 04 ⁰ 0 05 ¹ 0 | 00°0 01 ¹ 0 | 446 446 | 2.11 0.54 |
| 2461.998 2457.446 2452.807 2453.851 2463.345 | 12°0 13°10 14°0 1420 22°0 | 00.0 0110 02.0 0220 10.0 | 446 446 446 446 446 | 27.6 4.68 0.239 0.321 0.192 |
| 2563.341 2577.090 2580.118 2588.310 2551.466 2534.21 2554.3 2491.3 | 20°0 21 ¹ 0 22°0 2220 30°0 20°0 20°0 | 00°0 0110 02°0 0220 10°0 00°0 00°0 | 446 446 446 446 446 546 456 446 | 120. 12.2 0.348 0.648 0.696 0.454 0.384 0.192 |
| 2474.785 | 1220 | 00°0 | 446 | See Note A |
| 2798.290 2775.207 2784.370 2763.124 2753.508 2770.594 | 01 ¹ 1 02 ⁰ 1 02 ¹ 1 0311 0311 0331 | 00°0 01¹0 01¹0 02°0 0220 02°0 | 446 446 446 446 446 446 | 8.06 0.401 0.912 0.025 0.020 0.078 |
| 3363.974 3342.491 | 02 ⁰ 1 03 ¹ 1 | 00⁰0 0110 | 446 446 | 8.82 1.57 |

Table 14. N_2O Band Intensities (Contd)

| 4. | | | | |
|----------------------|------------------------------------------|--------------------------------|------------|------------------------------------------------------------|
| 3and Center | Upper | Lower | Isotope | S_v at 296K |
| ν _c | Level | Level | | (Multiply by 10 ⁻²⁰ |
| -1, | | | | Molecules ⁻¹ cm ² cm ⁻¹) |
| (cm ⁻) | | | | Molecules em em / |
| 3480.821 | 10 ⁰ 1 | 00 ⁰ 0 | 446 | 173. |
| 3473.212 | 1111 | 0110 | 446 | 19.24 |
| 3462.030 3464.713 | 12 ⁰ 1 | 02⁰0 0220 | 446 446 | 0.563 1.064 |
| 3445.921 | 1221 2001 1001 | 10°0 | 446 | 0.652 |
| 3443.659 | 1001 | 0000 | 546 | 0.627 |
| 3430.95 | 10°1 10°1 | 0000 00°0 00°0 | 456 | 0.627 0.348 |
| 3439.1 | | | 448 | 0.348 |
| 3466.54 | 06 <mark>2</mark> 0 0620 | 00 ⁰ 0 | 446 | See Note B |
| 3474.65 | 0640 | 00 <mark>o</mark> 0 | 446 | See Note A and B |
| 3748.252 | 22 <mark>0</mark> 0 23 ¹ 0 | 0000 | 446 | 3.52 |
| 3747.031 | 2310 | 0110 | 446 | 0.512 |
| 3620.941 | 14 ⁰ 0 | 00 ⁰ 0 | 446 | 0.492 |
| | 30 ⁰ 0 | | | 7.00 |
| 3836.373 3857.612 | 30°0 3110 | 00⁰0 0110 | 446 446 | 7.28 0.698 |
| | | 0 0 | | |
| 4061.979 | 1111 | 00 ⁰ 0 | 446 | 0.092 |
| 4335.798 | 23 ¹ 0 | 00°0 | 446 | 0.083 |
| 4417.379 | 00 <mark>°</mark> 2 | 00°0 | 446 | 6.07 |
| 4388.928 | 0112 | 0110 | 446 | 0.686 |
| 4630.164 | 12 ⁰ 1 | 0000 | 446 | 0.597 |
| 4730.828 | 20 ⁰ 1 | oo ^o o | 446 | 3.90 |
| 4730.408 | 2111 | 0110 | 446 | 0.410 |
| 4977.695 | 0112 | 0000 | 446 | 0.058 |
| 5026.34 | 3200 | 0000 | 446 | 0.255 |
| 5105.65 | 40°0 | 0000 | 446 | 0.255 |
| | | | | |

The intensities of the majority of the bands have been calculated from the experimental values for the entire band systems listed in Table 13. Calculating the intensity of an individual band from that of the entire band system involves the population of each energy level, the degeneracy of each level, and the relative transition probabilities.

In some of the band systems, the experimental results indicate that the transition probabilities are the same for all bands within a given system. However, as in the 12^0 0 band system, for example,, the transition probabilities are greater for the $13^10 - 01^10$ and $14^00 - 02^00$ 0 bands than for the 12^00 0 band. These differences in transition probabilities were found experimentally by comparing the relative intensities of several isolated lines within the system.

Equations relating the intensities of individual lines to that of the entire band are given in Section 3. These are applicable to the N_2O bands listed in Table 14 with the exception of two forbidden $A \leftarrow \Sigma$ bands, 02^2O and 12^2O , and those listed in Table 15. The factor ((see Section 3 Eq. (13)) that accounts for the Coriolis vibration-rotation interaction can be assumed to be **zero** for all bands in Table 14, except for the 03^1O and 11^1O bands; ζ equals approximately -0.01 and -0.007, respectively, for these bands.

Young (1972) has tabulated the relative intensities of the lines within a given band for which the Coriolis interaction is negligible. A large fraction of the intensity of a band system is in the main band; therefore, uncertainties in the relative transition probabilities within a band system do not seriously increase the uncertainty of the main-band intensity calculated on the basis of that of the entire band system. Thus, the percent of uncertainty in the intensity of the main band is approximately the same as that for the entire band system, whereas the uncertainty for the hot bands may be greater.

4.4.3 FORBIDDEN BANDS AND PERTURBED LINES

As a result of Coriolis interactions, transitions with $\ell' - \ell'' = \pm 2$ become allowed. Two $^{N}_{2}O$ bands of interest that arise from such "forbidden" transitions are the $02^{2}O - 00^{0}O$ and $12^{2}O - 00^{0}O$ bands centered at 1177.750 and 2474.785 cm⁻¹, respectively. The relationship between the intensities of the individual lines within a band is different for these bands than'for normal bands. As in the case of $^{CO}_{2}$, the intensities are given by Eq. (15) where $^{S}_{v}O = 1.36 \times 10^{-5}$ molecules $^{-1}$ cm 2 cm $^{-1}$ for the $^{O}_{2}O$ 0 band and $^{S}_{v}O = 9.5 \times 10^{-6}$ molecules $^{-1}$ cm 2 cm $^{-1}$ for the $^{O}_{2}O$ 0 band

A few rotational levels of the $06^{\circ}0$ vibrational state (centered at J = 46) and the $06^{\circ}0$ state (centered at J = 28) are perturbed by the corresponding levels of the $10^{\circ}1$ state to such an extent that the normally very weak lines "borrow" enough

| Line | Hand | | $\mathbf{s_{j}}$ |
|------|----------------------------------------------------|---------------------------------------|-----------------------------------------------------------------------------------|
| | | ν _ο (cm ⁻¹) | x10⁻²⁰ molecules ⁻¹ cm ² cm ⁻¹ |
| R45 | 10 ⁰ 1 | 1)3508.030 | 0.207 |
| R45 | 06 ⁰ 0 | 2)3508.186 | 0.046 |
| P47 | $\begin{smallmatrix}10\\0\\06\\0\end{smallmatrix}$ | 113430.230 | 0.136 |
| P47 | | 2)3430.400 | 0.031 |
| R27 | 1 0 0 1 | 1)3500.040 | 2.11 |
| R27 | 06²0 | 2)3499.970 | 0.0233 |
| P29 | 1001 | 113452.330 | 1.71 |
| P29 | 06²0 | 2)3452.260 | 0.0188 |
| R45 | 1001-1000 | 3)2226.713 | 0.0118 |
| P47 | 10⁰1 ← 1000 | 312149.246 | 0.0042 |

Table 15. Parameters of Perturbed Lines of N20

- 1) The perturbed line positions of the **10^o1** band are from observed values by Tidwell et al, (1960).
- 2) The calculated positions of perturbed lines of the $06^{\circ}0$ and $06^{\circ}0$ bands were determined from known perturbed positions of the $10^{\circ}1$ lines and Toth's (1971a) values of the line separations.
- 3) The calculated positions of the perturbed $10^{01} \leftarrow 10^{00}$ lines were determined from Toth's (1971a) results and the positions of the unperturbed lines calculated on the basis of the constants in Table 12.
- 4) The perturbed line intensities of the $06^{\circ}0$ and $06^{\circ}0$ bands are based on the intensities of the unperturbed lines of the $10^{\circ}1$ band and Toth's (1971a) results. The unperturbed line intensities of the $10^{\circ}1$ and $10^{\circ}1 \leftarrow 10^{\circ}0$ bands are based on the band intensities given. in Table 13 and Young's (1972) relative line intensities.

intensity from the $10^{\circ}1$ lines to appear, at the same time shifting the positions of the lines related to these rotational levels (**Toth,1971a**). The resulting positions and intensities of the affected lines have been calculated separately and are given in Table 15. The R27 and R29 lines of the $10^{\circ}1 - 10^{\circ}0$ band are not listed in *the* table because the changes in their intensities and positions are negligible.

4.4.4 LINE HALF-WIDTHS

Several workers have measured the half-widths of N_2O lines broadened by N_2 , which is a good approximation to broadening by air. Toth (1971b) has recently measured the widths of lines in the R branches of the 10^O1 and 02^O1 bands directly from observed spectra with a small correction for **the** effect of **the** spectrometer slitwidth. Margolis (1972) has used the same method to measure the lines in both the P- and R-branches of the 00^O2 band. The results of these two workers are in

good agreement, indicating that there is little, if any, dependence on vibrational mode. Lowder's (1972) recent measurements on the $00^{\circ}1$ band show approximately the same dependence on J as do the results of Toth and Margolis. although Lowder's values averaged approximately 10 percent less. Oppenheim and Goldman (1971) have measured half-widths indirectly by applying band models to low-resolution spectra of a wide variety of N_2O samples. Their results are in fair agreement with those of Margolis and Toth. Fraley et al, (1962) reported an average value of 0.05 cm⁻¹ at m⁻¹ for lines in the $00^{\circ}1$ band; this value is considerably lower than those reported by the workers mentioned above.

We have adopted half-widths of N_2 -broadened lines reported by Toth (1971b) to be used for atmospheric N_2O lines near 296^OK . A few values are listed in the tabulation below; values for other J's can be found by interpolation and for other temperatures by assuming the 'half-widths are inversely proportional to the square root of temperature.

J cm⁻¹ atm⁻¹

1 0.0915
4 0.0948
10 0.0892
20 0.0812
30 0.0767
40 0.0748
50 0.0698
60 0.0604

4.5 Carbon Monoxide

For the CO bands, we have depended heavily on the work of Young (1968). Table 16 provides the rotational constants which were used to compute the line positions of the main isotope. The positions of the less abundant isotopes were computed from the appropriate constants for the 26 isotope by applying **the** ratio **of** reduced masses. The accuracy of the line positions in the main isotope is expected to be about $+0.001 \, \text{cm}^{-1}$. **Theaccuracy** of the line positions of the **other** isotopes will be somewhat less, about $+0.01 \, \text{cm}^{-1}$.

The intensities for the fundamental and first two overtone bands were taken from Young and are reproduced in Table 17. The intensities for the isotopic bands were taken to be the same as for the 26 isotope reduced by the relative abundances given in Table 4 and the square of the frequency. The intensity of the fundamental appears to be known very accurately, perhaps within t 2 percent; the first overtone is less accurately known to \pm 10 percent; and the second overtone is known to \pm 4 percent (see Young and Eachus, 1966); Burch and Gryvnak (1967). Half-width values have been added to the compilation following the work of Hunt et'al, (1968).

| Symbol | Value |
|----------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------|
| ω _e ω _e X _e ω _e Y _e Β _e α _e γ _e D _c | 2169.836 13.295 0.0115 1.931285 0.017535 1.01x10-5 6.12x10 ⁻⁶ 1.0x10-9 |

Table 16. Rotational Constants Used in the Calculation of CO Line Positions

Table 17. Intensities of CO Bands

| | 1-o | 2-0 | 3-0 |
|------------------------------------------------------------|------------------------|------------------------|------------------------|
| Intensity, S(cm ⁻¹ /molecule-cm ⁻²) | 9.70x10 ⁻¹⁸ | 6.99x10 ⁻²⁰ | 4.83x10 ⁻²² |

4.6 Methane

This molecule is a spherical top, in the rigid rotor approximation. It has tetrahedral (T_d) symmetry in the rest configuration of its nuclei. Rotation-vibration interactions are complicated even for its simplest infrared-active bands. Starting from the molecular Hamiltonian and the electric dipole-moment operator, transition energies, selection rules, and intensities may be calculated. However, the techniques and the results are complex, and it is not convenient to summarize them here. Therefore, the user is referred to the original papers on this subject John (1968), Schaffer et al, (1939), Hecht (1960), Moret-Bailly (1961), Herranz (1961), Fox (1962), Dang-Nhu (1969), and Susskind (1972).

For the purpose of the present data compilation, we have established the following conventions in notation. The isotopic species $^{12}\text{CH}_4$, $^{13}\text{CH}_4$, and $^{12}\text{CH}_3\text{D}$ are denoted by the digits 211, 311, and 212, respectively, in columns 75 through 77. The quantum numbers for the initial and final states of a transition are specified in columns 36 through 69 as **follows**:

$$v'_1v'_2\ell'_2v'_3\ell'_3v'_4\ell'_4\ell'$$
 $v''_1v''_2\ell'_2v''_3\ell''_3v''_4\ell''_4\ell''$ J'R' C' N' J''R'' C'' N''

1X 811 1X 811 1X 212 1A1 111 111 1X 212 1A1 111 111

except for type E symmetry which has for C the format 1X **1A1** instead of **1A1** 111. The initial and final state vibrational and rotational quantum numbers have their usual meanings. To avoid ambiguity, we establish some further conventions for the present data compilation. The selection rule C' - C'' on T_d symmetry is always **taken** to be $A_1 - A_2$, $A_2 - A_1$, E - E, $F_1 - F_2$, or $F_2 - F_1$. The numbering scheme for the N's

begins with 1, 2, 3 . . . Whenever possible, N increases with increasing groundstate energy; the stronger lines correspond to the **selection** rule, N' - N'' = 0.

This section describes methane spectral data in the 3 to 8.5 μ m region. The following bands, as summarized in Table 18, have been included: v 2, v 3, v 4, v 2+ $v_4, 2v_4.$

Table 18. Methane Bands Included in Data Compilation

| Isotope | Band | Center (cm ⁻¹) | Upper State | Lower State | Intensity (cm ⁻¹ /mole-cm ⁻²) |
|---------|---------------------------------|-------------------------------|-----------------------|----------------|------------------------------------------------------|
| 311 | ν_4 | 1297.88 ^a | 00000111 | 00000000 | 6.59x10 -20h |
| 211 | "4 | 1305.9138 ^b | 00000111 | 00000000 | 5.87x10 ⁻¹⁸ⁱ |
| 211 | '2 | 1533.289' | 01100001 | 00000000 | 8.91x10 ⁻²⁰ⁱ |
| 311 | $\tilde{\nu_3}$ | 3009.53 ^d | 00011001 | 00000000 | 1.36x10 ^{-19h} |
| 211 | " 3 | 3018.9205 ^e | 00011001 | 00000000 | 1.21x10 ⁻¹⁷ⁱ |
| 211 | 2 v 4 | 2600 ^f | 00000222 | 00000000 | 1x10 ⁻¹⁹ j |
| 211 | ν ₂ + ν ₄ | 2818, 2838^g | 01100112 | 00000000 | 8x10 ^{-19h} |

- a. Kyle et **al.** (1970)
- b. Michelot and Fox (1973)
- c. Dang-Nhu (1968)d. McDowell (1966)
- e. **Bobin** and Fox (1973)
- Fox (1973)
- Benedict (1973)
- h. 1/89 times value for corresponding band of 211 isotope
 i. Armstrong and Walsh (1960)
 j. 1/100 times value for ν 3 of 211 isotope
 k.1/15 times value for ν 3 of 211 isotope

It is planned to add other weak but significant bands in this spectral region at a later time.

Many line positions, together with their absolute intensities and widths, have been included in the present data compilation, even though the corresponding quantum number assignments are uncertain or unknown at this time. It must be stressed that much of the needed theoretical and experimental research on spectra of methane is still incomplete. Consequently, a large portion of the data compilation should be considered tentative and subject to revision at a later time.

4.6.1 **LINE POSITIONS**

The band ν_3 at 3.3 μ m is the strongest infrared-active vibration-rotation fundamental of CH_4 . High-resolution measurements of line positions for $^{12}CH_4$ in the range 2884 to 3141 cm $^{-1}$ have been used. See Henryet al, (1970), and Barnes et al, (1972). Quantum number assignments for the allowed lines from 2840 to 3167 $^{\circ}$ were made by **Bobin** and Fox (1973) on the basis of fourth-order perturbation theory. Some forbidden lines were assigned by Barnes et al, (1972) using third order theory. Spectroscopic parameters determined for the ground-state and for ν_3 of CH_4 are listed in Tables 19 and 20, respectively. The corresponding band of the isotopic species $^{13}CH_4$ has been measured from 2873 to 3123 cm $^{-1}$. The assignments of McDowell (1966) with some modifications were used. The corresponding spectroscopic parameters are listed in Table 23.

Table 19. Spectroscopic Parameters for Ground State of $^{12}\mathrm{CH_4}$

| Parameter | Value (cm ⁻¹) |
|----------------|---------------------------------|
| B | 5.24059±0.00006 ^a |
| D _s | (1.086±0.003)×10 ^{-4a} |
| D _t | (4.403±0.099)×10 ^{-6b} |

- a. Barnes et al, (1972)
- b. **Ozier** et al, (1970). The error bar is derived from the values given by Barnes et al, (1972) and Husson and Dang **Nhu** (1971).

The band at 7.7 μ m is the next strongest fundamental of 12 CH₄. High resolution measurements in the 1225 to 1393 cm⁻¹ range made by Botineau (1972) were used to obtain spectral line positions. Quantum-number assignments for the allowed lines, to J=12 for the R and Q branches, and J=13 for the P branch, were made by Michelot and Fox, (1973) on the basis of a fourth order calculation.

For J=13 to 15 in the Q branch only, and for some J=13 R-branch lines, quantum-number assignments were taken from the work of Husson and Poussigue (1971). No forbidden lines of this band have been included in the data compilation yet. The determined spectroscopic parameters are given in Table 21. For ν_4 of 13 CH₄, the measurements of Kyle et al, (1970), extend from 1226 to 1359 cm⁻¹, and possibly further. The assignments of Kyle et al, (1970) with some modifications were used; spectroscopic parameters appear in Table 24.

| Parameter | Value (cm-') | Parameter | Value (cm") |
|------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------|
| m n p q s t X V | 3018.9205 9.87157 -4.0622x10 ⁻² -2.959x10-4 4.329x10-5 1.942x10-7 -9.11x10 ⁻⁸ -4.7921x10-2 3.622x10 ⁻⁵ | g h k L j U z 2' z'' | 4.265x10 ⁻³ 8.365x10 ⁻⁵ -1.925x10-5 2.509x10-7 5.84x10 ⁻⁸ 2.605x10 ⁻⁵ -5.39x10-8 1.49x10-6 7.08x10 ⁻⁸ |

Table 20. Spectroscopic Parameters* for ν_3 of $^{12}CH_4$

***Bobin** and Fox (1973)

Table 21. Spectroscopic Parameters* for ν_4 of $^{12}{
m CH}_4$

| Parameter | Value (cm ⁻¹) | Parameter | Value (cm-') |
|---------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| m n P q s t X V | 1305.9138 5.57 52 -6.4192x10 ⁻² 1.91x10-3 1.479x10-6 -1.11x10 ⁻⁶ -1.79x10-8 -5.2263x10 ⁻² 2.319x10-5 | g h k L j u z z' | 1.8643x10 ⁻² 6.590x10 ⁻⁴ 2.88x10 ⁻⁶ 1.67x10 ⁻⁷ -3.78x10 ⁻⁹ 2.077x10 ⁻⁵ -1.18x10 ⁻⁸ -1.901x10 ⁻⁶ 8.28x10 ⁻⁸ |

*Michelot and Fox (1973)

The ν_2 fundamental at 6.5 μm is relatively weakly infrared-active, by virtue its **Coriolis** interaction with ν_4 . Quantum-number assignments are based on the **results** of **Dang** Nhu (1969) who developed a fourth-order theory and applied it to **unpublished** spectra of moderately high resolution. Spectroscopic **parameters** are listed in Table 22.

High-resolution **spectra** of $v_2 + v_4$ and 2 v_4 are available in the region of approximately 2450 to 3200 cm⁻¹ (Plyler et al, 1960; and Hall, 1973). Quantum-number assignments for 2 v_4 have been made on the basis of a third-order theoretical analysis. A partial analysis of $v_2 + v_4$ has been **done** in **analogy** with the quantum-number assignments in the work of (Bregier, 1970; and Hilico, 1970), on $v_2 + v_3$. Spectroscopic parameters for $v_2 + v_4$ and $v_4 = v_4$ are given in **Tables 25** and $v_4 = v_4$ respectively.

Table 22. Spectroscopic Parameters* for ν_2 of $^{12}\mathrm{CH_4}$

| Parameter | Value (cm ⁻¹) |
|-----------|---------------------------|
| V2 | 1533.289 |
| B2 | 5.319 |
| B0 | 5.230 |
| d2 | 5.7x10-5 |
| d0 | 2.1x10-5 |
| 22 | 2.9x10-2 |
| f2 | -5.2x10 ⁻³ |
| e2 | -2.8x10 ⁻⁵ |
| e2 | -5.0x10-6 |

*Dang Nhu (1968)

Table 23. Spectroscopic Parameters* for ν_3 of $^{13}{\rm CH}_4$

| Parameter | Value (cm ⁻¹) |
|------------------------------------------------------|----------------------------|
| $\nu_{_{ m O}}$ -2(B ζ_{3})eff | 3009.05+0.03 |
| $B_o^{+B_{eff}^{P,Q}-2(B\zeta_3)}$ eff | 9.963 <u>+</u> 0.004 |
| $B_{\mathrm{eff}}^{\mathrm{P,R}}$ - B_{O} | -0.0386 <u>+</u> 0.0008 |
| 2(D _o +D ₁) | $(4.2\pm0.4)\times10^{-4}$ |
| D _o -D ₁ | $(2.1\pm0.5)\times10^{-5}$ |
| å ₃ | 0.046t0.005 |
| ${\scriptscriptstyle D}^{J^{\boldsymbol{\tau}}}$ | $(4.7\pm2.8)\times10^{-5}$ |
| d ^J ₹ | $(5.4\pm1.7)\times10^{-5}$ |

*McDowell (1966)

Table 24. Spectroscopic Parameters* for v_4 of 13 CH $_4$

| Parameter | Value (cm⁻¹) |
|----------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ν ₄ Β' Β' D ξ F4s to 44 t134 t224 | $1297.88+0.02$ $5.179+0.005$ $5.194+0.005$ $(1.16+0.02)\times10^{-4}$ $0.477+0.005$ $(2.26+0.02)\times10^{-3}$ -4.5×10^{-6} $(4.84+0.02)\times10^{-4}$ $(-1.46+0.01)\times10^{-2}$ |

*Kyle et al, (1970)

Table 25. Spectroscopic Parameters* for ${\it v}$ 2t ${\it v_4}$ of $^{12}{\rm CH_4}$

| Parameter | Value (cm") |
|---------------------------|-------------|
| ν _o (Q) | 2818, 2838 |

*Hiliev (1970) - Further analysis, including that of the interaction between $\mathbf{F_1}$ and F2 substates, is necessary in **order** to obtain more complete values of spectroscopic parameters.

Table 26. Spectroscopic Parameters* for 2 $\pmb{v_4}$ of $^{12}\mathrm{CH}_4$

| Parameter | Value (cm-') |
|-----------------|------------------------|
| ε | 2600.29 |
| B | 5.175 |
| Bζ | 2.520 |
| D | 1.0x10-4 |
| G ₄₄ | 3.1 |
| g | 1.837x10 ⁻² |
| h | 6.579x10 ⁻⁴ |

*Fox (1962)

4.6.2 LINE INTENSITIES

Although it is recognized that it would be desirable to include in the data compilation all methane lines whose absolute intensity exceeds the cutoff specified in Table 3, it has not been possible to achieve this goal because of present experimental and theoretical limitations.

Absolute intensities for the allowed lines in ν_3 of $^{12}\mathrm{CH_4}$ were calculated, starting from the measured values for $\mathrm{R}(0)$; $\mathrm{R}(1)$, and $\mathrm{R}(2)$. The relative intensities of forbidden lines (Barnes et al, 1972) were used for calculating their absolute intensities. The absolute line intensities for ν_3 of $^{13}\mathrm{CH_4}$ were calculated on the basis of those for ν_3 of $^{12}\mathrm{CH_4}$, together with the terrestrial $^{12}\mathrm{C}/^{13}\mathrm{C}$ ratio (see Table 4). Calculated and/or measured absolute band intensities are listed in Table 18.

Absolute line intensities for ν_4 have been calculated on the basis of the measured values for R(0), R(1), and R(2). For $^{13}\text{CH}_4$, absolute intensities were calculated as for ν_3 . Absolute band intensities are given in Table 18.

Absolute line intensities for ν_2 , have been calculated on the basis of theoretical relative-line intensities and the experimental absolute band intensity in Table 18.

Absolute -line intensities for $\nu_2 + \nu_4$ were determined from the solar spectra of Hall (1972), with an assumed CH_4 air mass of approximately 4×10^{19} molecules/cm² and an assumed temperature of $273^{\circ} K$ and a pressure of 0.65 atm.

Absolute line intensities for $2\nu_4$ were calculated from the relative intensity formula of Fox (1962) together with the absolute band intensity in Table 18. The latter intensity was taken to be approximately 1 /100 of that for ν_3 of $^{12}{\rm CH}_4$.

4.6.3 LINE WIDTHS

The J- and T-dependence of methane line widths is taken from the results of Varanasi et al, (1971, 1972) and Tejwani and Varanasi (1971). The only measured values of air -broadened CH_4 half-widths are for multiples of ν_3 and $2\nu_3$ at $T=295^{\circ}K$. For $J\approx1$ to 5, $\gamma^{\circ}\approx0.061$ cm $^{-1}$ atm $^{-1}$; for $J\approx15$ to 17, $\gamma^{\circ}\approx0.048$ cm $^{-1}$ atm $^{-1}$. These results agree with values calculated from Y $^{\circ}$ for CH_4-0_2 , assuming N_2 and 0_2 with their partial pressures in air. Measurements and calculations of Yo for CH_4-H_2 in ν_4 suggest, but do not prove directly, that Y $^{\circ}$ may be independent of vibration-rotation band. For the purpose of the present data compilation, we adopt the value $\gamma^{\circ}=0.055$ cm $^{-1}$ atm $^{-1}$ for all CH_4 lines. There are no results available for the T-dependence of γ° for CH_4 -air or even CH_4-N_2 or CH_4-0_2 broadening. From the calculations and measurements for CH_4-H_2 broadening with T, we assume the usual $T^{-1/2}$ dependence. In conclusion, for the present data compilation, we

$$\gamma^{\circ} = 0.055 \left(\frac{296}{T}\right)^{1/2} \left(\frac{p}{1 \text{ atm}}\right). \tag{16}$$

4.7 Oxygen

The infrared atmospheric bands of oxygen have been interpreted by Van **Vleck** as magnetic dipole transitions between intersystem electronic combinations, a singlet-triplet transition $\mathbf{a}^1\Delta_{\mathbf{g}}\mathbf{-X}^3\Sigma_{\mathbf{g}}$. The A $\mathbf{v=0}$ (0,0) band at 7882.39 cm $^{-1}$ (1.27 μ m) has an Einstein A coefficient of $\mathbf{1.9x10^{-4}\,sec^{-1}}$ Jones and Harrison (1958). The (0,0) band, and the weaker (1,0) band at 9365.89 cm $^{-1}$ have been observed in terrestial atmospheric absorption by Herzberg and Herzberg (1947). The (0,1) band at 6325.99 cm $^{-1}$ has been observed in the twilight $\mathbf{airglow}$ emission by Jones and Harrison (1958). In addition to these bands there is an electric \mathbf{quad} -rupole ($\mathbf{b}^1\Sigma_{\mathbf{g}}^+\mathbf{a}^1\Delta_{\mathbf{g}}$) transition at 1.908 μ m that has been detected in the emission spectrum of a $\mathbf{discharge}$ through $\mathbf{0_2}$ and helium (Noxon, 1961). Finally, $\mathbf{submillimeter}$ -wave rotational transitions ($\mathbf{McKnight}$ and Gordy, 1968) and spin reorientation spectra (Zimmerer and Mizushima. 1961) at 60 GHz have been observed in the ground electronic state. The (\mathbf{a} - \mathbf{x}) system and the microwave spectra are discussed below. The atmospheric "A" band at 7619Å, representing the magnetic dipole transition $\mathbf{b}^1\Sigma_{\mathbf{g}}^+\mathbf{-x}^3\Sigma_{\mathbf{g}}^-$, is also included (Wark and \mathbf{Mercer} , 1965; \mathbf{Burch} and Gryunak, 1967)

With the molecular rotational momentum designated by \mathbf{K} and the electronic spin vector by \mathbf{S} , the total angular momentum \mathbf{J} is given by

J=K+S.

Thus, for the singlet-delta state \mathbf{J} = \mathbf{K} , and the energy levels, apart from the vibration, are given by

$$F = B_v K(K+1) - D_v K^2 (K+1)^2,$$
 (17)

where $\mathbf{B_v}$ is the rotational constant and $\mathbf{D_v}$ is the first order centrifugal distortion constant for the particular vibrational state. The constants for this state, obtained from measurements of the infrared bands, are listed in Table 27.

The expressions for the rotational energies **of** the rho-type triplet are obtained from a solution of the Hamiltonian (West and Mizushima, 1966):

$$H = B K^{2} + \frac{2}{3} \lambda (3S_{z}^{2} - S^{2}) + \mu K \cdot S.$$
 (18)

where A is the spin-spin interaction coupling constant and μ is the spin-rotation interaction coupling constant.

| Table 27. Constants of the ¹ 4 | d g State of 0 2 | (Herzberg and | Herzberg, | 1947) |
|-------------------------------------------|--------------------------------|---------------|-----------|-------|
|-------------------------------------------|--------------------------------|---------------|-----------|-------|

| Constant | Value (in cm ⁻¹) |
|---------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------|
| B _o B ₁ D _o ω _e ω _{ex_e} ΔG ν _ε 1/2 | 1.41783 1.4007 4.86x10 -6 1509.3 12.9 1483.50 7918.134 |

Centrifugal stretching effects are approximately corrected for by assuming a K(K+1) dependence for B. A and μ , namely:

$$B = B_{v} - D_{v}K(K+1) + H_{v}K^{2}(K+1)^{2},$$

$$\lambda = \lambda_{o} - \lambda_{1}K(K+1), \text{ and}$$

$$\mu = u_{o} - \mu_{1}K(K+1).$$
(19)

For each value of the quantum number at end-over-end rotation, K, the triplet energies are given by $F_1(K)$, $F_2(K)$, and $F_3(K)$ where J = K+1, J=K and J=K-1, respectively. Both $F_1(K)$ and $F_3(K)$ average about 2 cm⁻¹ lower than the $F_2(K)$ component. Values for the constants of the triplet-sigma state, obtained from both infrared and microwave measurements, are given in Table 28.

The band centers are given by

$$G(\mathbf{v}',\mathbf{v}'') = \mathbf{v}_{e} + \omega_{e}'(\mathbf{v}'+1/2) - \omega_{e}'\mathbf{x}_{e}'(\mathbf{v}'+1/2)^{2} + \dots - \omega_{e}''(\mathbf{v}''+1/2) + \omega_{e}''\mathbf{x}_{e}''(\mathbf{v}''+1/2)^{2} - \omega_{e}''\mathbf{y}_{e}'(\mathbf{v}''+1/2)^{3} + \omega_{e}''\mathbf{z}_{e}''(\mathbf{v}''+1/2)^{4} + \dots,$$
(20)

where the prime and double primes refer to the singlet and triplet states respectively.

The selection rules for magnetic dipole radiation are

$$\Delta J = 0, + 1$$

and

| Constant | Reference | Value (cm ⁻¹) |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| B ₀ B ₁ D ₀ D ₁ H ₀ λ ₀ λ ₁ μ ₀ μ ₁ ω _e ω _e y _e ω _e z _e Δ _{G₁/2} | a b b b c c c c b b | 1.4376809 1.421979 4.913x10-6 4.825x10-6 3.0x10-10 1.9847530 -1.950x10-6 -8.42930x10-3 8.01x10-9 1580.3613 12.0730 5.46x10-2 |
| ω _e z _e ΔG _{1/2} | b b | -1.43x10-3 1556.3856 |

Table 28. Constants for the ${}^{3}\Sigma_{\sigma}$ State of 0

- a. McKnight and Gordy (1968) b. Babcock and Herzberg (1948)
- c. West and Mizushima (1966)

The possible branches and the nomenclature used here for the ' $A_z - {}^3 \Sigma_g^-$ transition are shown in Table 27. Since the oxygen-16 nuclei obey Bose-Einstein statistics, only the positive rotational levels occur. In the ground state this causes an alternation of lines such that only odd values of the rotational quantum number K are present. For the heteronuclear isotopes of oxygen, however, all rotational levels occur; the $0^{17}0^{17}$ molecule has alternate rotational levels with nuclear statistical weights of 5 and 7 (Gordy et al, 1953). In $0^{16}0^{16}$ (and $0^{18}0^{18}$) there are four branches with $\Delta K=+1$, three with $\Delta K=0$, and two with $\Delta K=+2$, the latter branches being designated by superscripts S and 0. On the magnetic tape the six quantum numbers of the transition, v', J', K', v'', J'', K'', are given in the field of columns 38 through 62. In addition, the nine branches are listed in columns 64 and 65 with the superscript, representing the AK of the transition, preceding the AJ designation. A diagram indicating the transitions involved in the ${}^1\!\Delta_g - {}^3\Sigma_g^-$ band is given in Figure 1.

The above description generally applies to the microwave transitions of pure rotation and transitions between levels of the triplet state. In the latter the labelling is given as K+ and K-, designating the transitions $\mathbf{F_2(K)}$ - $\mathbf{F_1(K)}$ and $F_2(K) - F_3(K)$ respectively. Intensities have been calculated (see Townes and Schawlow, 1955). A good summary of the various bands of oxygen molecule can he found in the recent review article by Krupenie, 1972.

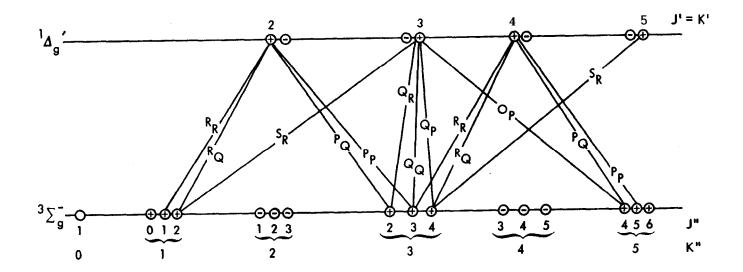


Figure 1. Transitions in the ${}^1\!\Delta_g - {}^3\!\varSigma_g^{\text{-}}$ Band of Oxygen

5. CONTINUOUS ABSORPTION BY ATMOSPHERIC GASES

Although not part of the data tape of primary concern in this report, a few words should be said about the relatively continuous regions of absorption of particular interest in the atmospheric "windows" near 2500 cm⁻¹(4 μ m), from approximately 1250 cm⁻¹ to 700 cm⁻¹(8 μ m - 14 μ m), and near 450 cm⁻¹ (22 μ m) In other spectral regions the contribution by nearby absorption lines is much greater than that by the continuum absorption, so that for practical purposes the continuum effect can be neglected, although it may be greater than in the windows.

This continuous absorption is caused by one or more of the following three processes: (1) extreme wings of strong collision-broadened absorption lines centered more than $10-20\,\mathrm{cm}^{-1}$ away; (2) pressure induced absorption resulting from transitions that are forbidden for unperturbed molecules; and (3) the possible existence of the water dimer $(H_20;H_20)$ in the case of the 8 to 14 $\mu\mathrm{m}$ region.

The absorption coefficient due to continuum absorption can be expressed as

$$k = C_s P_s + C_b P_b$$
 (22)

where $\mathbf{C_s}$ is the self-broadened coefficient and $\mathbf{C_b}$ is the foreign gas broadening coefficient, $\mathbf{P_s}$ is the partial pressure of species, s, and $\mathbf{P_b}$ is the foreign gas pressure.

Figure 3 gives the spectral dependence of $\mathbf{C_s}$ for water vapor absorption in the 8 to 14 μ m region for three temperatures (Burch, 1970). The $\mathbf{C_b}$ value has been most reliably measured by McCoy et al, 1969, and is found for nitrogen to be $\mathbf{C_b}$ = 0.005 $\mathbf{C_s}$ at room temperature.

Figure 2 gives the spectral dependence of $\mathbf{C_s}$ for the water vapor absorption in the region near 4 μm for four different temperatures (Burch et al, 1971a). Note that the $\mathbf{T=296}^{\mathbf{O}}\mathbf{K}$ curve is an extrapolation based on the measurements at higher temperature. These same workers found the ratio $\mathbf{C_b/C_s}$ for nitorgen broadening to be 0.12 + 0.03.

Figure 4 gives the spectral dependence of the absorption coefficient due to the pressure-induced nitrogen absorption centered near 2330 cm⁻¹(Burch et al, 1971a) Measurements have also been made by Shapiro and Gush, 1966, and Farmer and Houghton, 1966. Since the foreign gas broadening in this case results from a gas (oxygen) having a constant mixing ratio in the atmosphere, Eq. (22) reduces to

$$K = Const. x P$$
 (23)

Since the nitrogen abundance in the atmosphere is also directly proportional to P, the absorption depends on P^2 and Figure 4 has as ordinate the absorption coefficien expressed in the units atm⁻² Km⁻¹.

Since line wings as given by the Lorentz shape, Eq. (1), have been found to be in error in **the** extreme wings, an appropriate rule to follow for the truncation of

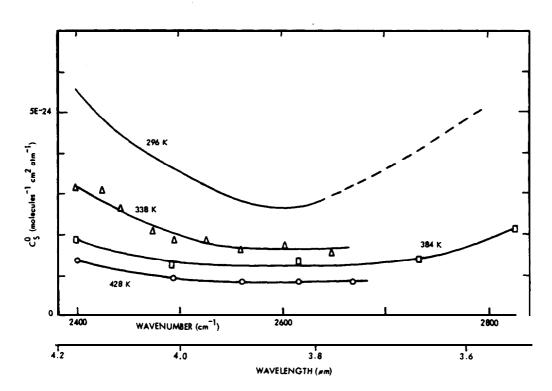


Figure 2. Normalized Continuum Absorption Coefficient for $\mathbf{H_2O}$ at Three Temperatures

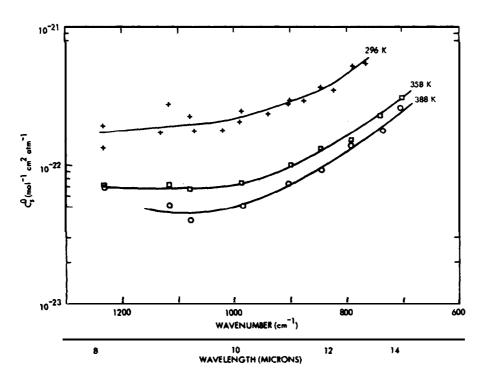


Figure 3. Normalized Continuum Absorption Coefficient Between 2400 and 2820 cm $^{-1}$ for Pure ${
m H_2O}$ at Four Temperatures

line wings and the introduction of continuum absorption coefficients in accordance with Figures 2 through 4 is difficult to state. It is recommended that the user familiarize himself with this problem (see, for example, **Burch** et al, 1969) and in any case the use of the Lorentz shape beyond 20 or 30 wavenumbers of line centers is inappropriate (see also discussion on line shape on p. 3).

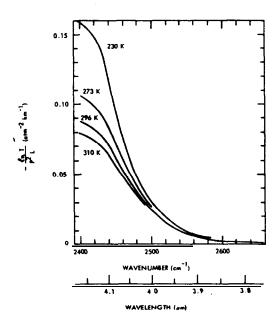


Figure 4. Spectral Plot of Absorption Coefficient for Atmospheric ${\bf N_2}$ at Four Temperatures

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Appendix A

Computer Program Listing for Reading Tape

```
PROGRAM RU TP( INPUT. OUTPUT. TAPE2)
    DIMENSION R (400) .TT (15)
     A=U
    IEOF=0
 24 BUFFER IN(2+0) (R(1) +R(340))
     IF (UNIT (2) ) 25+30+35
 J5 PRINT 36+TT(1)
 36 FORMAT (* PARITY ERROR AFTER *+F12.3)
     GO TO 24
 3 6 IEOF=IEUF+1
    PRINT +1+IEOF
 3 1 FORMAT (# EOF NO*+15)
      IF (IEOF.GT.7) SO TO 1001
      G 0 TO 4
 25 DECOJE (10,39,R(1)) IRED
 41 FORMAT(F10.3.E10.3.F5.3.F10.3.546.45.13.14.13)
     I = 1
  39 FORMAT(110)
    L=5
     0 0 40 K=1. IRED
     DECODE (80,41,9(L)) (TT(I),1=1,13)
     PRINT 41 (TT(1) , I=1 , 13)
     L=L+d
     IF(TT(1)+LT+A) PRINT 153+A+TT(1)
      A=TT(1)
153 FORMAT(* 0 U TOF DRDER *, 2F12.3)
  40 CONTINUE
     GO TO 24
1001 CALL EXIT
       s TOP
      END
```

Appendix **B**

computer Program for Homogeneous Path Transmittance Calculation

The computer program (Program LBL) provided in this Appendix is intended for use as a check to ensure that a user of the AFCRL Data Tape will be using the data correctly. The spectral region chosen for a sample spectrum (Figure 5) contains spectral lines from four different atmospheric gases. The program was constructed for use with constant pressure and temperature paths only, so the user will be left to his own devices for real atmospheric applications. After computing transmittance at closely spaced monochromatic frequencies, a convolution is performed over a triangular slit function whose half-width can be chosen. Comment cards have been used freely, so no further discussion of this program will be given here.

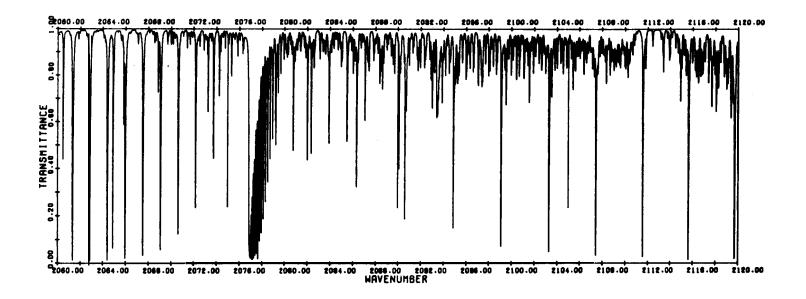


Figure B1

Synthetic Spectrum Generated using the Data Compilation. Conditions are as follows: pressure = 188 mb, T = 219K, W $_{20}$ = 2.00 x $_{10^{20}}$, $_{20}$ = 2.05 x $_{10^{21}}$, $_{20}$ = 3.23 x $_{20^{18}}$, $_{20}$ = 4.67 x $_{20}$ = 10.17. Lines belowing to other molecular species contained on tape are not present in this spectral region. Spectral resolution is 0.01 cm⁻¹.

 PROGRAM LBL(INPJT+0JTPUT+TAPEZ)
DIMENSION W(7), R(325), GNU(3000), S(3000), A_PHA(3000), EDP(3000)
DIMENSION MOL(3000), CAYI(7), OPD(3000), FNU(1000), TRANS(1000)
DIMENSION SUM1(7), CSZ(7)

PROGRAM BY R . MCCLATCHEY.

I F (VBOT.GE.5000.0) WFILE=4

N O PUNCHED DECKS WILL BEDISTRIBUTED.

THIS PROGRAM GENERATES 4 TRANSMITTANCE SPECTRJY WITH OUTPUT RESULTS PRINTED EVER Y DELW MAVENUMBERS BETWEEN THE INITIAL FREQUENCY.

VI, AND THE FINAL FREQUENCY, V2. CALCULATIONS A QEPERFORMED FOR A UNIFORM, CONSTANT PRESSURE. CONSTANT TEMPERATURE PATH CONTAINING ANY DRALL OF THE MOLECULAR SPECIES DESCRIBED IN THIS QEPDQT IN ARBITRARY AMOUNTS. MOLECULAR ABUNDANCES MUST BE SPECIFIED IN THE UNITS (MOLECULES/CM2). MONOCHROMATIC CALCULATIONS ARE MADE AT FREQUENCY INTERVALS, DV. AND A TRIANGULAR SLIT FUNCTION Of HALF-WIDTH, A, I S CONVOLVED WITH THE MONOCHROMATIC RESULTS.

IEOF=0 DEPTH=0.001 PI=3.14159 SUM=0%0 IV=1

READINPUT PARAMETERS (PERESSURE), (TETEMPERATURE), W(1)=H20, W(2)=CO2, W(3)=O3, W(4)=N20, W(5)=CO, W(6)=CH4, W(7)=O2, V1AND V2 ARE FREQUENCY LIMITS FOR WHICH OUTPUT RESULTS A? EREQUIRED. DVI S MONOCHROMATIC FREQUENCY INCREMENT.

BOUND IS THE FREQUENCY FROM 4 N Y LINE CENTER BEYOND WHICH THE LINE WILL BE NEGLECTED.

A ISTHE HALF-WIDTH OF 4 TRIANGULAR SLIT FUNCTION.

DELVIS FREQUENCY IY CREYENT OF CONVOLNED OUTPUT TRANSMITTANCE RESULTS.

READ 77+P+T PRINT 77, P.T READ 81+ (W(M)+M=1+7) PRINT 83 PRINT AL, (W(M), M=1,7) READ 85, VI, VZ, DV, BQUND, A, OELV VISUA COUDE VC - SV - 18 TRISH IF (A+2/UV+1.GT.3000) CALCULATION CANNOT BE DONE IF THERE A R E MORE THAN 3 0 0 0 LINES READ FROM TAPE I $\,{
m V}$ 4 FREQUENCY RANGE O F 2(A+30U0D) CALCULATION CANNOT 3E DONE OVUOB-A-1V=TOBV VTOP=V2+A+BOUND MFILE=9 I F (VBOT-GE-500-0) MF ILE=1 IF tVdor.GE.1000.0) MFILE=2 IF tVHol.GE.2000.0) MFILE=3

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MFILE DETERMINES THE NUMBER OF ENDS OF FILE TO BE READ OVER
C
      BEFORE COMING TO THE PERTINENT DATA ON THE TAPE.
      WE ARENOW READY TO READ TAPE.
      I = I
      ILL=1
      BUFFER IN (2+0) (R(1)+R(325))
1
      IF (UNIT(2)) 7,5,3
3
      PRINTHY GNU(I)
      GO TO 1
      IEOF=IFUF+1
      PRINT 91. IEOF
      IF (IEAF.GE.7) SO TO 75
      G o TO
      IF (MFILE.GT.IEOF) 30 TO 1
7
      DECODE (10,93,8(1) ) IREC
      NT= (B+14EC) -6
      DECODE (10,95,R(NT) )TMAX
      IF (TMAA.LT. VBOT) GO 1
      DO 9 K=1. IREC
      DECODE (60.95.R(L))GNU(I).S(I).ALPHA(I).EDP(I).IDAT.ISOT.MOL(I)
      IF (GNU(I).LT.V3OT) GO TO 9
      M=MOL([)
       PATH=S(1) +W(M)/(PI+0.06+P/1013.0)
      IF (PATH-LT-DEPTH) 30 TO 9
       IF (GNU(I).GT.VTOP) GO TO LL
       I = I + i
       CONTINUE
       I F (1.61.2960) 30 TO 11
       60 TO 1
       I1=[
11
       PRINT 97. VUOT. VTOP. GNU( I1). Il
       15=1
       A-C/U08-(11) U/D=95V
c
       TAPE HAS BEEN READ FOR ALL NECESSARY LINES OR FOR THE MAXIMUM NO. OF LINES POSSIBLE SUBJECT TO RECYCLING.
C
       HALFWINTHS WILL 3E SUPPLIED BELOW WHEN THEY DO NOT APPEAR
c
       ON TAPE.
       00 15 [= ]LL+II
       (I) JCM=M
       IF (4.E).1) GO TO 15
       IF (ALPHA(I).GT.0.0) GO TO 13
       IF (4.53.2) ALPHA(1)=0.07
       IF (4.63.3) ALPHA(I)=0.11
       IF (M.E3.4) ALPHA(I)=0.08
       IF (4.E3.5) ALPHA(1)=0.06
       IF (M.E3.6) ALPHA(I)=0.055
       IF (M.FQ.7) ALPHA(I)=0.048
IF (ALPHA(I).LT.0.01.0R.ALPHA(I).GT.1.0) ALPHA(I)=0.06
 13
```

```
15
      CONTINUE
IS=1
      P0=1013.00
      10=296.00
      CS1=(T0-T)/(T0+T+0.5946)
C
      ROTATIONAL PARTITION FUNCTION IS DEFINED BELOW
      Do 214=1,7
      IF (M.EQ.1) GO TO 17
IF (M.EQ.2) GO TO 19
     , IF (M.EQ.3) GO TO 17
      IF (M.EQ.4) GO TO 19
      IF (4.EQ.5) GO TO19
      IF (M.EQ.6) GO TO 17
      If (M.EQ.7) GO TO19
      CS2(4) = ((T0/T) **1.5)
17
      Go TO 2A
      CS2(4) = F0/T
19
      CONTINUÉ
CA= ((TO/T) ##0.5) #(P/P0)
51
      TEMPERATURE DEPENDENCE OF ALL LINE INTENSITIES COMPUTED HERE.
С
      00 23 I=ILL.II
      M=MOL([]
      S(1)=S(1)+CS2(M)+EX>(-EDP(1)+CS1)
      ALPHA(I) = ALPHA(I) +CA
23
      V=V1-A
      DO 27 M=1.7
25
      CAY1 (M) =0.0
27
      SUM1 (M) =0.0
      DETERMINE INDICES (15 AND 16) INDICATING WHICH SPECTRAL LINES
      ARE TO BE USED IN THE CALCULATION AT FREQUENCY V.
      Do 33 1=15.11
      IF (V-ROUND-GNU(I)) 29,29,33
IS=I
29
      Go TO 35
      CONTINUE
33
      15=I1
      Go TO 49
      D o 39 J=15,11
35
      IF (V+90UND-GNU(J)) 37,37,39
      16=J-1
37
      GO TO 43
      CONTINUE
39
      16=11
      COMPUTE THE OPTICAL DEPTH AND TRANSMITTANCE AT FREQUENCY V.
43
      00 45 1=15.16
      M=MOL(I)
```

```
Z=ABS (V=GNU(I))
      SUM1 (M) #S(I) #ALPHA(I)/(Z##2+ALPHA(I) ##2)
      CAYI (M) =CAYI (M) +SUMI (M)
      CONTINUE
45
       CAY=0.0
      Do 47 M≠1.7
      CAY=CAY+CAY1(M)+W(M)
47
      OPD(IV) =CAY+0.3183
       GO TO 51
      OPD(IV)=0.0
49
51
       OPD (IV) = EXP (-OP) (IV))
       IF ((V+QV).GT.V22) 30 TO 53
       IF (V.SE.V2+A) 50 TO 53
       IF (IV.9E.3000)30 TO 53
       VG+V=V
       Go TO 25
       AT THIS POINT, CYCLE BACK TO STATEMENT 25 AND COMPUTE THE
c
       MONOCHROMATIC TRANSMITTANCE AT V+3V+ETC.
c
       IF STATEMENT 53 IS REACHED • ALL POSSIBLE MONOCHROMATIC TRANSMITTANCE VALUES HAVE BEEN COMPUTED. AND THE SLIT FUNCTION CONVOLUTION WILL!
\mathbf{c}
\mathbf{c}
       NOW BE PERFORMED IN LOOP 57
\mathbf{c}
53
       FREQ=VI
       PRINT 101, IV.V.VZP
       FINAL=V1+3000.+DV-A-DELV
       V=V1-A
       JFNU=1
       L=DELV/9V+0.01
       IA=1
55
       SUM=0.0
       Do 57 [=IA.IV
       SUM=SUM+(A-ABS(V-FREQ))+OPD(T)
V=V+DV
       IF (V-(FREQ+A)) 57,59,59
57
       CONTINUE
       TRANS (JFNU) = SUM+DV/(A+A)
       FNU (JFNJ) =FREQ
       IF (FREQ.GT.V2) 30 TO 61
       IF (FREJ.GT.V2P) GO TO 51
        I F (FRE2.GE.FINAL) 30 TO 61
       FREQ=FREQ+DELV
        IF (JFNU.GE.1000) GO To 61
        JFNU=JFNU+1
        IA=IA+L
        V=FREQ-A
        SUM=0:0
        Go TO 53
        CONVOLVED TRANSMITTANCE RESULTS ARE NOW PRINTED OUT.
 c
        PRINT 103, JFNU
 51
        PRINT 104
```

```
PR.NT 105, (FNU(J) ,TRANS(J) ,J=1,JFNU)
      IF (FREQ.GE.V2) 30 TO 75
      IF (FREQ.GT.V2P) GO TO 57
      IF $JFNU.GE.1000) GO TO 65 IF (FREQ.GE.FINAL) 30 TO 63
      Go TO 75
      V1=FINAL+DELV
53
      15=1
      Iv=1
      JFNU=1
      V=V1-A
      GO TO?5
      IA=IA+L
55
      IF STATEMENT 65 IS REACHED. ADDITIONAL MONOCHROMATIC CALCULATIONS
c
      AREREQUIRED TO SATISFY THE TOTAL FREQUENCY RANGE OVER WHICH
      CONVOLVED RESULTS ARE REQUIRED.
C
       JFNU=1
      V=FREQ-A
      Go To 52
      Iv=1
67
C
       IF STATEMENT 67 IS REACHED, THE DATA FROM THE DATA TAPE WILL! BE
С
      REORGANIZED AND THE TAPE WILL BE READ AGAIN.
C
       JFNU=1
       V1=FRED
       GRUOR-A-1V=TOEV
       Do 6+[4=1+I1
       IF (GNU(IN).GT.V30T) GO TO 71
       CONTINUE
64
       IN=II
71
       IJ=IN
       L=1
       DO 73 [=IJ+II
       GNU(L)=GNU(I)
       S(L)=S(1)
       ALPHA(L)=ALPHA(I)
       EDP(L)=EDP(I)
       MOL(L)=40L(I)
L=L+1
73
       I =L
       ILL=L
       GO TOL
       CALL EXIT
7 o
       STOP
77
       FORMAT (E12.5.F7.2)
       FORMAT (* PRESSURE =*,E12.5,*TEMPERATURE =*,F7.2)
79
       FORMAT (7E10.3)
ġ1
       FORMAT (3x, +WATER+, 6x, +CO2+, 6x, +OZONE+, 7x, +N2O+, 7X, +CO+, 8x, +CH4+, 7
93
      1X,#02#,4X)
85 '
      FORMAT (6F10.3)
```

```
37
        FORMAT (* VA =+,F10.3,+V2 =+,F10.3,+DV=+,F10. 3,+BOUND =+,F10.3,+A
       1=+,F10.3.*DELV =*.F10.3)

FORMAT(* PARITY ERROR ENCOUNTERED AT*.F12.3)

FORMAT (* END OF FILE ENCOUNTERED*.I5)

FORMAT (I10)
97
91
93
        FORMAT (F10.3.E10.3.F5.3.F10.3.35X, I3.I4.I3)
FORMAT(*VBOT=*,F12.3.* VTOP =*,F12.3.*GNU=*,F12.3.* 11 ● 918)
95
97
         FORMAT (15,2F10.4)
101
        FORMAT (* JFNU **+15)
FORMAT (5(* FREQUENCY
103
                                                           • ))
104
                                           TRANs.
105
         FORMAT 15(F10.30E12.5))
```

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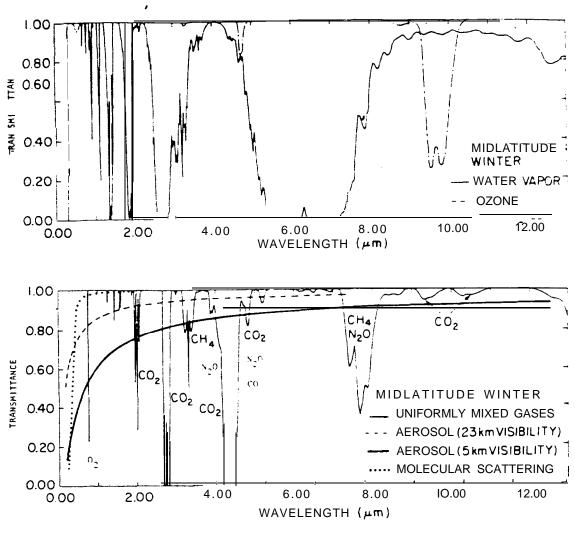


Figure 4. Vertical Path to Space From Sea Level for the Midlatitude Winter Model Atmosphere Showing the Separate Contributions to the Total Transmittance